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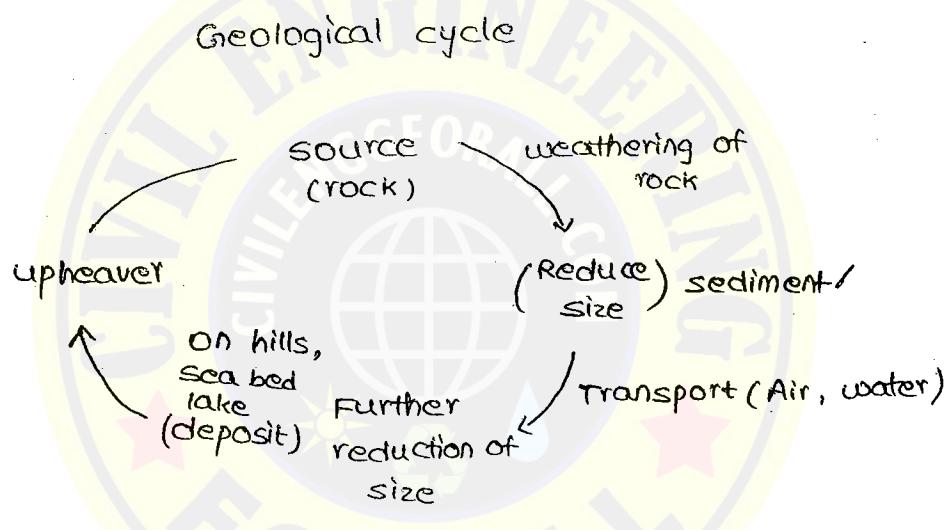
**CIVIL ENGINEERING STUDENTS AND GRADUATES**



UNIT - IORIGIN OF SOILS (1M)**Soil:-**

Soil is an assemblage of discrete (discollected) solid particles (organic or inorganic) with a composition of air and/or water occupying the void space among the particles.

The solid particles may be varying size and shape like clay soils, silt soils, gravel soil etc. may be a mixture.

**Formation of soils:-****Types of weathering:-**

1. physical weathering:-



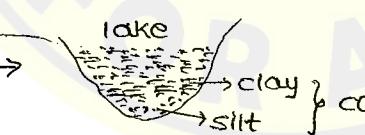
No change in chemical composition.

2. chemical weathering:-

1. size reduction takes place
2. change in chemical composition.
3. It results in fine grained and cohesive soils.

Agency /	deposited place	Name of soil
1. water	River (banks)	Alluvial (or) Fluvial soils (riversand)
2. water	Lake	Lacustrine soils (varved clay)
3. Water	sea	Marine soils (soft clays)
4. Air/wind	-	Aeolian soils → Loess (silt), sand dunes (Fine sand)
5. ICE/Glaciers	-	Glacier soils (Drift, Till)
6. Gravity	-	Colluvial soils (Talus).
Coarse grain soils		Fine grain soils
1. Sandy, Gravel		1. silt, clay (Rock floor → Stone dust)
2. 3-dimensional size		2. 2-Dimensional particle
3. gravity force predominate		3. surface charge predominate
4. friction is present ( $\phi$ )		4. cohesion is present ( $kN/m^2 = c$ )
5. pervious		5. less pervious.
6. specific surface area is low.		6. specific surface area is high

### Some important soils:-

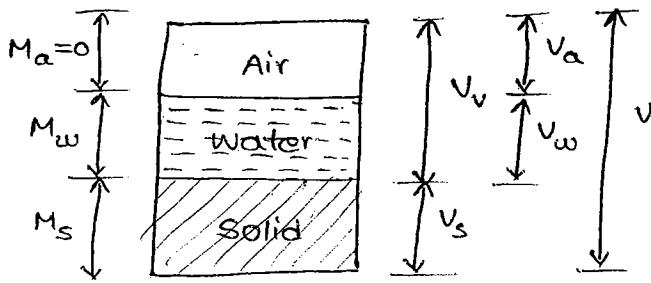
- Varved clay →  combination of these two is called varved soils.
- Moorum, → It is a gravel mixed with red clay.
- Loam → Mixture of sand, silt and clay (in equal proportion)  
(Triangular soil classification chart)
- Bentonite → It is a decomposed volcanic ash.  
It is a highly compressibility, swelling and shrinkage.

## UNIT - 2

### DEFINITION AND PROPERTIES OF SOILS (2M)

(2)

phase diagram :-



1. Void ratio (e) :-

$$e = \frac{\text{volume of voids}}{\text{volume of solids}} = \frac{V_v}{V_s}$$

- a.  $e_{cgs} < e_{fgs}$
- b.  $e < 1$  (coarse grain soils)
- c.  $e \leq 1$  (fine grain soils)
- d.  $e > 0$
- e.  $e = 0.91$  (max in spherical grains arranged in cubical array)
- f.  $e = 0.35$  (least in spherical grain arranged in diagonally)

2. porosity :- (n)

It is also called percentage of voids.

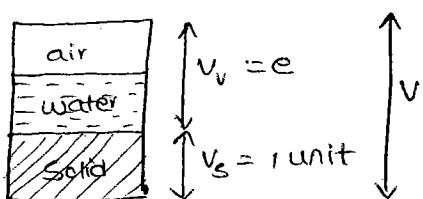
$$\% \text{ of voids} = n = \frac{\text{volume of voids} \times 100}{\text{total volume of soil}}$$

$$n = \frac{V_v}{V} \times 100$$

Range :  $0 < n < 100 \%$ .

Relation between 'n' and 'e' is

$$n = \frac{V_v}{V}$$



$$n = \frac{e}{1+e}$$

$$e = \frac{n}{1-n}$$

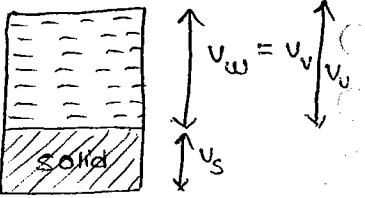
### 3. Degree of saturation ( $S$ ) :-

$$S = \frac{\text{volume of water}}{\text{volume of voids}} \times 100 \%$$

$$S = \frac{V_w}{V_v} \times 100 \%$$

For dry soil,  $V_w = 0$

$$\therefore S = 0 \%$$



For fully saturated  $V_w = V_v$

$$\therefore S = 100\% \text{ (or) } 1$$

Range:

$$\boxed{0\% \leq S \leq 100\%}$$

$$\boxed{0 \leq s \leq 1}$$

### 4. Air content ( $a_c$ ) :-

$$a_c = \frac{V_a}{V_v} \times 100 \%$$

For a saturated soil,  $V_a = 0$

$$\therefore a_c = 0\%$$

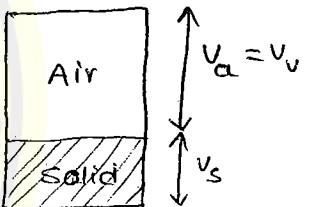
For dry soil,  $V_a = V_v$

$$\therefore a_c = 100\%$$

Range:

$$\boxed{0\% \leq a_c \leq 100\%}$$

$$\boxed{0 \leq a_c \leq 1}$$



Ex:-

$$\gamma_d = \frac{g \gamma_w}{1 + e}$$

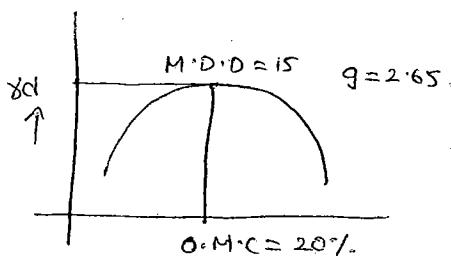
$$15 = \frac{2.65 (10)}{1 + e}$$

$$e = 0.76$$

$$\gamma_w = S \cdot e$$

$$2.65 (20\%) = S \cdot (0.76)$$

$$S = 70\% \Rightarrow S + a_c = 100\% \Rightarrow a_c = 30\%$$



## 5. percentage air voids ( $n_a$ ):-

$$n_a = \frac{v_a}{v} \times 100 \%$$

For saturated soil,  $v_a = 0$

$$\therefore n_a = 0\%$$

For dry soil,  $v_a = v_v$

$$\therefore n_a = \frac{v_v}{v} \times 100$$

$$\therefore n_a = n\%$$

Range :  $0 \leq n_a \leq n$

Relation :  $n_a = n \cdot a_c$

## 6. specific volume ( $v'$ ):-

$$v' = \frac{\text{Total volume}}{\text{volume of solids}}$$

$$v' = \frac{v}{v_s}$$

$$= \frac{v_v + v_s}{v_s}$$

$$= 1 + \frac{v_v}{v_s}$$

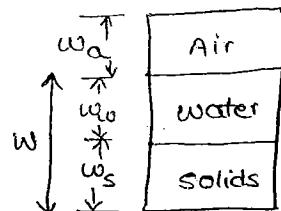
$$v' = 1 + e$$

## 7. water content (or) moisture content ( $w$ ):-

$$w = \frac{\text{weight of water}}{\text{weight of solids}} \times 100$$

$$w = \frac{w_w}{w_s} \times 100$$

$$w = \frac{w_{\text{dry wet}} - w_{\text{dry}}}{w_{\text{dry}}} \times 100$$



Range: greater than ( $w \geq 0$ )

sometime it can be greater than 100%.

### Methods of water content:-

#### 1. Oven dry method :-

Take 80gm of wet soil.

weight of container =  $w_1$

container + wet soil =  $w_2$

weight of dry soil + container =  $w_3$

After 24 hrs,  $105^{\circ}\text{C}$

$$\begin{aligned} W &= \frac{w_2 - w_3}{w_3 - w_1} \times 100 \\ &= \frac{w_{\text{water}}}{w_{\text{dry}}} \times 100. \end{aligned}$$

It is a laboratory method.

#### 2. pycnometer :- (Lab method)

It is also called density bottle method.

pycnometer  
(coarse)

- 1. sand
- 2. gravel
- 3. coarse aggregate
- 4. bitumen

density bottle  
(fines)

- 1. cement
- 2. clay
- 3. stone dust
- 4. Bentonite

Empty wt. of pycnometer =  $w_1$

pycnometer +  $\frac{1}{3}$  wet soil =  $w_2$

pycnometer + wet soil + water =  $w_3$

pycnometer + water only =  $w_4$

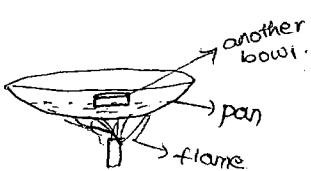
$$\text{Water content, } W = \left[ \frac{w_2 - w_1}{w_3 - w_4} \cdot \left( \frac{G_n - 1}{G_n} \right) - 1 \right] \times 100$$

↑  
sp. gravity  
 $G_n$  = solids

#### 3. Sand bath method :-

Empty wt. of container =  $w_1 = 80 \text{ gms}$

Container + wet soil =  $w_2 = 200 \text{ gms}$



Container + dry soil = 160 gm

(2)

$$\text{Water content, } w = \frac{200 - 160}{160 - 80} \times 100$$

$$w = 50\%.$$

#### 4. Torsion balance method:-

It is used in Research laboratories. It consumes more power.

#### 8. Specific gravity ( $G$ ):-

Specific gravity are two types:

1. True sp. gravity (or) sp. gravity of grains (or) sp. gravity of solids =  $G$  (or)  $G_s$  = constant.
2. Mass sp. gravity ( $G_m$ )

$$G = \frac{\gamma_{\text{solid}}}{\gamma_{\text{water}}} = \frac{w_{\text{solid}}}{w_{\text{water}}}$$

#### 9. Density ( $\rho$ ):-

$$\rho = \frac{\text{Mass}}{\text{Volume}} = \frac{g}{c.c}$$

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#### 10. Unit weight ( $\gamma$ ):-

$$\gamma = \frac{\text{Weight}}{\text{Volume}} = \frac{w}{v} \text{ KN/m}^3$$

$$\gamma = \rho \cdot g$$

buoyant (or) Effective  
(or)

$$\gamma'_{(\text{submerged})} = \gamma_{\text{sat}} - \gamma_{\text{dry}}$$

$$= 22 - 10 \Rightarrow 12 \text{ KN/m}^3$$

$$\gamma_{\text{solids}} = \frac{w_s}{v_s}$$

$$\gamma_{\text{solids}} = 27 \text{ KN/m}^3 > R.C.C \\ (24 \text{ KN})$$



$$\text{partially} \rightarrow \gamma_{\text{wet}} = \frac{w_{\text{wet}}}{v}$$

$$= \frac{w_s + w_w}{v}$$

$$\text{fully} \rightarrow \gamma_{\text{saturated}} = \frac{w_s + w_w}{v}$$

$$\gamma'_{\text{submersed}} < \gamma_{\text{dry}} < \gamma_{\text{wet}} < \gamma_{\text{saturated}} < \gamma_{\text{solids}}$$

$$w_{\text{solid}} = w_{\text{dry}} = 50 \text{ g}$$

$$v_s = \frac{\text{weight of water displaced}}{\gamma_{\text{water}}}$$

$$= \frac{w_w}{\gamma_{\text{water}}} \rightarrow 1.9 \text{ m/c.c}$$

## Some important relationships

$$\begin{aligned}
 1. \quad \gamma_{\text{saturated}}' &= \frac{\gamma_s + (\gamma_w + \sigma)}{\gamma_s + (\gamma_w + \gamma_a)} \\
 &= \frac{\gamma_s + \gamma_w}{\gamma_s + \gamma_v} \\
 &= \frac{\gamma_s (1 + \frac{\gamma_w}{\gamma_s})}{\gamma_s (1 + \frac{\gamma_v}{\gamma_s})} \\
 &= \gamma_s \frac{(1 + w)}{1 + e} \quad \sigma_s = \frac{\gamma_s}{\gamma_w}
 \end{aligned}$$

$$2. \quad \gamma_{\text{wet}} = \frac{\sigma \gamma_w (1+w)}{1+e} \rightarrow \textcircled{1} \quad (\text{partially saturated})$$

If water content is zero

$$\gamma_{\text{dry}} = \frac{\sigma \gamma_w}{1+e} \rightarrow \textcircled{2}, \text{ sub in eq } \textcircled{1}$$

$$\gamma_{\text{dry+wet}} = \gamma_{\text{dry}} (1+w)$$

$$\boxed{\gamma_{\text{dry}} = \frac{\gamma_{\text{wet}}}{1+w}}$$

$$3. \quad \gamma_{\text{sat}} = \frac{\sigma \gamma_w (1+w)_{\text{sat}}}{1+e}$$

$$= \frac{\gamma_w (\sigma + \sigma w_{\text{sat}})}{1+e}$$

$$\boxed{\gamma_{\text{sat}} = \frac{\gamma_w (\sigma + e)}{1+e}}$$

$$\sigma w_{\text{sat}} = S_r \cdot e$$

$$\therefore \sigma w_{\text{sat}} = 1 \cdot e.$$

$\therefore S_r = 1$  for  
saturated

$$7. \quad \gamma' = \gamma_{\text{sat}} - \gamma_{\text{water}}$$

$\gamma'$  = submerged

$$= \left[ \left( \frac{\sigma + e}{1+e} \right) \gamma_w \right] - \gamma_{\text{water}}$$

$$= \gamma_w \left[ \frac{\sigma + e}{1+e} - 1 \right]$$

$$\boxed{\gamma' = \gamma_w \left( \frac{\sigma - 1}{1+e} \right)}$$

$$8. \gamma_{wet} = \gamma = \gamma_d(1+w)$$

$$= \left( \frac{\gamma_w}{1+e} \right) (1+w)$$

$$= \frac{\gamma_w}{1+e} (G + Gw)$$

$$\boxed{\gamma_{wet} = \frac{\gamma_w}{1+e} (G + Ge)}$$

(S)

$$9. \gamma_{wet} = \gamma_{dry} + s(\gamma_{sat} - \gamma_{dry}) \Rightarrow$$

$$\gamma_{sat} - \gamma_{dry}' = \left( \frac{G+e}{1+e} \right) \gamma_w - \frac{G\gamma_w}{1+e}$$

proof:-

$$\frac{\gamma_w}{1+e} (G+Ge) = \gamma_{wet}$$

$$\gamma_{sat} - \gamma_{dry}' = \frac{e\gamma_w}{1+e} \therefore$$

$$\frac{\gamma_w G}{1+e} + \frac{\gamma_w \cdot Ge}{1+e} = \gamma_{wet}$$

$$\gamma_{dry} + s \left( \frac{e}{1+e} \right) \gamma_w = \gamma_{wet}$$

$$\boxed{\gamma_{dry} + s [\gamma_{sat} - \gamma_{dry}] = \gamma_{wet}}$$

For  $s=0$  (for dry soil)

$$\gamma_{dry} = \gamma_d$$

For  $s=100\%$ . (fully saturated soil).

$$\gamma_{sat} = \gamma_{dry} + l(\gamma_{sat} - \gamma_d)$$

10.

$$\boxed{\gamma_{dry} = \frac{(1-n_a) G \gamma_w}{1+Gw}}$$

11.

$$e = \frac{V_v}{V_s}$$

$$w = \frac{w_w}{w_s}$$

$$\boxed{e = \frac{V_v}{V_s} = V_v}$$

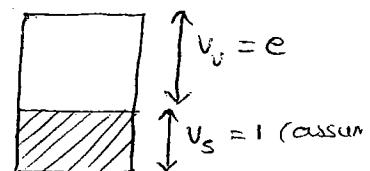
$$w = \frac{\gamma_w \cdot V_w}{\gamma_s \cdot V_s}$$

$$s = \frac{V_w}{V_v} = \frac{V_w}{e}$$

$$= \frac{\gamma_w \cdot V_w}{\gamma_s \cdot (1)}$$

$$es = V_w$$

$$w = \frac{V_w}{(\frac{s}{e} \cdot \gamma_w)} = \frac{V_w}{G_s}$$



∴

$$\boxed{es = w G_s}$$

$$V_w = w G_s$$

$$12. \quad \gamma_{dry} = \frac{w_{dry}}{v} = \frac{G \gamma_w}{1+e}$$

$$\gamma_{d_1} v_1 = \gamma_{d_2} v_2$$

$$\frac{\gamma_{d_1}}{\gamma_{d_2}} = \frac{v_2}{v_1} \rightarrow ①$$

$$\gamma_{d_1} v_1 = \gamma_{d_2} v_2$$

$$\gamma_{d_1}(1+e_1) = \gamma_{d_2}(1+e_2)$$

$$\gamma_{d_1}(1+e_1) - \gamma_{d_2}(1+e_2) \rightarrow ②$$

$$\boxed{\frac{v_1}{v_2} \propto \left( \frac{1+e_1}{1+e_2} \right)}$$

P.Q No:- 9

5 :-  $e = 1$  (Before compaction)

$e = 0.6$  (After compaction)

$$\frac{v_{BC}}{v_{AC}} = \frac{1+e_{BC}}{1+e_{AC}}$$

$$v_{AC} = v_{BC} \left( \frac{1+e_{AC}}{1+e_{BC}} \right)$$

$$= v_{BC} \left( \frac{1+0.6}{1+1.0} \right)$$

$$v_{AC} = 0.8 v_{BC}$$

P.Q No:- 8

$$11. \quad n = 50\% = 0.05$$

$$15. \quad e = 0.5$$

$$e = \frac{n}{1-n}$$

$$= \frac{0.5}{1-0.5}$$

$$e = 1$$

$$n = \frac{e}{1+e}$$

$$= \frac{0.5}{1+0.5}$$

$$n = \frac{5}{15} = 0.333$$

Additional questions:-

(6)

P.g No :- 9

$$1. \quad r_{\text{bulk}_1} = 1.8 \text{ gm/c.c.} \quad w_1 = 5\%, \quad e = \text{constant}$$

$$r_{\text{bulk}_2} = ? \quad w_2 = 10\%$$

$$r_{\text{bulk}} = r_{\text{dry}} (1+w)$$

$$r_{\text{bulk}_1} = \frac{G \cdot r_w}{1+e} (1+w_1)$$

$$r_{\text{bulk}_2} = \frac{G \cdot r_w}{1+e} (1+w_2)$$

$\therefore$  If void ratio is const  
 $r_{\text{dry}}$  also constant

$$\Rightarrow \frac{r_{\text{bulk}_{21}}}{r_{\text{bulk}_1}} = \frac{G \cdot r_w}{1+e} (1+w_1)$$

$$r_{\text{bulk}_2} = \frac{G \cdot r_w}{1+e} (1+w_2)$$

$$\Rightarrow r_{\text{bulk}_2} = r_{\text{bulk}_1} \left( \frac{1+w_2}{1+w_1} \right)$$
$$= 1.8 \left( \frac{1+0.1}{1+0.05} \right)$$

$$r_{\text{bulk}_2} = 1.88 \text{ gm/c.c.}$$

(or)

$$r_{\text{bulk}_1} = r_d (1+w_1)$$

$$1.8 = r_d (1+0.05)$$

$$r_d = 1.71 \text{ gm/c.c.}$$

$$r_{\text{bulk}_2} = r_d (1+w_2)$$

$$= 1.71 (1+0.1)$$

$$= 1.88 \text{ gm/c.c.}$$

3. Given /  $\alpha = 2.5$ ,  $e = 1$

$$\frac{\gamma_{sat}}{\gamma'} = \frac{\left(\frac{\alpha+e}{1+e}\right) \gamma_w}{\left(\frac{\alpha-1}{1+e}\right) \gamma_w}$$

$$= \frac{\alpha+e}{\alpha-1}$$

$$= \frac{2.5+1}{2.5-1}$$

$$\frac{\gamma_{sat}}{\gamma'} = 2.3$$

4.  $r_{bulk} = 2.4 \text{ gm/c.c.}$

$$w = 20\%$$

$$r_d = \frac{r_b}{1+w}$$

$$= \frac{2.4}{1+0.2}$$

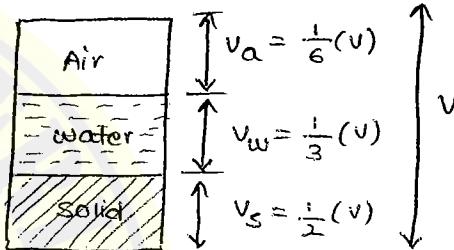
$$= \frac{2.4}{1.2}$$

$$r_d = 2 \text{ gm/c.c.}$$

$$6. v_v = v_a + v_w \\ = \left(\frac{1}{6} + \frac{1}{3}\right) v \\ = \frac{1}{2} v$$

$$e = \frac{v_v}{v_s} \\ = \frac{\frac{1}{2} v}{v} \\ = \frac{1}{2} v$$

$$e = 1$$



$$7. v_v = v_s$$

$$e = \frac{v_v}{v_s} = 1$$

$$\rho = \frac{e}{1+e} = \frac{1}{1+1} = 0.5$$

previous A.P.P.S.C. questions:-

P.Q NO:- 9

$$1. w = 10\%, s_r = 90\%, \alpha = 2.7, \gamma_{dry} = ?$$

$$\gamma_{dry} = \frac{\alpha \gamma_w}{1+e}$$

$$e = \frac{w\alpha}{s} = \frac{0.1(2.7)}{0.9} = 0.3$$

$$\gamma_{dry} = \frac{2.7(10)}{1+0.3} = \frac{27}{1.3}$$

(7)

$$\gamma_{dry} = 20.76 \text{ kN/m}^3$$

$$2. n = 20\%$$

$$c = \frac{n}{1-n}$$

$$= \frac{0.2}{1-0.2} = \frac{0.2}{0.8} = \frac{1}{4} = 0.25$$

$$3. w = 15\% \quad \gamma_G = 2.67 \quad c = 0.49 \quad s = ?$$

$$s \cdot c = \frac{\gamma_w}{\gamma_d}$$

$$s = \frac{\gamma_w}{c} = \frac{2.67(0.15)}{0.49}$$

$$= 0.817 \text{ or } 81.7\%$$

$$4. n = 45\% \quad V = 1 \text{ m}^3$$

$$n = \frac{V_v}{V}$$

$$(0.45 \times 1) = V_v$$

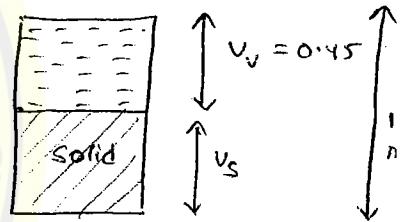
$$V_v = 0.45 \text{ m}^3$$

$$V_w = V_v = 450 \text{ lit}$$

$$r_w = \frac{m_w}{V_w}$$

$$M_w = 1000 (0.45) \text{ kg}$$

$$= 450 \text{ kg.}$$



$$6. \text{ Moist soil + tin lid} = 24 \text{ gms.}$$

$$\text{Empty wt. of tin lid} = 14 \text{ gms}$$

$$\text{Moist soil} = 24 - 14 = 10 \text{ gms}$$

$$\text{dry soil + lid} = 22 \text{ gms}$$

$$\text{Dry soil} = 22 - 14 = 8 \text{ gms}$$

$$w = \frac{w_{wet} - w_{dry}}{w_{dry}} \times 100$$

$$= \frac{10 - 8}{8} \times 100$$

$$w = 25\%$$

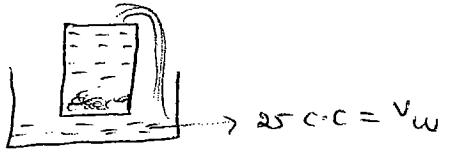
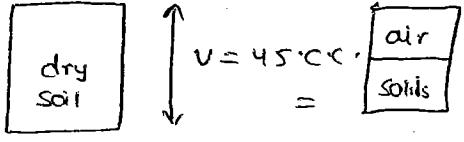
Ex:- A sampler with a volume of 45 c.c. is filled with dry soil sample. When the soil is poured into the graduated cylinder it displaces 25 c.c. of water. What is a void ratio of soil.

A) Given /  $V = 45 \text{ cm}^3$ ,  $V_s = 25 \text{ c.c.}$

$$e = \frac{V_v}{V_s}$$

$$= \frac{V - V_s}{V_s}$$

$$e = \frac{45 - 25}{25} = \frac{20}{25} = 0.8$$



Ex:- A saturated clay has water content of 39.3% and bulk sp. gravity of 1.84. The sp. gravity of soil and void ratio?

A.  $w = 39.3\%$ ,  $G_m = 1.84$  (bulk or mass)

$$e = \frac{wG}{s} \quad (\text{saturated}, s = 1)$$

$$e = \frac{1.84(0.393)}{1}$$

$$e = 0.723$$

$$G_m(\text{dry}) = \frac{\gamma_d}{\gamma_w}$$

$$G_m(\text{sat}) = \frac{\gamma_{\text{sat}}}{\gamma_w} \neq \frac{(G_m + e)}{1+e} \gamma_w$$

$$1.84 = \frac{\gamma_{\text{sat}}}{10} = \cancel{\left(\frac{G_m + e}{1+e}\right)}$$

$$\gamma_{\text{sat}} = 18.4 \text{ KN/m}^3$$

$$\gamma_w \left( \frac{G_m + e}{1+e} \right) = 18.4$$

$$\frac{G_m + e}{1+e} = \frac{18.4}{10}$$

$$G_m = 1.84(1+e) - e \Rightarrow 1.84(1+0.723) - 0.723$$

UNIT - 3
SOIL STRUCTURES AND CLAY MINEROLOGY (1 M)

Types of structures:-

1. Single grained structure:-

$$e_{c.g.s} < e_{f.o.s}$$

coarse grained soil

$$e_{sand} < e_{clay}$$

Fine grained soil.

1. When c.g.s material are arranged in loose packing the density is low and void ratio is maximum.

$$e_{max} = 0.91$$

void is taken in sand or gravel

$$e = 0.91$$

Loose packing

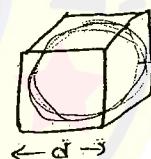
$$e_{dense} = 0.35$$

$$V_T = d^3$$

$$V_S = \frac{\pi d^3}{6}$$

$$V_V = V - V_S$$

dense packing



sphere is placed  
← d →

2. Honey comb structure:-

1. present in fine sands or silt.

2. Under vibrations and shocks, the structure collapse and large deformation takes place.

Clay Mineralogy:-

Kaolinite:-

1:1 clay mineral

Silica /  
Gibbsite / Alumina

1. Silica sheet and Gibbsite/Alumina sheet with equal proportion.
2. It is a stable mineral. No swelling and no shrinkage
3. China clay.

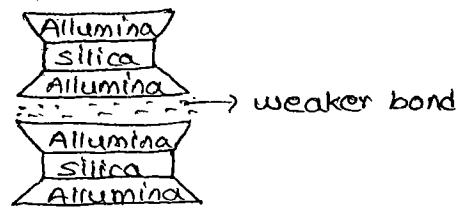
## Illite Mineral:-

1. It is a 2:1 clay
2. It exhibits medium swelling and shrinkage.

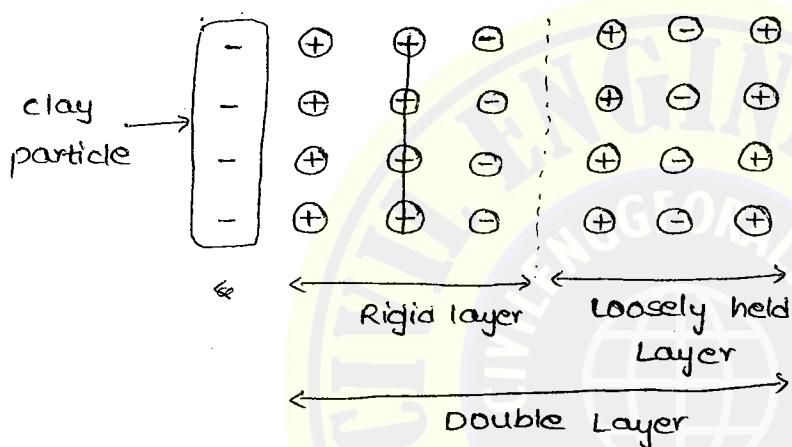
Gibbsite
Silica
Gibbsite

## Montmorillonite:-

1. It is a 2:1 clay
2. It exhibits large swelling and large shrinkage.



## Diffuse Double Layer and absorbed water:-



19-11-2011

UNIT - 4INDEX PROPERTIES OF SOILS (3M)

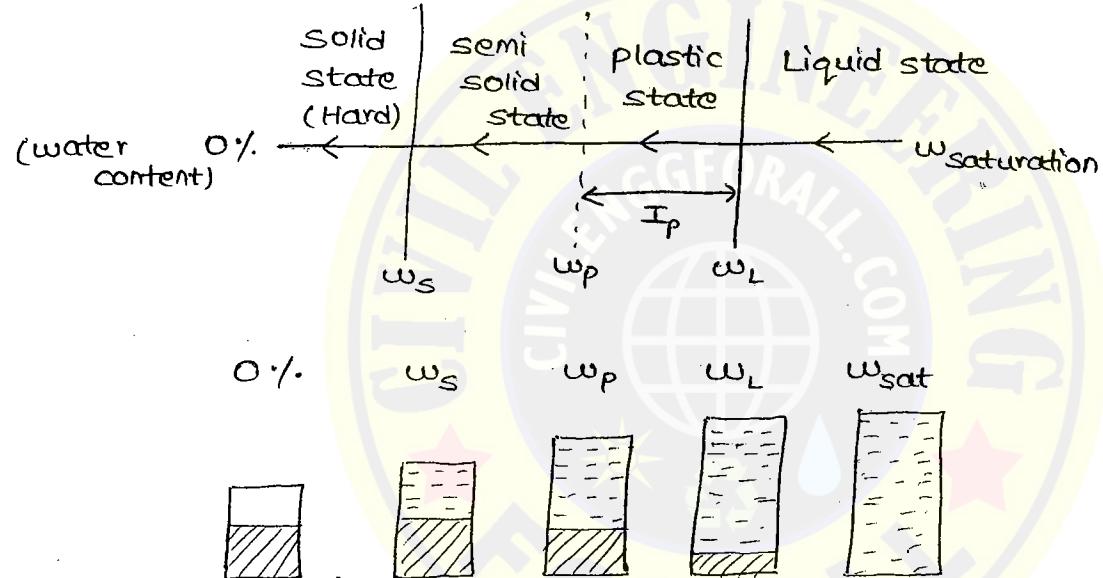
## Properties of soil

Index properties

Engineering properties

Index properties of Fine grained soils:-

Limit of consistency (Atterberg's limit):-

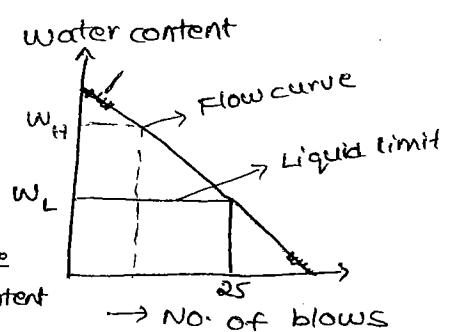


Liquid Limit:-

$$(\text{flow curve}) I_f = \frac{(w_1 - w_2)}{\log_{10} \left( \frac{n_2}{n_1} \right)} = \frac{(w_H - w_L)}{\log_{10} \left( \frac{N_H}{N_L} \right)}$$

$I_f$  = Flow index  
Grooving tool

H = Higher value  
of water content



ASTM



Used for silt

Casagrande

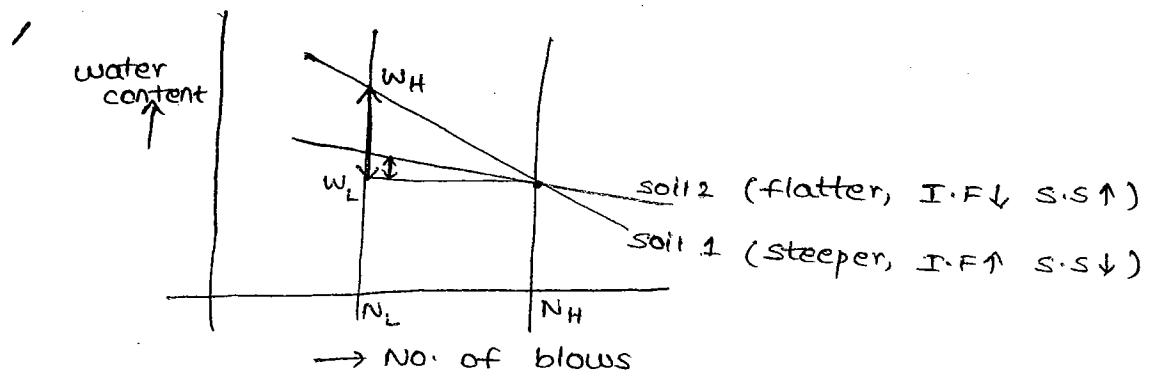


Used for sticky silts, (clays) or plastic

$$\therefore I_f \propto \frac{1}{\text{shear strength of soil}}$$

$$I.F \propto \frac{1}{S.S}$$

If I.F is increase, shear strength is decrease.



Fall cone test:-

- It is used for non plastic (or) silt (loose) and also plastic soils (or) clay (sticky silt).

Inorganic soils  $L.L < 50\%$

Organic soils of volcanic ash is High L.L

Fat clays  $L.L > 50\%$ . (% of clay is larger) (CH are fat clays)

Bentonite  $L.L \approx 786\%$ .

Plastic limit test:-

- soil passing  $425 \mu$

$$P.I = L.L - P.L$$

$$I_P = W_L - W_P$$

$I_P$  plasticity  
0 Non-plastic

(Lean clays - % of clays is less and silt is more)

$< 1'$  Low plastic (Lean clays, clays having a less sticky nature is called low plastic)

7-17 Medium plastic

$> 17$  Highly plastic

## Shrinkage limit test:-

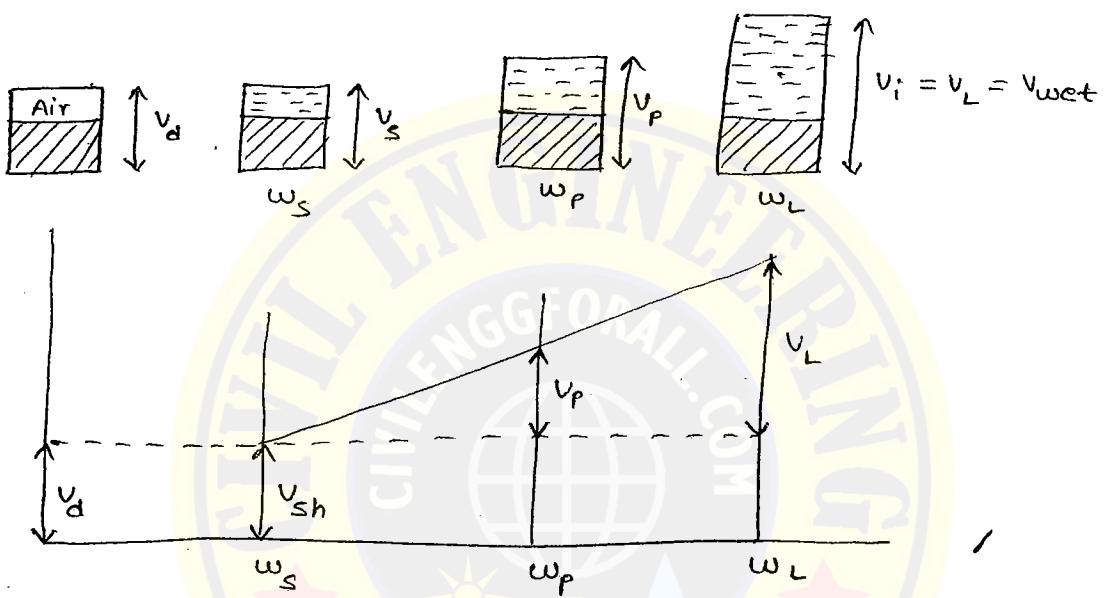
wt. of only dish =  $w_1$

wt. of wet soil + dish =  $w_2$

wt. of dry soil + dish =  $w_3$

$$w = \frac{w_2 - w_3}{w_3 - w_1} \times 100\%$$

$$w = \frac{w_w}{w_s} \times 100\%$$



(a)  $w_s = [w_i - \text{loss of water from } w_L \text{ to } w_s]$

$$= [w_i - \frac{(v_L - v_d) \cdot \gamma_w}{w_s}] \times 100$$

$$w_i = \frac{w_{\text{wet}} - w_{\text{dry}}}{w_{\text{dry}}}$$

$$(b) w_s = \frac{(v_d - v_s) \gamma_w}{w_s} \times 100$$

$$(c) w_s = \frac{(v_d - v_s) \gamma_w}{w_s}$$

$$v_s = \frac{w_s}{\gamma_s}$$

$$= \frac{\left(v_d - \frac{w_s}{\gamma_s}\right) \gamma_w}{w_s}$$

$$= \frac{v_d \gamma_w}{w_s} - \frac{\gamma_w}{\gamma_s}$$

$$= \frac{\gamma_w}{w_s} - \frac{\gamma_w}{\gamma_s}$$

$$\Rightarrow \left[ \frac{\gamma_w}{v_d} - \frac{\gamma_w}{\gamma_s} \right] \Rightarrow \left[ \frac{1}{(\gamma_d/\gamma_w)} - \frac{1}{(\gamma_s/\gamma_w)} \right]$$

$$\Rightarrow \left[ \frac{1}{\gamma_d} - \frac{1}{\gamma_s} \right]$$

$$d. \quad w_s = e/g$$

Shrinkage Ratio:-

$$S.R = \frac{\frac{\Delta v}{v_d} \times 100}{w_h - w_i}$$

$$S.R = \frac{\frac{(v_L - v_p)}{v_d} \times 100}{w_L - w_p}$$

Ex:-)

$$\begin{aligned} i) \quad S.R &= \frac{\frac{v_L - v_p}{v_d} \times 100}{w_L - w_p} \\ &= \frac{\frac{35 - 25}{15} \times 100}{65 - 35} \end{aligned}$$

$$S.R = 2.23$$

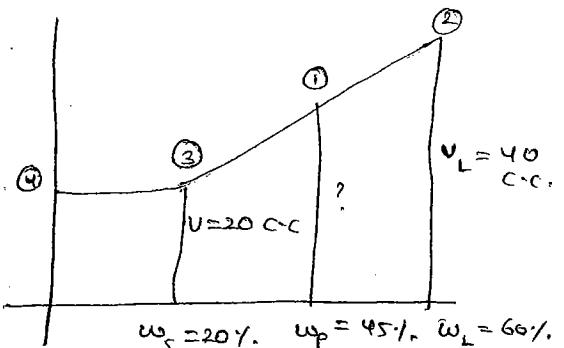
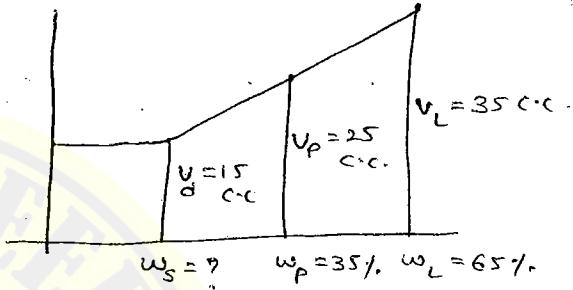
$$\begin{aligned} ii) \quad S.R^m &= \frac{\frac{v_p - v_s}{v_d} \times 100}{w_p - w_s} \\ &= \frac{\frac{25 - 15}{15} \times 100}{35 - w_s} \end{aligned}$$

$$w_s =$$

Ex:-)

$$\begin{aligned} S.R &= \frac{\frac{v_L - v_s}{v_d} \times 100}{w_L - w_s} = \frac{\frac{v_L - v_p}{v_d} \times 100}{w_L - w_p} \\ &= \frac{\frac{40 - 20}{20} \times 100}{0.6 - 0.2} = \frac{\frac{40 - v_p}{20} \times 100}{0.6 - 0.2} \end{aligned}$$

$$v_p =$$



Volumetric shrinkage :-

$$\alpha_s \neq S.R = \frac{\frac{\Delta V}{V_d} \times 100}{w_H - w_L}$$

$$S.R (w_H - w_L) = \frac{\Delta V}{V_d} \times 100$$

$$S.R (w_H - w_L) = \frac{\Delta V}{V_d} \text{ (volumetric shrinkage)}$$

$$S.R (w_H - w_L) = v_s \text{ (volumetric shrinkage)}$$

1.  $w_s$  upto  $w_L$ ,  $S = 100\%$ .

2.  $w=0$ ,  $S=0$

3.  $w=0$  and  $w_s$ ,  $0 < S_r < 100\%$ .

4. ① & ②

$$e = \text{constant}, r_{sd} = \frac{M_s}{V} = \frac{G_s \cdot r_w}{1+e}$$

5. ② & ④

$$e = \text{variable}, S_r = \frac{V_w}{V_v}$$

6. ② & ④

$$\Delta V = \text{variable}, G_s = \text{constant}$$

7. ① & ④

water content = variable

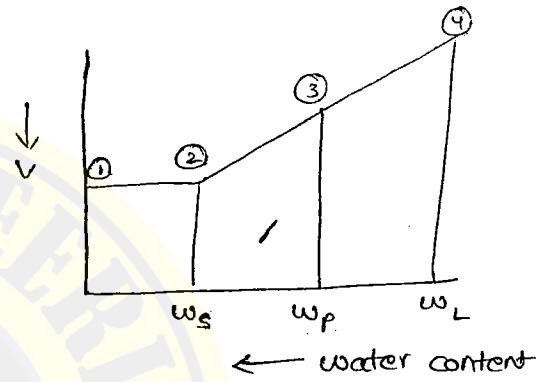
8. ① & ④

$S_r = \text{constant}$

8. Appsc:-

1. If  $w.c_{\text{natural}} = 27\%$ . Is  $w_s$  &  $w_p$

2. If  $w.c_{\text{natural}} = 45\%$ . Is  $w_p$

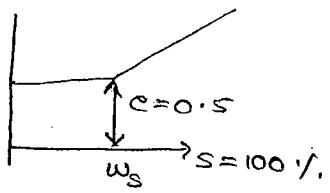


$$Ex:- \quad G_w_s = sc$$

$$G_w_s = 1 \cdot c$$

$$w_s = \frac{c}{G} = \frac{0.5}{2.72} \times 100$$

=



$$G_s = 2.72$$

Consistency Index ( $I_c$ ): -

$$I_c = \frac{w_L - w_{natural}}{w_L - w_p} = \frac{w_L - w}{I_p}$$

i)  $w_{nat} = 0$  (dry)

$$= \frac{w_L}{w_L - w_p} \quad (I_c > 1)$$

ii)  $w_{nat} \Rightarrow w_s$

$$I_c = \frac{w_L - w_s}{w_L - w_p} \quad \text{Greater} \quad (I_c > 1)$$

iii)  $w_{nat} = w_p$

$$I_c = \frac{w_L - w_p}{w_L - w_p} = 1 \quad (I_c = 1)$$

iv)  $w_{nat} = w_L$

$$I_c = \frac{w_L - w_L}{w_L - w_p} = 0 \quad (I_c = 0)$$

v)  $w_{nat} \Rightarrow w_L$

$$I_c' = \frac{w_L - (w_{sat})}{w_L - w_p} \quad (I_c = -ve)$$

$$(w_{sat} > w_L)$$

Liquidity Index :-

$$I_L = \frac{w_{nat} - w_p}{w_L - w_p}$$

i)  $w_{nat} = 0, \quad I_L = -ve$

iii)  $w_{nat} = w_p, \quad I_L = 0$

ii)  $w_{nat} = 0, \quad I_L = -ve$

iv)  $w_{nat} = w_L, \quad I_L = 1$

$w_{sat} > w_L$   
 $I_L > 1$

Toughness Index :- ( $I_T$ ) :-

$$I_T = \frac{I_p}{I_f} , I_f \propto \frac{1}{S.S}$$

(12)

Activity :-

$$\text{Activity (A)} = \frac{\% I_p}{\% \text{ clay fraction}}$$

If activity,  $A < 0.75$  (In active)

$A = 0.75 - 1.25$  (Normal)

$A > 1.25$  (Active)

Ex:- Soil Bentonite - High swelling and shrinkage

$A > 4$  for montmorillonite

C.G.S. (Index properties) :-

Density Index ( $I_D$ ) (or) Relative density :-

$$I_D = \frac{e_{max} - e}{e_{max} - e_{min}} \times 100$$

V. loose ( $R_D = 0\%$ )

Loose

Mud

Dense

V. Dense ( $R_D = 100\%$ )

Range:-  $0\% \leq R_D \leq 100\%$ .

Note :-

1. Relative density test is suitable for Friction soil.

2. Relative density      Description

0% - 15%      very loose material (this soil is used for ground improvement)

15 - 30%      loose material

30 - 65%      Medium material

65 - 85%      Dense material

> 85%      very dense material.

3. General shear failure occur when  $R_D > 30\%$ .

shape of particle:-

Engineering properties depends on shape of particle  
(coarse grained soil).



Angular

— Angle of friction ( $\phi$ ) is more



sub-angular



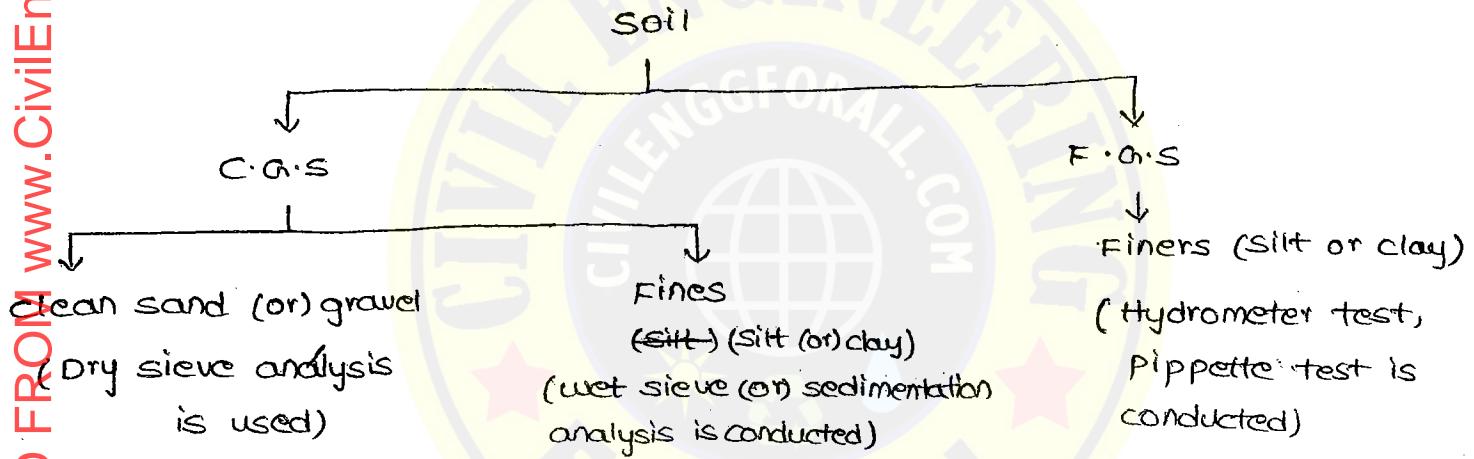
Rounded



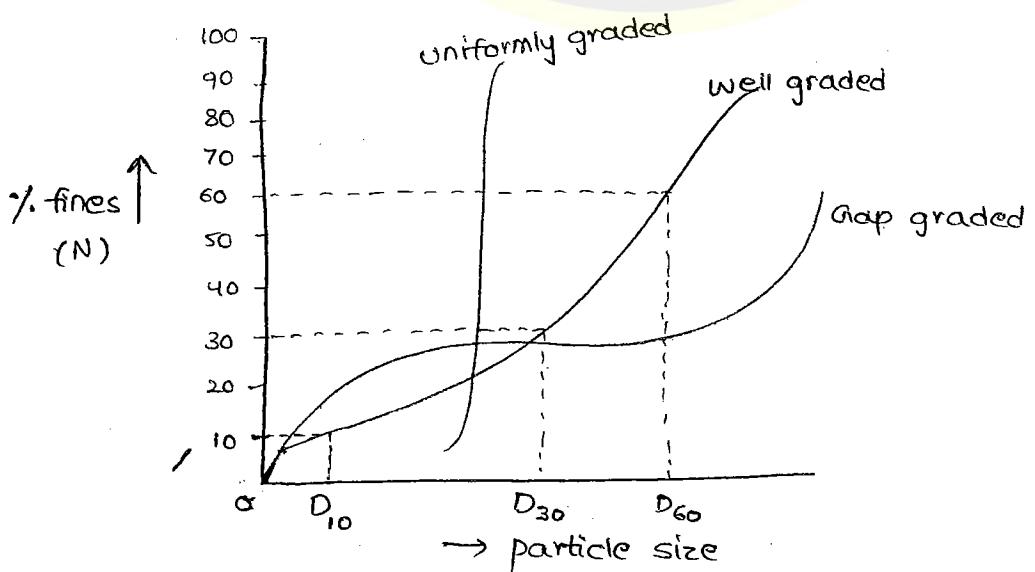
well rounded — Angle of friction ( $\phi$ ) is less

C.G.S material are generally called Bulky material (or)  
3D particle.

particle size distribution:-



\* In  $75\mu$  sieve there are 200 openings in one inch.



coefficient of uniformity ( $C_u$ ):-

$$C_u = \frac{D_{60}}{D_{10}}$$

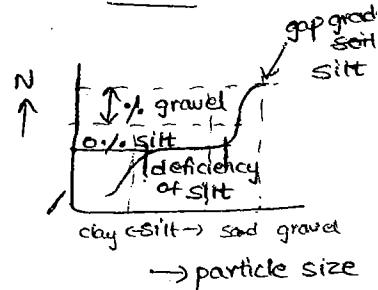
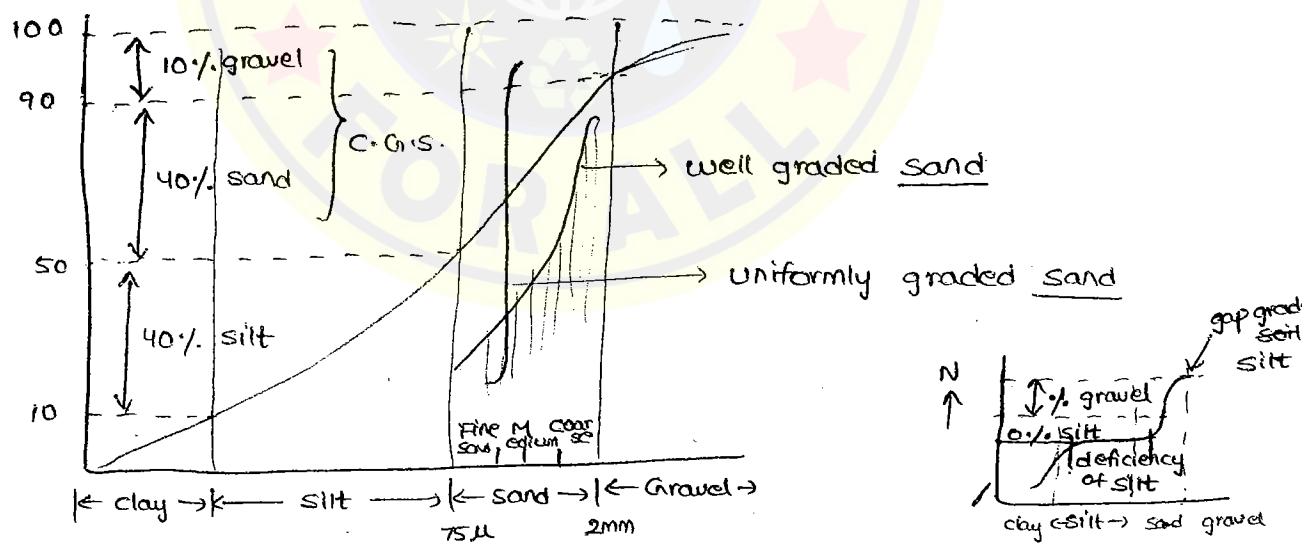
$D_{10}$  is also called effective size (mm)

1.  $C_u$  cannot be less than '1'.
2. A uniformly graded soil,  $C_u$  lies between 1 and 2.
3. A well graded <sup>gravel</sup> ~~silt~~,  $C_u$  must be greater than 4.
4. For well graded sand,  $C_u$  must be greater than 6.
5. Uniformly graded soil is also called poorly graded soil.

Coefficient of curvature (or) concavity (or) gradation ( $C_c$ ):-

$$C_c = \frac{D_{30}^2}{D_{60} \times D_{10}}$$

1. It represents particle size curve.
2. For well graded soil,  $C_c$  lies in between 1 and 3.
3. For uniformly graded soils,  $C_c \approx 1$ .



- If curve is present in gravel zone then the curve is called "Uniformly graded Gravel" (or) some other curve.
- Well graded are "Wide Range" ( $C_u > 6$ )
- poorly graded are "Narrow or steep Range". ( $C_u = 1$ )

1. Well graded soil - Aeolian soil, Talus, Glacier soils (Till)  
 (well sorted soil)
2. poorly graded soil (uniformly graded soil) - Marine deposit  
 EX:- Marine deposit, Beach sand

P-9 No:- 19

Given,  $C_u = 4$ ,  $C_c = 1$ ,  $D_{30}/D_{10} = ?$

$$C_u = \frac{D_{60}}{D_{10}} \Rightarrow 4 D_{10} = D_{60}$$

$$C_c = \frac{D_{30}^2}{D_{60} \times D_{10}}$$

$$1 = \frac{D_{30}^2}{D_{60} \times D_{10}}$$

$$D_{30}^2 = D_{60} \times D_{10}$$

$$D_{30}^2 = 4 D_{10} \times D_{10}$$

$$\left(\frac{D_{30}}{D_{10}}\right)^2 = 4$$

$$\frac{D_{30}}{D_{10}} = 2$$

Stoke's law:-

$$\text{Terminal velocity, } v_s = \frac{g}{18} (G-1) \frac{d^2}{2v}$$

$$\% \text{ of finer obtained by } N = \left[ \frac{R_h (\text{corrected})}{1000} \times \frac{\left(\frac{G}{G-1}\right)}{m/v} \right] \times 100$$

$v$  = volume of water (1 lit)

$m$  = mass of finer

$R_h$  = hydrometer reading corrected.

UNIT - 5SOIL CLASSIFICATION

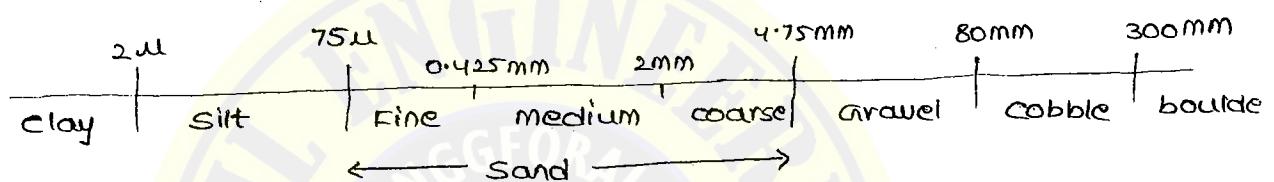
Labelling of soil is soil classification.

Criteria:-

1. Method used should be simple
2. It should give more information
3. Easy to understand.

I.S. particle size classification:-

Classification is done based on grain size only.



AASHTO (American Association of State Highways and Transportation Officials):-

1. It is also called Public Road Administration (PRA) or Highway Research Board (HRB).
2. AASHTO classification is used for Road purpose not general purpose.

Soil classification:-

1. Soil is classified into groups like A<sub>1</sub>, A<sub>2</sub>, ..., A<sub>7</sub>.
2. A<sub>1</sub> is good quality soil, A<sub>7</sub> is poor quality soil.
3. Black cotton soils (or) clay comes under A<sub>7</sub> group.
4. Stone fragments (or) Gravel (or) sand comes under A<sub>1</sub>, A<sub>2</sub>, A<sub>3</sub>.
5. Fine sand, silt, clay comes A<sub>4</sub>, A<sub>5</sub>, A<sub>6</sub>, A<sub>7</sub>.

Group Index:-

$$G.I = 0.2(a) + 0.005(a \cdot c) + 0.01(b \cdot d)$$

$a = \%$  of soil passing through 75μ sieve,  $> 35\%$  and  $\leq 10\%$  exceeding 75%. [The range is 0 to 40]

b = % of soil passing through 75  $\mu$  sieve, > 15% and not exceeding 55%. [Range is 0 to 40%]

c = a portion of L.L. > 40% and not exceeding 60%.  
[Range is 0 to 20%]

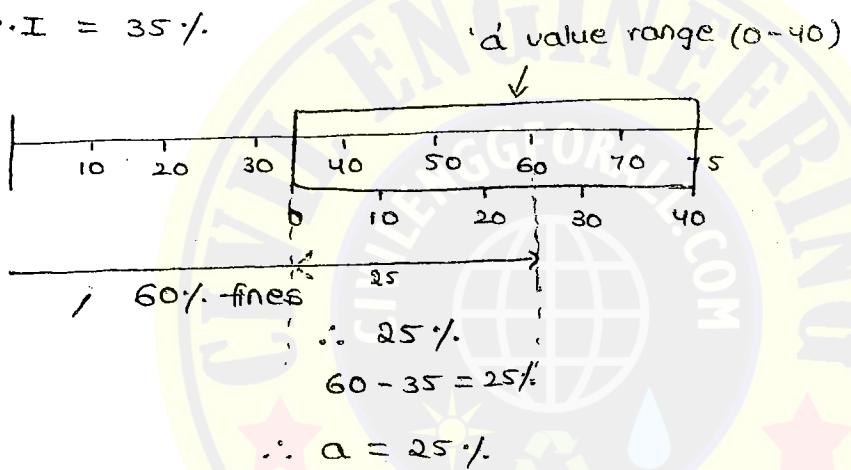
d = a portion of P.I. > 10% not exceeding 30%.  
[Range is 0 to 20%]

Group index is used to indicate quality of soil within its own group.

Ex:-

$$L.L = 60\%$$

$$P.I = 35\%$$



L.L. :- 75  $\mu$  sieve  
 $\downarrow$   
60% fines passed  
 $\uparrow$   
'a' value

Ex:- soil passing through a 75  $\mu$  is 78% and L.L = 55%,  
P.I = 24%. Find Group Index (GI).

A)  $G.I = 0.2(a) + 0.005(a \cdot c) + 0.01(bd)$

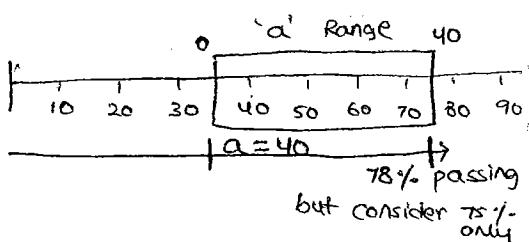
$$\therefore a = 40 \quad b = 40 \quad c = 15\% \quad d = 14\%$$

$$G.I = 0.2(40) + 0.005(40 \times 15) + 0.01(40 \times 14)$$

$$= 8 + 3 + 5.6$$

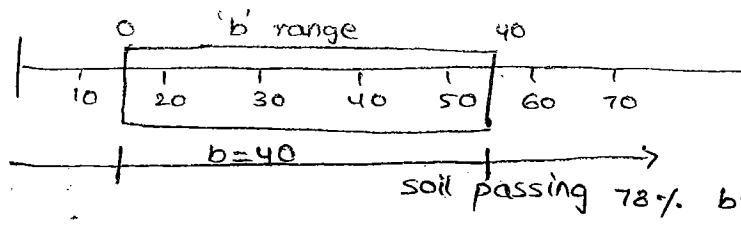
$$= 16.6$$

$$\approx 17$$

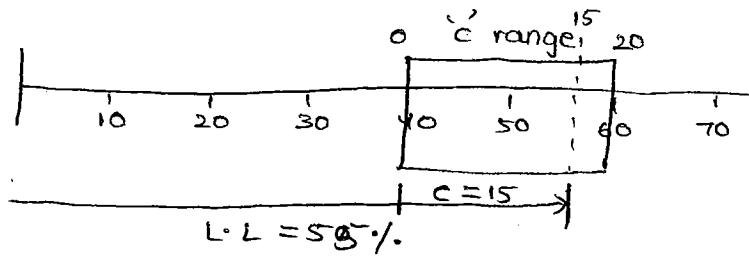


Note:- Actually 'a' value is 43 but in G.I 'a' Ranges 0 to 40, so take 40 (not exceed 40). Actually 'b' value is 63, but 'b' Ranges is 0 to 40. so consider 'b' is 40 (not 63).

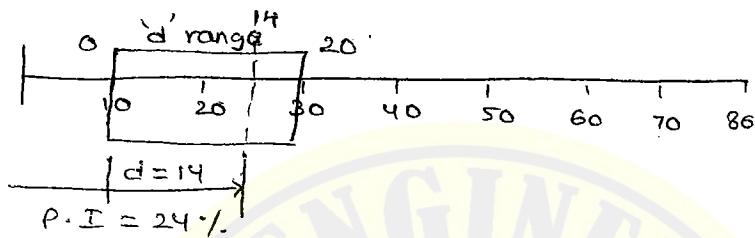
(15)



soil passing 78%. but consider 'b' max range is 55%.



$$L \cdot L = 55\%$$



$$P \cdot I = 24\%$$

Plasticity chart :-

C → clay

L → Low compressibility

M → silt

I → Intermediate compressibility

O → Organic silt

H → High compressibility.

Ex:-

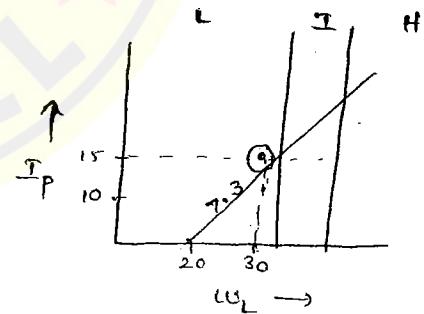
$$L \cdot L = 30\%$$

$$P \cdot L = 15\%$$

$$I_p = 30 - 15 = 15\%$$

$$\begin{aligned} A\text{-line} &= 0.73(\frac{I_p}{L \cdot L} - 20) \\ &= 0.73(30 - 20) \\ &= 7.3 \end{aligned}$$

⇒ CL



Note:- If  $I_p$  value is above the A-line (7.3) then soil comes under clay. Liquid limit is given 30%. it is in L-zone (Low zone). Then the soil classification is CL

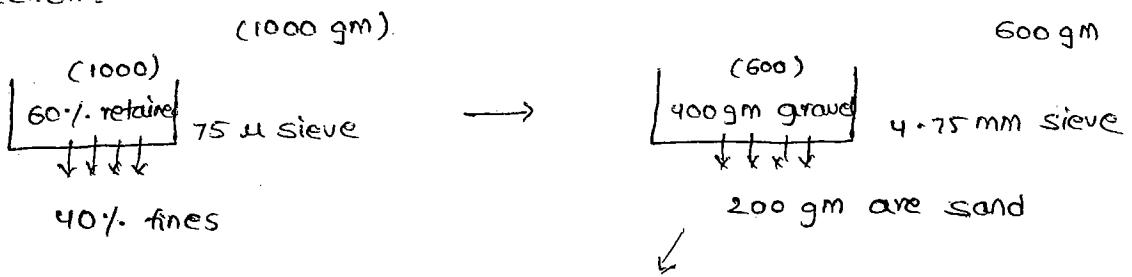
∴ plasticity chart is used only for fine grained soils.

50% of soil is retained on 75  $\mu$  sieve

↓  
C.G.S (50% retained)

↓  
F.G.S (50% retained)

## Coarse fraction :-



If 50% is retained on 4.75 mm sieve then the coarse fraction is gravel.

$\therefore$  Gravel > Sand.

Note:- SC - clayey sand (sand is major part, sand > clay)  
clayey, silty whichever is end with ey, ty (y) that is minor part.

Ex:- clayey silty gravel

clay < silt < Gravel.

## Gravel :-

GW F < 5%.  $C_u > 4%$ .  $C_c = 1 \text{ to } 3$

GP F < 5%.

GM F > 12%. Silt > clay

GC F > 12%. Clay > silt

## Sand :-

SW F < 5%.  $C_u > 6$ ,  $C_c = 1 \text{ to } 3$

SP F < 5%.

SM F > 12%. Silt > clay

SC F > 12%. Clay > silt

If  $F = 5\text{--}12\%$ . Dual symbol

## Gravel :-

GW - GC } clay > silt (Atterberg limits)  
GP - GC }  $C_u > 4$ ,  $C_c = 1 \text{ to } 3$

GW - GM } silt > clay  
GP - GM }  $C_u > 4$ ,  $C_c = 1 \text{ to } 3$

## Sand :-

Clay > silt

silt > clay

SW - SC }  $C_u > 6$ ,  $C_c = 1 \text{ to } 3$   
SP - SC }

SW - SM }  $C_u > 6$ ,  $C_c = 1 \text{ to } 3$   
SP - SM }

29-11-2017

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## UNIT - 6

### PERMEABILITY

Darcy's Law :-

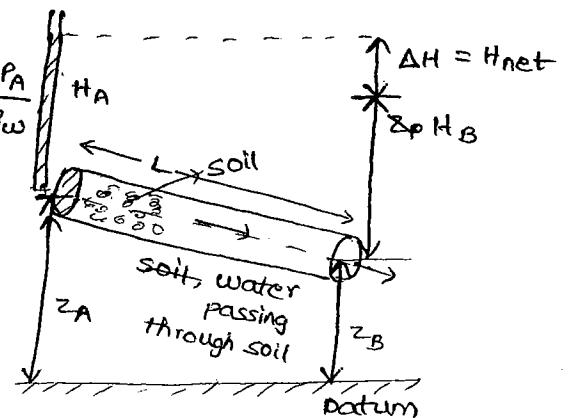
$$\frac{V_A^2}{2g} + \left( \frac{P_A}{\gamma_w} + z_A \right)$$

↓  
potential head

(or)

Total head

$$\frac{V_B^2}{2g} + \left( \frac{P_B}{\gamma_w} + z_B \right)$$



$$\Delta H = \left[ \frac{P_A}{\gamma_w} + z_A \right] - \left[ \frac{P_B}{\gamma_w} + z_B \right]$$

For flow through soils

$$v \propto i$$

$v$  = average velocity (or) Discharge velocity (or) superficial velocity

$$i = \text{hydraulic gradient} = \frac{\Delta H}{L} \quad (\text{no units})$$

$$v = k i$$

Multiply both sides by Area(A)

$$v \cdot A = k i A$$

$Q = k i A$

$$\frac{m^3}{sec} = \frac{m}{sec} \times m^2$$

when  $i = 1$ ,  $v = k$

$k$  = coefficient of permeability

$A$  = c/s of soil fabric =  $(A_v + A_s)$

$$A_v = \frac{A_{\text{seepage}}}{A_{\text{voids}}} v_{\text{seepage}}$$

$$v_{\text{seepage}} = v \cdot \frac{A}{A_{\text{voids}}}$$

$$= (v_{\text{discharge}}) \cdot \frac{1}{\left( \frac{A_v}{A} \cdot \frac{H}{H} \right)}$$

$v_{\text{seepage}} = \frac{v_{\text{discharge}}}{\frac{V_v}{V}} = \frac{v_{\text{discharge}}}{n}$

$$0.1 < n < 100.$$

Note! - seepage velocity always greater than discharge velocity

$$v_{\text{seepage}} > v_{\text{discharge}}$$

$$V_{\text{seepage}} \propto V_{\text{discharge}} \propto i$$

$$V_{\text{seepage}} \propto i$$

$$\frac{V_{\text{seepage}}}{V_{\text{discharge}}} = \frac{k_p i}{k i}$$

$$k_{\text{percolation}} = \frac{V_{\text{seepage}}}{V_{\text{discharge}}} \cdot k$$

$$k_p = \frac{k}{n}$$

$\therefore k_p$  is always greater than 'k'.

$$\rightarrow Q = k i A$$

$$Q = \left[ C \cdot D_{10}^2 \cdot \frac{\gamma_w}{\mu_w} \cdot \frac{e^3}{1+e} \right] \cdot i A$$

D = effective grain size

$\mu$  = viscosity of percolating fluid

e = void ratio

C = shape constant depends upon the type of soil.

property of percolating fluid:-

$$K \propto \gamma_w \propto \frac{i}{\mu_{\text{fluid}}}$$

$$K_1 \mu_1 = K_2 \mu_2$$

21°                    40°

$$K_{40^\circ} = K_{21^\circ} \cdot \frac{\mu_{21^\circ}}{\mu_{40^\circ}}$$

Void ratio:-

$$K \propto \frac{e^3}{1+e}$$

The above equation is not valid for clays, it is valid for sand and gravel (C.G.S material)

Before compaction

$$K = 10^6 \text{ cm/sec}$$

$$e = 0.9$$

After compaction

$$K = ?$$

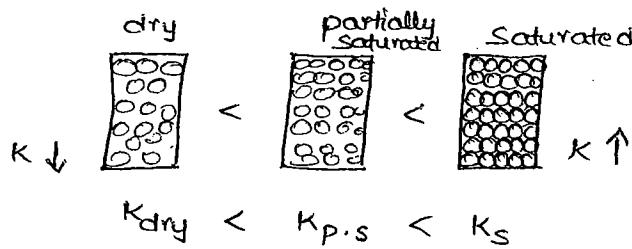
$$e = 0.35$$

$$10^6 = 1$$

$$\frac{K_{BC} \propto \frac{e_{BC}^3}{1+e_{BC}}}{K_{AC} \propto \frac{e_{AC}^3}{1+e_{AC}}} \Rightarrow K_{AC} = 0.08$$

## permeability of different types of soil :-

(17)

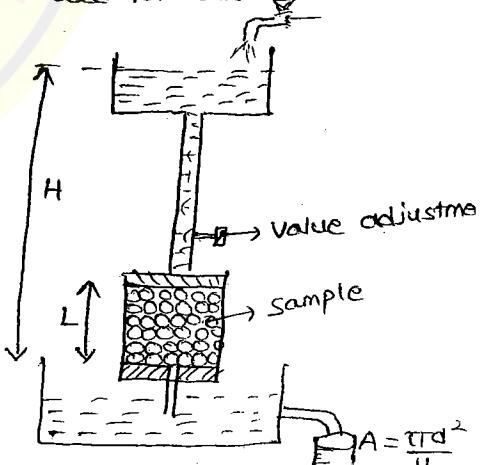
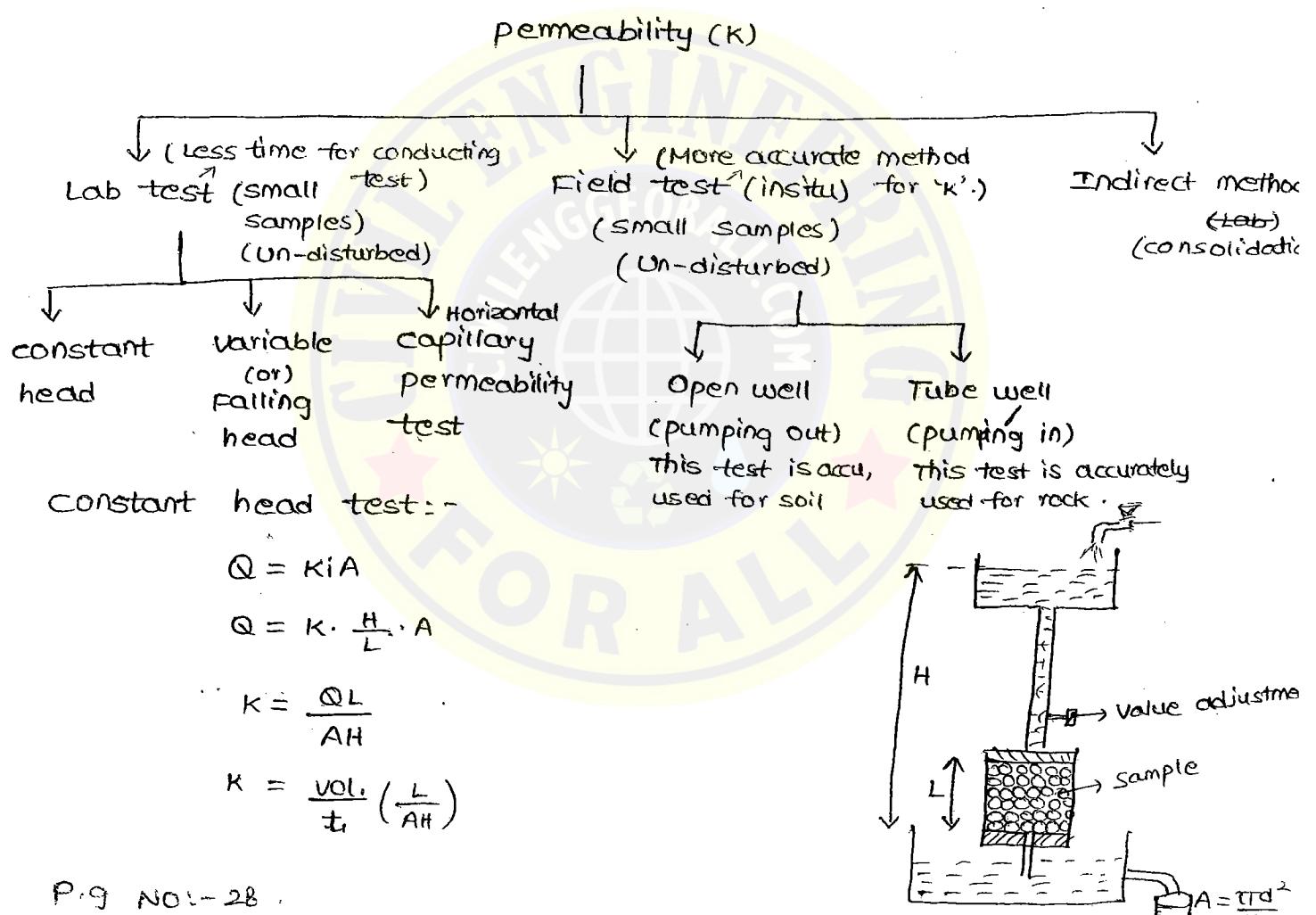


Complete Class Note Solution  
JAIN'S / MAXCOI  
SHRI SHANTI ENTERPRISES  
37-38, Suryalok Complex  
Abids, Hyd.  
Mobile. 9700291147

'K' is high in saturated soil.

In clay permeability is low because it having a adsorbs water.

## Testing (or) Determination of permeability (K) :-



4. Given  $A = 10 \text{ cm}^2$ ,  $i = 0.5$ ,  $t = 60 \text{ sec}$ ,  $V = 600 \text{ c.c.}$

$$Q = K i A$$

$$K = \frac{Q}{i A}$$

$$= \frac{(V)}{0.5 \times \pi (10)^2 / 4}$$

$$= \frac{600/60}{0.5 \times \pi (10)^2 / 4} = 2.0 \text{ cm/s}$$

1. Temperature  $\uparrow \mu \downarrow = 0.75$

Temperature  $\uparrow \gamma_w \downarrow = 0.9$

Condition - ①

Low temp.

$$\mu = \mu_1$$

$$\gamma_w = \gamma_{w_1}$$

$$K = K_1$$

Condition - ②

High temp

$$\mu_2 = 0.75(\mu_1)$$

$$\gamma_{w_2} = 0.90(\gamma_{w_1})$$

$$K = K_2$$

$$K_2 \propto \frac{\gamma_{w_2}}{\mu w_2}$$

$$K_1 \propto \frac{\gamma_{w_1}}{\mu w_1}$$

$$\frac{K_2}{K_1} = \frac{\gamma_{w_2}^{0.9 \times \mu_1}}{\gamma_{w_1}} \times \frac{\mu w_1}{\mu w_2} \downarrow 0.75 \mu_1$$

$$K_2 = K_1 (1.20)$$

Variable head test (or) Falling head test :-

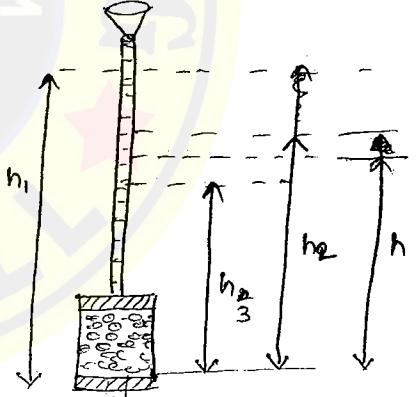
$$\Delta q = K \cdot i \cdot A$$

$$-(a \cdot \frac{dh}{dt}) = K \cdot \frac{h}{L} \cdot A$$

$$r \int \frac{dh}{h} = \frac{K}{L} \cdot \frac{A}{a} \int dt$$

$$[\log_e h]_{h_1}^{h_2} = -K \cdot \frac{A}{a \cdot L} (t_2 - t_1)$$

$$K = \frac{aL}{At} \log_e \left( \frac{h_1}{h_2} \right)$$



Highly percolous soil use larger diameter pipe. Low percolous soil small diameter pipe is used.

P. Q No:- 28

$$2. \frac{a}{At} \log_e \left( \frac{h_1}{h_2} \right) = \frac{a}{At} \log_e \left( \frac{h_2}{h_3} \right) \quad \therefore \text{time is same}$$

$$\frac{h_1}{h_2} = \frac{h_2}{h_3}$$

$$h_2^2 = h_1 \times h_3$$

$$h_2 = \sqrt{h_1 \times h_3}$$

Note:-

Fine Sand is suitable for both constant head, and variable (or) falling head test.

Ex:-)

constant head

$$V = 600 \text{ c.c}$$

$$t = 60 \text{ sec}$$

$$A = 100 \text{ cm}^2$$

$$H = 100 \text{ cm}$$

$$L = 10 \text{ cm}$$

Same sample is tested on variable head test

$$h_1 = 100 \text{ cm}$$

$$h_2 = 75 \text{ cm}$$

$$a = 10 \text{ cm}^2$$

$$t = ?$$

$$K = \frac{a \cdot L}{A \cdot t} \log_e \left( \frac{h_1}{h_2} \right)$$

$$\frac{Q}{iA} = 10 \left( \frac{aL}{At} \log_e \left( \frac{h_1}{h_2} \right) \right)$$

$$\frac{QK}{hA} = \frac{aK}{At} \log_e \left( \frac{h_1}{h_2} \right)$$

$$\frac{\left( \frac{V}{t} \right)}{H} = \frac{a}{t} \log_e \left( \frac{h_1}{h_2} \right)$$

$$\frac{\frac{600}{60}}{\frac{100}{100}} = \frac{10}{t} \log_e \left( \frac{100}{75} \right)$$

$$t = 12.49 \text{ sec} \quad 28.76 \text{ sec}$$

Capillary permeability test:-

$$\frac{x_2^2 - x_1^2}{t_2 - t_1} = \frac{2 \cdot K_{0.5}}{s \times n} \cdot h_1 + h_c$$

$$\frac{x_2^2 - x_1^2}{t_2 - t_1} = C \times K_{0.5} \times (h_2 + h_c)$$

Note:-

Acquifer is used for constructing of wells.

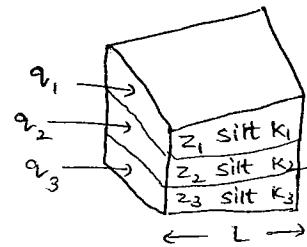
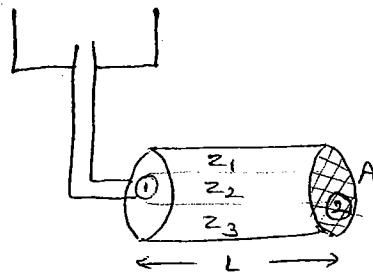
Acquifer - Gravel, sand

Aquiclude - clay

$$K_{\text{aquifer}} = \frac{Q \ln \left( \frac{r_2}{r_1} \right)}{\pi (h_2^2 - h_1^2)} = \frac{Q \ln \frac{R}{r_w}}{\pi (H^2 - h_w^2)} \rightarrow \text{pumping out test}$$

## permeability of stratified soil deposits:-

- a. Flow is parallel to planes of stratification.



Loss of head or hydraulic gradient is same for all layers

$$i = \frac{H_{\text{net}}}{L}$$

$$i = i_1 + i_2 + i_3 + \dots$$

$$q = q_1 + q_2 + q_3 + \dots$$

$$q_T = \sum q$$

$$q_T (\text{through entire soil}) = q_1 + q_2 + q_3 + \dots$$

$$K_i A = K_1 i_1 A_1 + K_2 i_2 A_2 + K_3 i_3 A_3 + \dots$$

'i' is same

$$K_{\text{entire soil}} = K_1 (A_1) + K_2 (A_2) + K_3 (A_3) + \dots$$

$$K_{\text{horizontal}} = K_1 (z_1 x_1) + K_2 (z_2 x_1) + K_3 (z_3 x_1) + \dots$$

$$K_h (A_T x_1) = K_1 z_1 + K_2 z_2 + K_3 z_3 + \dots$$

$$K_{\text{avg}} (1 \times z_1) = K_1 z_1 + K_2 z_2 + K_3 z_3 + \dots$$

$$K_{\text{avg}} = \frac{\sum K_i z_i}{\sum z_i}$$

$$K_h = \frac{\sum (K_i z_i)}{\sum z_i}$$

$$K_h = \frac{K_1 z_1 + K_2 z_2 + K_3 z_3 + \dots}{z_1 + z_2 + z_3 + \dots}$$

- b. Flow through perpendicular to stratification:

$$K_v = \frac{z_1 + z_2 + z_3 + \dots}{\frac{z_1}{K_1} + \frac{z_2}{K_2} + \frac{z_3}{K_3} + \dots}$$

$\therefore K_h$  is always greater than  $K_v$ .

P.g NO:- 27

(19)

Ex:- 3)  $K_H = \frac{k_1 z_1 + k_2 z_2 + k_3 z_3}{z_1 + z_2 + z_3}$

$$= \frac{10^{-4}(1) + 10^{-3}(1) + 10^{-4}(1)}{1+1+1}$$
$$= \frac{10^{-4}[1+10+1]}{3}$$
$$K_H = 4 \times 10^{-4} \text{ cm/s}$$

$$\begin{array}{c|c} z=1 & 10^{-4} \text{ cm/sec} \\ \hline z=1 & 10^{-3} \\ \hline z=1 & 10^{-4} \end{array}$$

$$\therefore 10^{-3} \Rightarrow 10^1 \times 10^{-4}$$

P.g NO:- 26

3. Given  $k_1 = 4 \times 10^{-5} \text{ cm/sec}$

$$u = u_1, \quad u_2 = 0.5u_1 \text{ (half reduced)}$$

$$K \propto \frac{1}{u}$$

$$\frac{k_1}{k_2} = \frac{u_2}{u_1}$$

$$k_2 = \frac{k_1}{u_2} \times u_1$$

$$= k_1 \left( \frac{u_1}{0.5u_1} \right)$$

$$= \frac{4 \times 10^{-5}}{0.5}$$

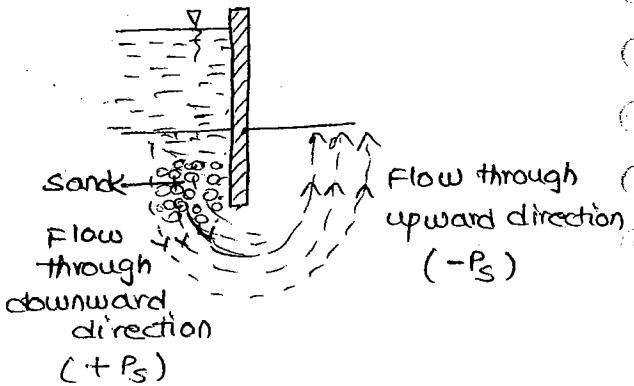
$$k_2 = 8 \times 10^{-5}$$

30-11-2014

UNIT - 8SEEPAGE PRESSURE AND CRITICAL HYDRAULIC GRADIENTSeepage pressure ( $P_s$ ):-

$$P_s = \pm \gamma_w h$$

$$P_s = i z \cdot \gamma_w = \gamma_w i L$$

 $i'$  is for upward flow is decreases $i'$  for downward flow is increases

Critical hydraulic gradient and quick sand condition:-

$$i' = 0 = \gamma' L - P_s$$

$$0 = \gamma' L - P_s$$

$$\gamma' L = P_s$$

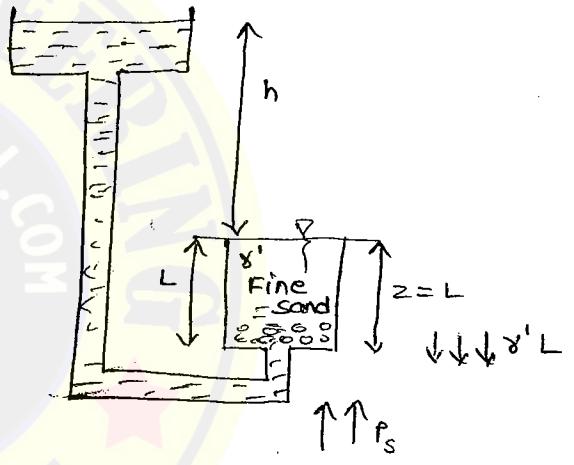
$$\gamma' L = \gamma_w i_c L$$

$$\gamma' = \gamma_w i_c$$

$$i_c = \frac{\gamma'}{\gamma_w}$$

$$= \left( \frac{G-1}{1+e} \right) \gamma_w$$

$$i_c = \frac{G-1}{1+e} \Rightarrow (G-1)(1-n)$$



void ratio in dense state = 0.35

Medium state =

Loose state = 0.91

Quick sand condition occurs when the soil having a low permeability (fine sands). Quick sand condition not occur for coarse sand or gravel.

seepage pressure increases quick sand condition will be reduced.

## Effect of surcharge on quick condition :-

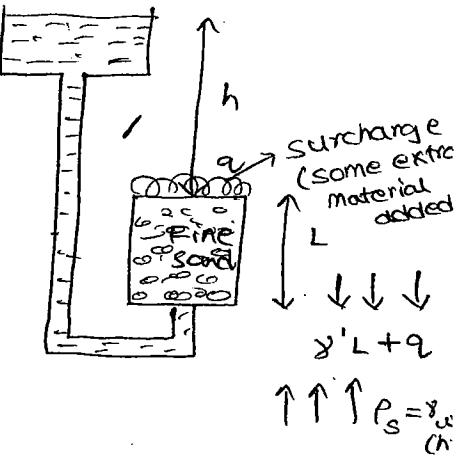
(20)

$$\epsilon' = 0$$

$$q + \gamma' L = (h + L) \gamma_w$$

$$q + \gamma' L = \gamma_w h + \gamma_w L$$

$$\frac{q + \gamma' L - \gamma_w h}{\gamma_w} = h$$



Piping:-

$$1. \frac{i_c}{i_{exit} (\text{smaller})} = F.S \quad (\text{Factor of safety})$$

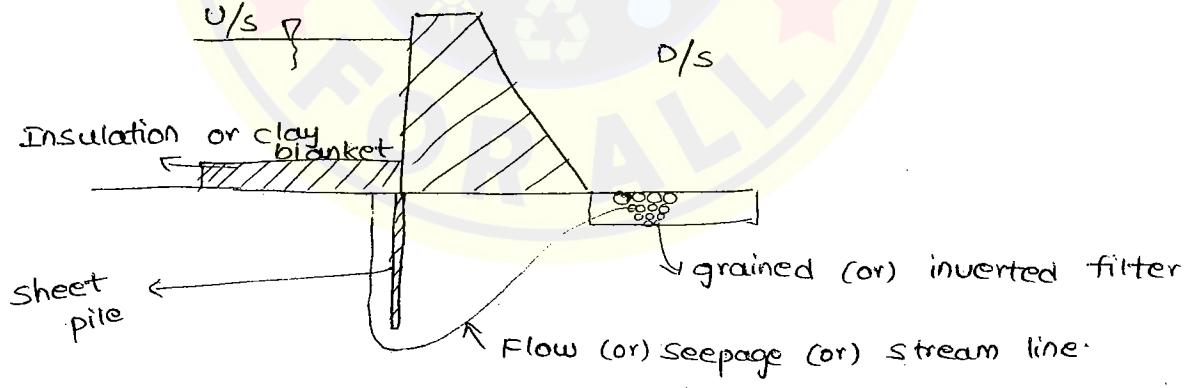
$\therefore F.S > 1$  (NO piping) (or) safe criteria

$$2. \frac{i_c}{i_{exit} (\text{greater})} = F.S$$

$\therefore F.S < 1$  (piping occur) (or) unsafe criteria

$$3. \frac{i_c}{i_{exit}} = F.S$$

$\therefore F.S = 1$  (critical)



P.g NO:- 35

$$1. \text{ Given } e = 0.62 \quad G = 2.62 \quad F.S = 5$$

$$F.S = \frac{i_c}{i_{exit}}$$

$$F.S = \frac{\frac{G-1}{1+e}}{i_{exit}}$$

$$i_{exit} = \frac{2.62 - 1}{1 + 0.62} = \frac{1}{5} = 0.2$$

Q. Given  $\gamma/G = 2.7$ ,  $c = 0.7$ ,  $L = 2m$

Quick sand condition is occur then  $F.S = 1$

$$F.S = \frac{i_c}{i_{exit}}$$

$$1 = \frac{i_c}{i_{exit}}$$

$$i_c = i_{exit}$$

$$\frac{\gamma - 1}{1 + c} = i_{exit}$$

$$\frac{2.7 - 1}{1 + 0.7} = i_{exit}$$

$$1 = i_{exit} = \frac{h}{L}$$

$$h = L = 2m$$

## UNIT - 12

### COMPACTION

#### Compaction:-

Compaction is artificial process in which partially saturated soils will be compacted by mechanical means to expell most of the air voids instantly. This is one of the economical ground improvement technique.

#### Benefits of compaction:-

1. Void ratio decreases
2. Permeability decreases
3. Future compressibility will be lesser
4. Erodability will reduce
5. Durability of structure increases
6. Stability increases

#### Objective of compaction:-

Compaction test are done to determine

- a. amount of compaction
- b. the optimum moisture content (OMC)

P.G No:- 55

$$8. \frac{\text{Energy}}{\text{cm}^3} = \frac{\text{wt. of hammer} \times \text{ht. of fall} \times \text{No. of layers} \times \text{blows per each layer}}{\text{volume of soil compaction}}$$

$$\frac{\text{Energy}}{\text{cm}^3} = \frac{2.6 \times 30.48 \times 3 \times 25}{1}$$

$$= 5,952 \text{ kg-cm.}$$

$$= 59.52 \text{ kg-m}$$

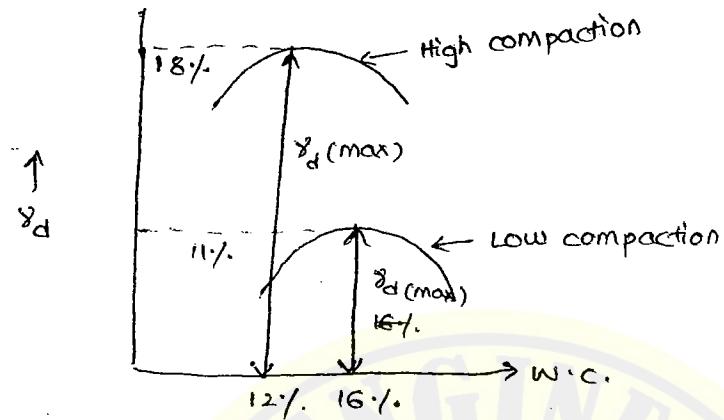
Note:-

$$\frac{\text{Energy}_M}{\text{Energy}_S} = \frac{\frac{49 \times 45 \times 5 \times 25}{1000}}{\frac{2.6 \times 30.48 \times 3 \times 25}{1000}} = \frac{1102.5}{237.74} = 4.637$$

## Compaction Test (Lab):-

1. To judge the suitability of soil for specific use.

Comparison between Low compaction and High compaction (or) Standard proctor test and Modified proctor test.



Dry density increases  
OMC decreases

→ 0% air voids line and 100% saturated line are same.

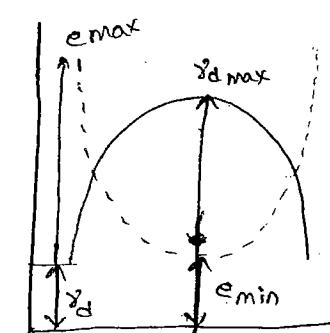
$$\gamma_{d, \text{theoretical}} = \frac{G \gamma_w}{1 + G w} = \gamma_{d, \text{(saturated line)}}$$

(0% line)

$$\gamma_{d, \text{(sat)}} = \frac{G \gamma_w}{1 + \frac{G w}{s}} \quad \therefore s = 1 \text{ (saturated)}$$

→ 95% of saturation line and 5% of Air content are same

→ 95% of saturation line and 5% of air voids are different



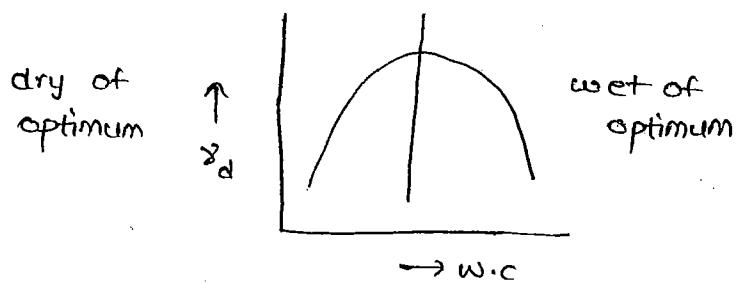
$$e = \frac{G \gamma_w}{\gamma_d} - 1$$

Relative Compaction:-

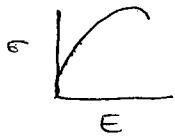
$$= \frac{\text{dry density in the field}}{\text{Max. dry density obtained in the lab}} \times 100$$

$$= \frac{\gamma_d \text{ (field)}}{\gamma_d \text{ (Max)}} \times 100$$

Dry of optimum:-



- |  |   |
|--|---|
| 1. Flocculated<br>2. water is deficient<br>3. permeability is more<br>4. swelling is more. | 1. Dispersion<br>2. water is excess<br>3. permeability is less<br>4. swelling is less |
|--|---|



- |                                 |                                 |
|---------------------------------|---------------------------------|
| 5. pore water pressure ↑<br>(u) | 5. pore water pressure ↓<br>(u) |
|---------------------------------|---------------------------------|

23-11-20

UNIT - 7EFFECTIVE STRESS

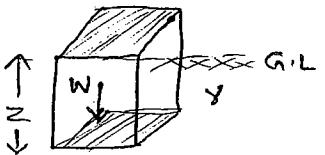
Stress:-

$$W = \gamma V$$

$$= \gamma (A \cdot Z)$$

$$\sigma = \frac{F}{A} = \frac{W}{A} = \frac{\gamma A Z}{A}$$

$$\therefore \sigma = \frac{F}{A} = \gamma Z$$



$$\gamma = \frac{W}{V}$$

$$\gamma V = W$$

## Stresses

Geo stress

stress due to applied load

Saturated soil:-

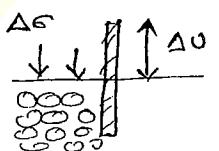
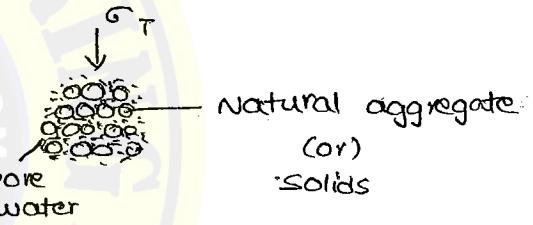
$$\sigma_T = \sigma' + u$$

$\sigma'$ ,  $u$  are measurable

$\sigma'$  = non measurable

$u$  = pore water pressure (or) Neutral pressure (or) hydrostatic pressure.

$$\sigma' = \sigma_T - u$$



$\Delta u$  = Hydro dynamic pressure (or) excess of pore water pressure occur when applied the load.

$\Delta \sigma$  = Applied stress

$\sigma'$  = effective stress.

Note:-

- When there is no water table (or) soil is completely dry

$$\sigma' = \sigma_T \quad \therefore (u=0)$$

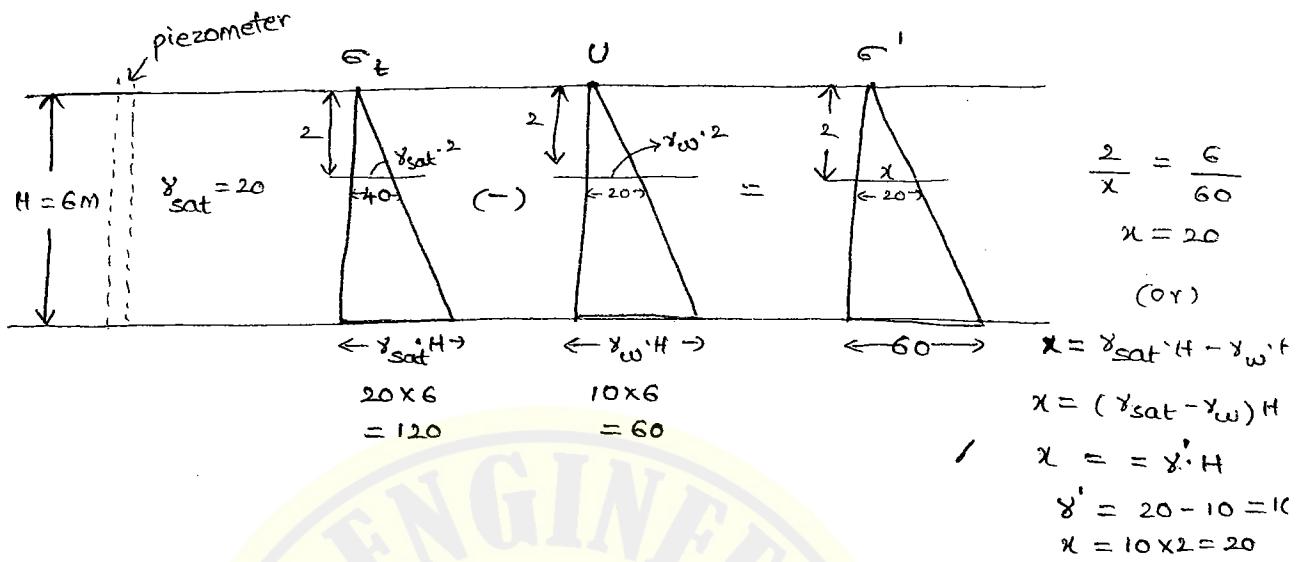
$$\sigma' (\gamma_{dry} \cdot H)$$

2. When soil is wet,  $\sigma_T = \sigma'$   $\rightarrow \gamma_{wet} \times H$

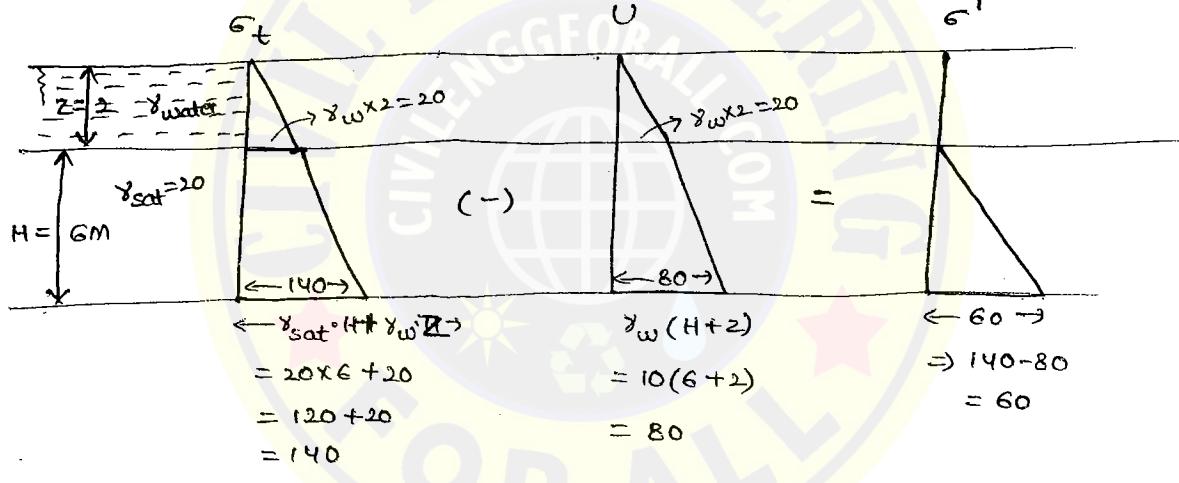
(23)

3. When soil is saturated (Non capillary),  $\sigma' = \sigma_T$   $\rightarrow \gamma_{sat} \times H$

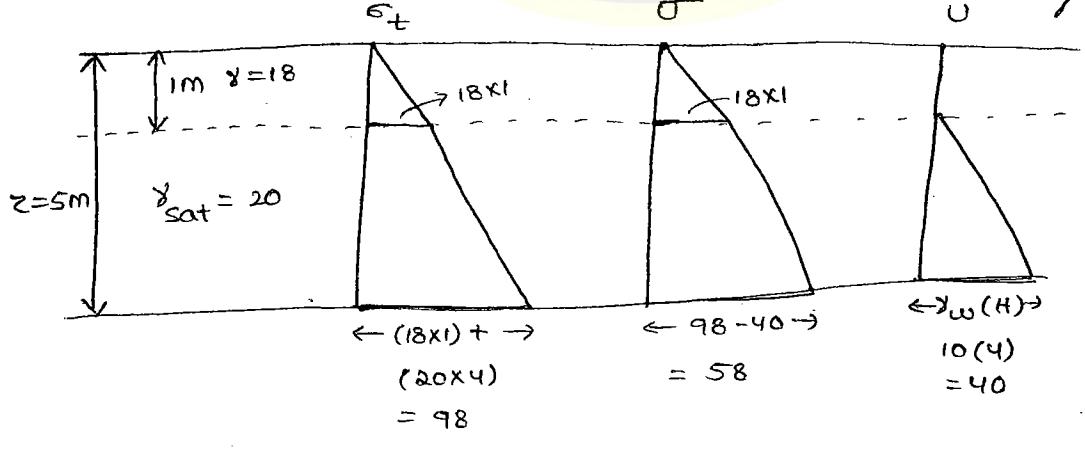
Ex:-



Ex:-



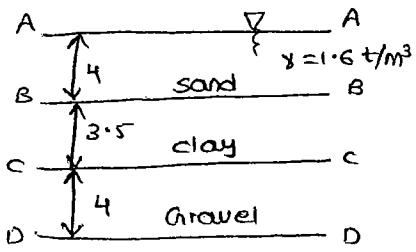
Ex:-



P.9 NO:- 30

$$\begin{aligned} \text{Ex:- 1)} \quad \sigma_{cc} &= (\gamma') (4) + (\gamma') (3.5) \\ &= (0.6)(4) + (0.9)(3.5) \\ &\leq 5.5 \text{ t/m}^2 \end{aligned}$$

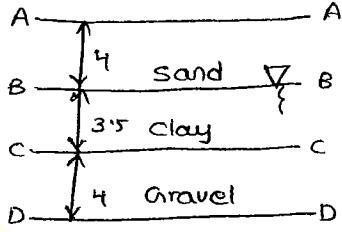
$$\begin{aligned} \sigma_{dd} &= (5.5) + (0.925)(4) \\ &= 9.25 \text{ t/m}^2 \end{aligned}$$



$$\therefore \gamma_{sub} = \gamma_{sat} - \gamma_{water}$$

$$\begin{aligned} \sigma_{cc} &= (1.6)(4) + (0.9 \times 3.5) \\ &= 9.55 \text{ t/m}^2 \end{aligned}$$

$$\begin{aligned} \sigma_{dd} &= 9.55 + 0.925(4) \\ &= 13.25 \text{ t/m}^2 \end{aligned}$$



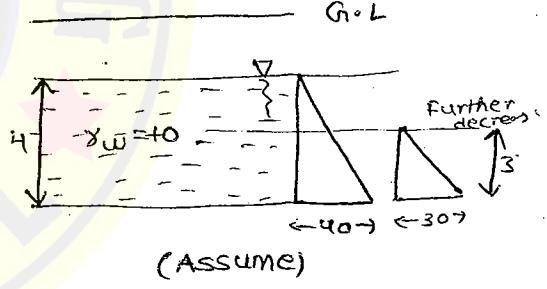
Note:-

$$\gamma_y = 1 \text{ t/m}^3 \quad (\text{or}) \quad 10 \text{ kN/m}^3 \quad (\text{or}) \quad 62.5 \text{ lb/m}^3$$

P.9 NO:- 32

$$\therefore \uparrow \epsilon' = \epsilon_t + U \downarrow$$

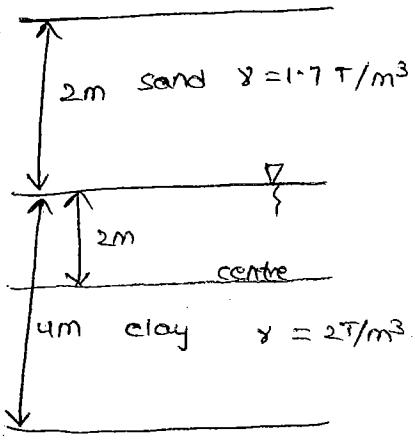
If water table decreases below the ground level "pore water decreases" and effective stress increases.



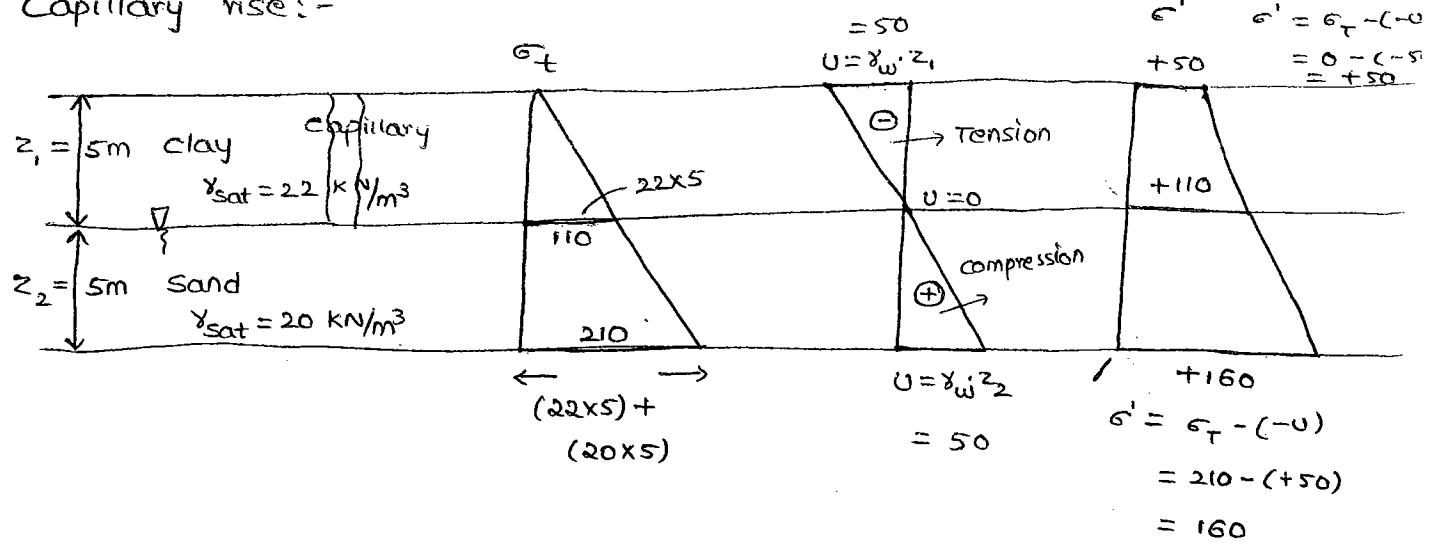
$$\therefore \downarrow \epsilon' = \epsilon_t + U \uparrow$$

If water table is rise gradually above the ground then pore water increases and effective stress decreases.

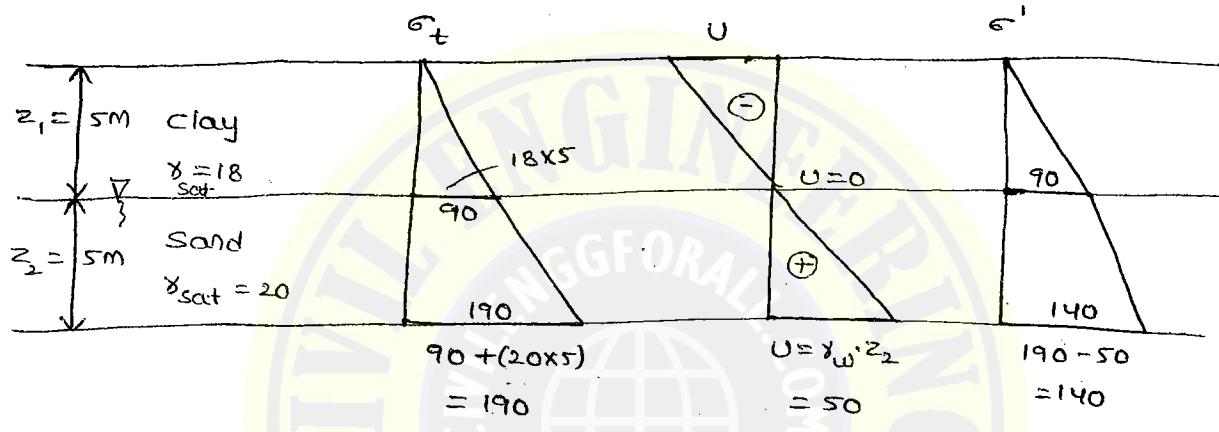
$$\begin{aligned} \text{19. } \epsilon' &= (1.7)(2) + (2-1)(2) \\ &\downarrow \text{submerged} \\ &= 3.4 + 2 \\ &= 5.4 \text{ t/m}^2 \end{aligned}$$



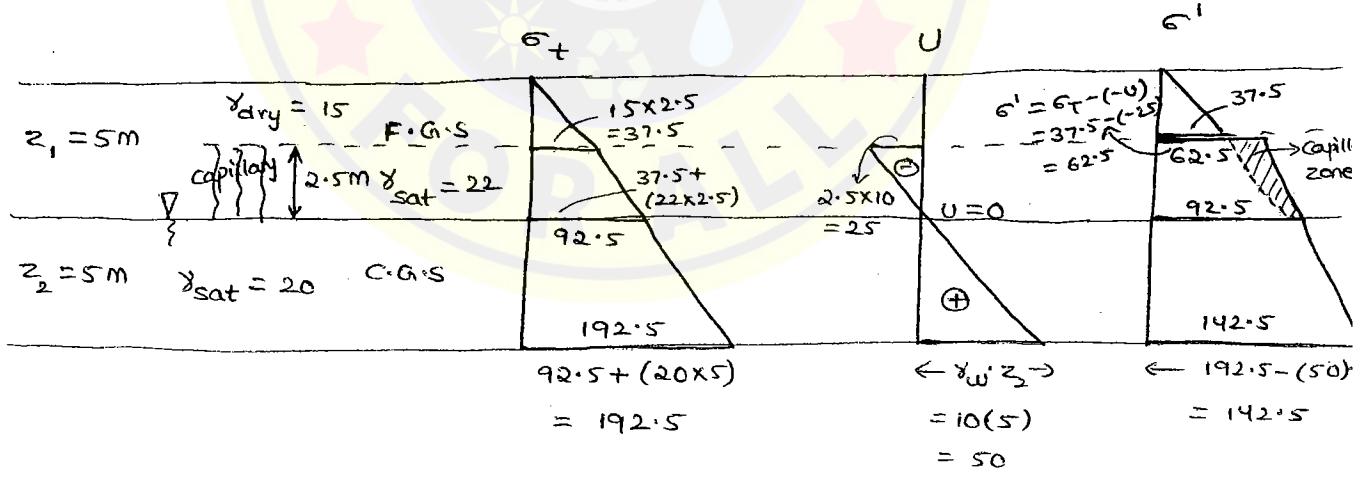
## Capillary rise :-



Without capillary



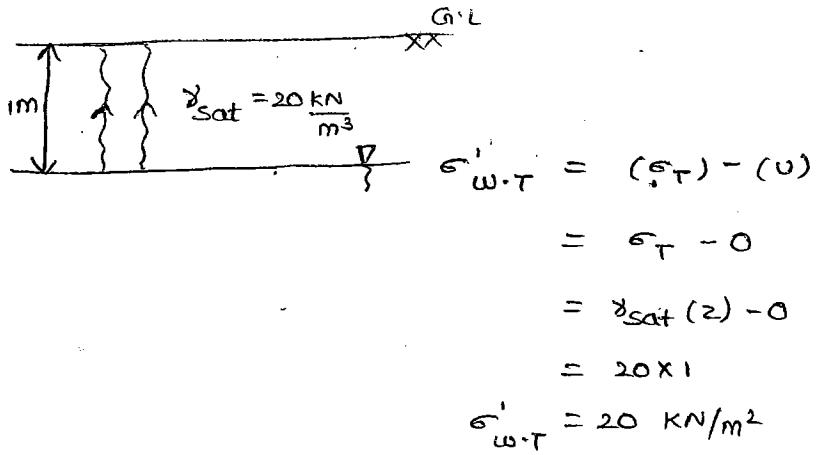
Ex:-



Note:-

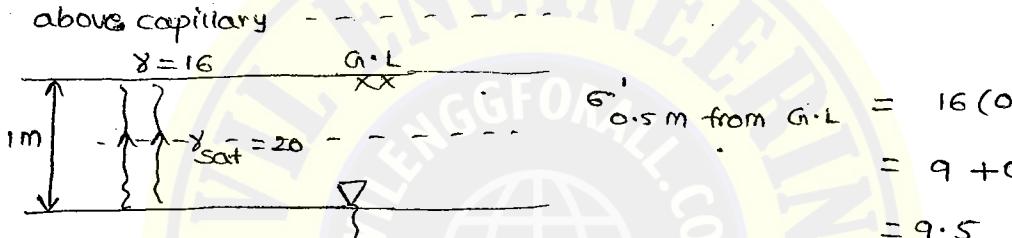
When Capillary is increasing up then effective stress is increasing. If capillary is decreasing downwards then effective stress decreasing.

Q2.



$$\begin{aligned}\sigma'_{G.L.} &= \sigma_T - u \\ &= 0 - (-10) \\ &= 10 \text{ kN/m}^2\end{aligned}$$

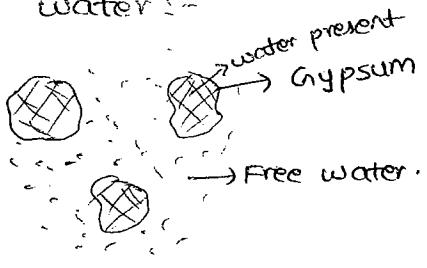
Ex:-



Water in soil :-

- Held water (against gravity) :-
- 2. structural water (any soil)
- 3. Adsorbed water (clay)
- 4. capillary water (fine, medium, coarse sand, silt and clay)

Structural water :-



In gypsum (water present + free water) can be removed in oven dry at  $105^\circ\text{C}$ . But other minerals water is not present in structure cannot be removed in oven dry at  $105^\circ\text{C}$ . If want to remove uses higher temperature ( $>105^\circ\text{C}$ )

Capillary water :-

surface tension force

$$\gamma_w \cdot v_w = (\gamma \cos\alpha) (\pi d)$$

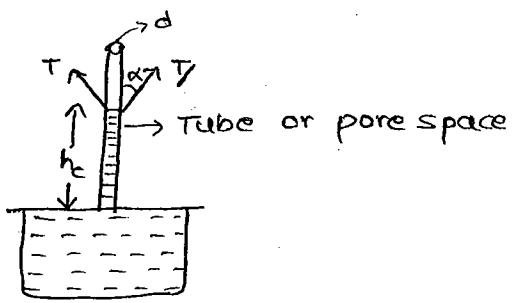
$$\gamma_w \cdot \left(\frac{\pi}{4}d^2 \times h_c\right) = (\gamma \cos\alpha) (\pi d)$$

$$h_c = \frac{4 \gamma \cos\alpha}{\gamma_w d}$$

$$h_c \propto \frac{1}{d_{\text{porespace}}}$$

$$\text{Clays } h_c \uparrow \propto \frac{1}{d_{\text{porespace}} \downarrow}$$

For clays,  $h_c \approx 25 - 30 \text{ m}$



27-11-2014

UNIT - 10STRESS DISTRIBUTION

Boussinesq's Equation:-

$$\sigma = \sqrt{x^2 + y^2}$$

$$\Delta \sigma_v(p) = \frac{Q}{z^2} (I_B)$$

$I_B$  = Boussinesq's influence factor

$$I_B = \frac{3}{2\pi} \left[ \frac{1}{1 + (\frac{r}{z})^2} \right]^{5/2}$$

$$I_B = \frac{3}{2\pi} \text{ (or) } 0.4775 \text{ (Under point load)}$$

This is applicable for weightless soil.

Westergaard's theory:-

$$\Delta \sigma_v(p) = \frac{Q}{z^2} (I_w)$$

$$I_w = \frac{1}{\pi} \left( \frac{1}{1 + 2(\frac{r}{z})^2} \right)^{3/2}$$

Ex:- Calculate the vertical stress at a point by using Boussinesq's equation.

A. Given  $Q = 100 \text{ KN}$ ,  $z = 2$

$$I_B = \frac{3}{2\pi} \left( \frac{1}{1 + (\frac{r}{z})^2} \right)^{5/2}$$

$\sigma = 0$  at point A.

$$I_B = \frac{3}{2\pi}$$

$$\Delta \sigma_{v(A)} = \frac{Q}{z^2} (I_B)$$

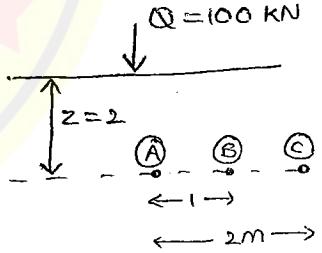
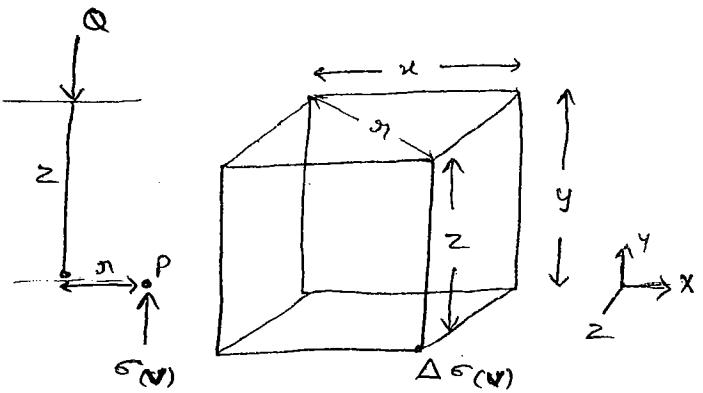
$$= \frac{100}{2^2} (0.4775)$$

$$\Delta \sigma_{v(A)} = 11.93 \text{ KN/m}^2$$

At point B:-

$$r = 1, z = 2$$

$$I_B =$$



$$\begin{aligned}\Delta \epsilon_{v(B)} &= \frac{Q}{z^2} (I_B) \\ &= \frac{100}{4} ( \\ &= 6.825 \text{ KN/m}^2\end{aligned}$$

At point C:-

$$r = 2, z = 2$$

$$I_B = \frac{3}{2\pi} \left( \frac{1}{1 + \left(\frac{2}{2}\right)^2} \right)^{5/2}$$

$$= I_B =$$

$$\begin{aligned}\Delta \epsilon_{v(C)} &= \frac{Q}{z^2} (I_B) \\ &= \frac{100}{4} ( \\ &= 2.11 \text{ KN/m}^2\end{aligned}$$

Note:-

1. If  $\frac{r}{z} = 0$ ,  $I_B = \frac{3}{2\pi}$  (or)  $0.4775$
2. If  $\frac{r}{z} = 10$ ,  $I_B = 0$

Ex:- Calculate the stresses by using Boussinesq's equation.

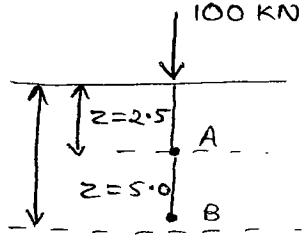
$$A. \quad \frac{\Delta \epsilon_A}{\Delta \epsilon_B} = \frac{\frac{Q}{z^2} (I_B)}{\frac{Q}{z^2} (I_B)}$$

$$r = 0, \text{ then } I_B = \frac{3}{2\pi}, Q = 100$$

$$\begin{aligned}&= \frac{\frac{100}{2.5^2} \cdot \left( \frac{3}{2\pi} \right)}{\frac{100}{5^2} \left( \frac{3}{2\pi} \right)}\end{aligned}$$

$$= \left( \frac{5}{2.5} \right)^2$$

$$\frac{\Delta \epsilon_A}{\Delta \epsilon_B} = 4$$



10. Given  $Q = 700 \text{ kN}$ ,  $z = 2\text{m}$ ,  $r = 1.0\text{m}$ ,  $\sigma_v = ?$

$$I_B = \frac{3}{2\pi} \left( \frac{1}{1 + \left(\frac{r}{z}\right)^2} \right)^{5/2}$$

$$= \frac{3}{2\pi} \left( \frac{1}{1 + \left(\frac{1}{2}\right)^2} \right)^{5/2}$$

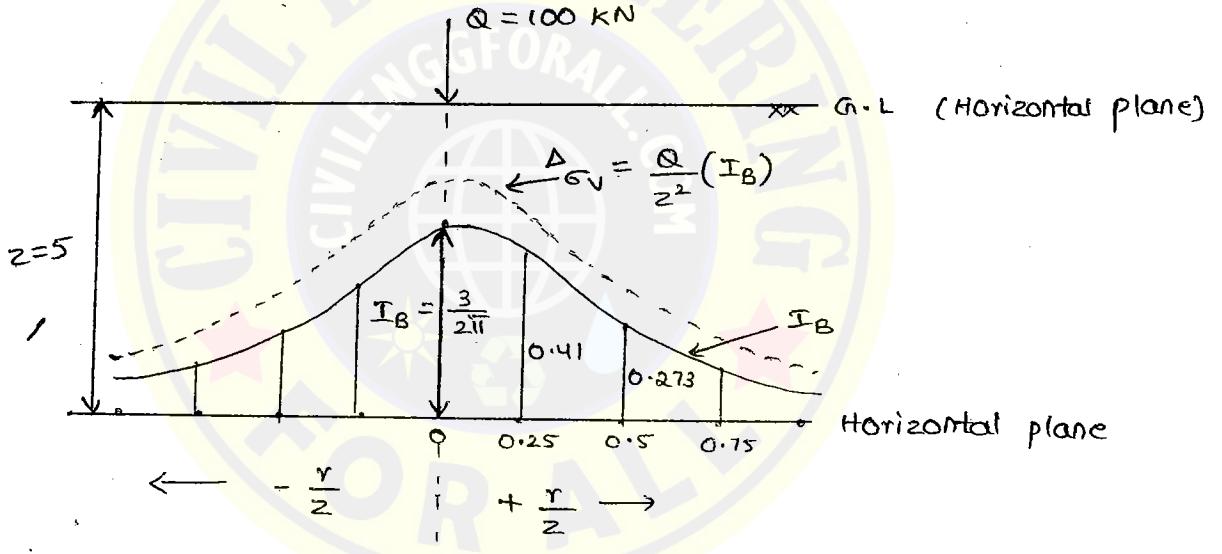
$$I_B = 0.275$$

$$\sigma_v = \frac{Q}{z^2} (I_B)$$

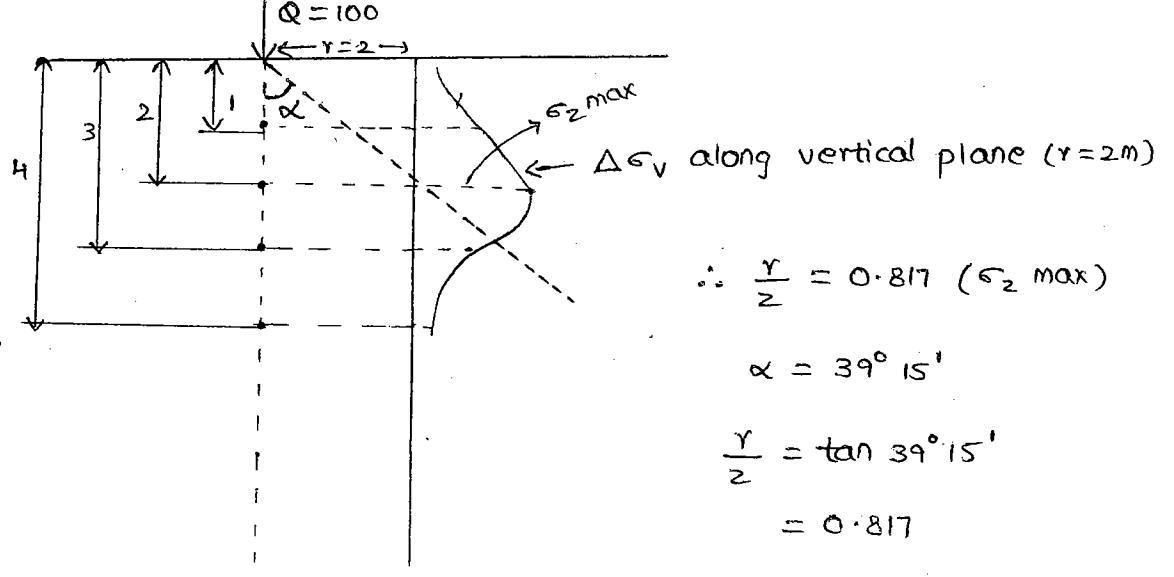
$$= \frac{700}{2^2} (0.275)$$

$$\sigma_v = 47.8 \text{ kPa (or) } \text{KN/m}^2$$

\* Verticle stress distribution on horizontal plane :-

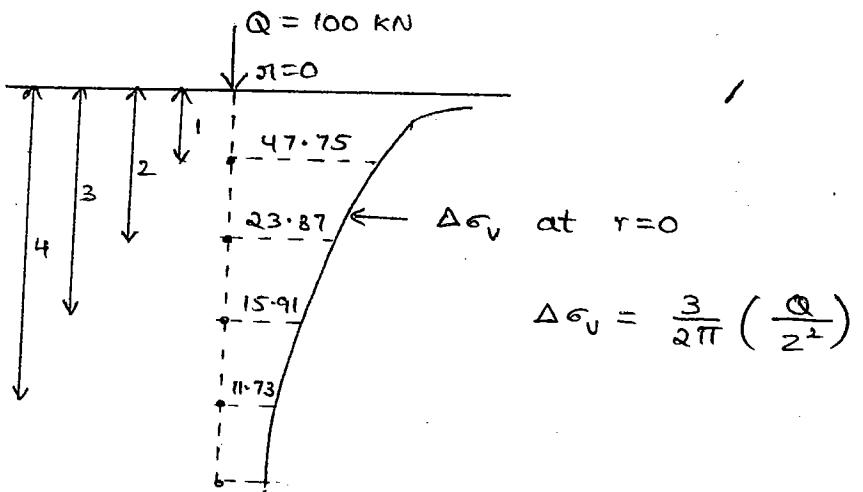


Verticle stress distribution on verticle plane :-

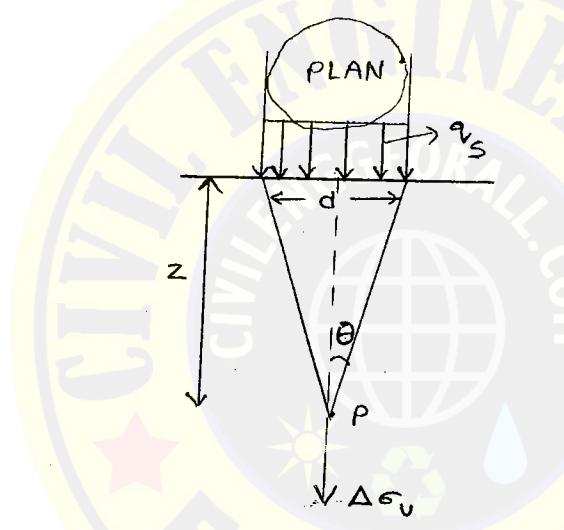


## Verticle stress distribution on verticle plane ( $r=0$ ) :-

(27)



Verticle stress due to circular loaded area :-



$$\tan \theta = \frac{r}{z}$$

$$\Delta\sigma_v = q_s' (\text{I}_{\text{circular}})$$

$$= q_s \left[ 1 - \left( \frac{1}{1 + \left( \frac{r}{z} \right)^2} \right)^{3/2} \right]$$

$$\Delta\sigma_v = q_s [1 - \cos^3 \theta]$$

$q_s$  = load intensity.

P.g No:- 44

Given  $d = 2 \text{ m}$ ,  $q_s = 100 \text{ kN/m}^2$ ,  $z = 1 \text{ m}$ ,  $r = 1 \text{ m}$

$$\tan \theta = \frac{r}{z} = \frac{1}{1} = 1$$

$$\theta = 45^\circ$$

$$\Delta\sigma_v = q_s (1 - \cos^3 \theta)$$

$$= 100 (1 - \cos^3 45)$$

$$= 64.65 \text{ kN/m}^2$$

Note:-

If  $Q = 750 \text{ kN}$  is given then  $q_s = ?$

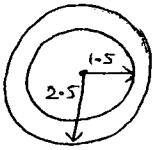
$$d = 2 \text{ m}$$

$$q_s = \frac{750}{\pi (2)^2} = 238 \text{ kN/m}^2$$

$$q_s = \frac{Q}{A_f}$$

Ex:- For shallow surface

$$\Delta \epsilon_v = q_s \left[ \left( 1 - \cos^3 \theta \right)_{\text{outer}} - \left( 1 - \cos^3 \theta \right)_{\text{inner}} \right]$$



Ex:-

$$\frac{\Delta \epsilon_A}{\Delta \epsilon_B} = \frac{q_s (1 - \cos^3 \theta_1)_A}{q_s (1 - \cos^3 \theta_2)_B}$$

$$\tan \theta_1 = \frac{r}{z_1} = \frac{1}{1}$$

$$\theta_1 = 45^\circ$$

$$\tan \theta_2 = \frac{1}{2} = 0.5$$

$$\theta_2 = 26^\circ 33'$$

$$\begin{aligned} \frac{\Delta \epsilon_A}{\Delta \epsilon_B} &= \frac{100 (1 - \cos^3 45)}{100 (1 - \cos^3 26^\circ 33')} \\ &= 2.27 \end{aligned}$$

Strip footing:-

$$\tan \alpha_1 = \frac{x}{z}$$

$$\tan \alpha_2 = \frac{B_f + x}{z}$$

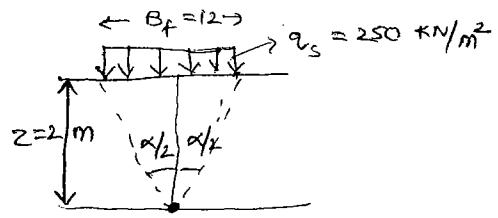
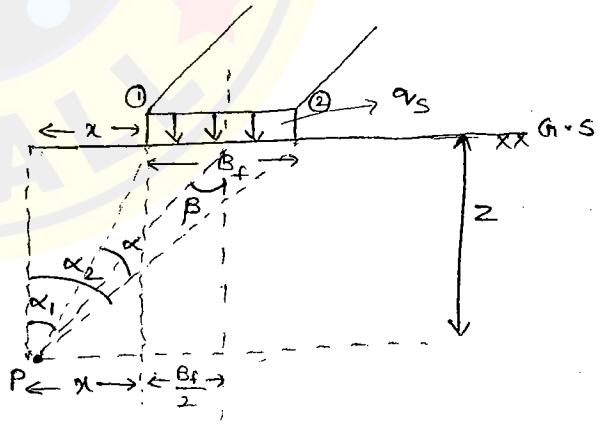
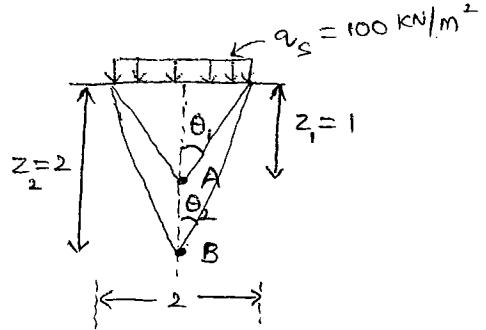
$$\tan \beta \geq \frac{x + (\frac{B_f}{2})}{z}$$

$$\epsilon_z(P) = \frac{q_s}{\pi} \left[ \alpha + \sin \alpha \cos 2 \beta \right]$$

$$\Delta \epsilon_v(\text{centre}) = \frac{q_s}{\pi} [\alpha + \sin \alpha]$$

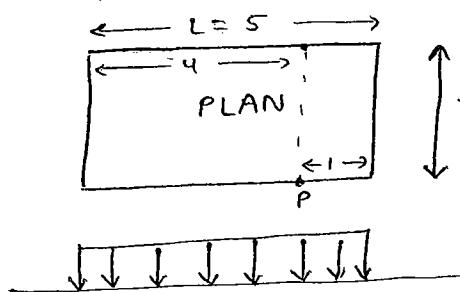
Ex:-

$$\epsilon_v(\text{centre}) = \frac{q_s}{\pi} (\alpha + \sin \alpha)$$



## Faculties concept

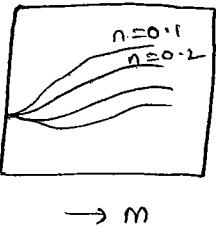
Ex:-)



$$z = 2m$$

Find at 'P'

$$I_f \uparrow$$



$$\Delta \epsilon_v = q_s (I_{f_1} + I_{f_2})$$

For  $I_{f_1}$ ,

$$m = \frac{L_1}{2} = \frac{4}{2}$$

$$n = \frac{B_1}{2} = \frac{3}{2}$$

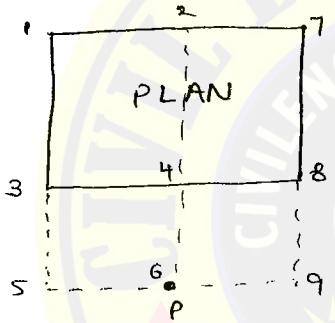
For  $I_{f_2}$

$$m = \frac{L_2}{2} = \frac{1}{2}$$

$$n = \frac{B_2}{2} = \frac{3}{2}$$

using this  $m, n$  values in chart we can find  $I_f$

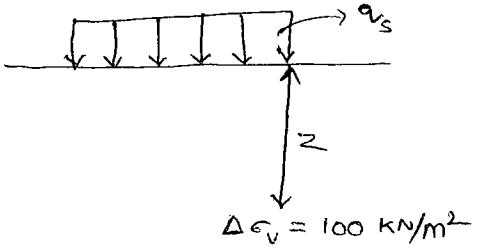
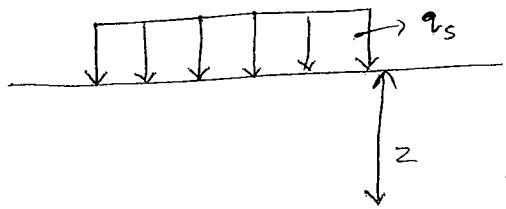
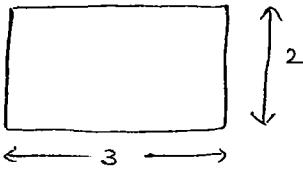
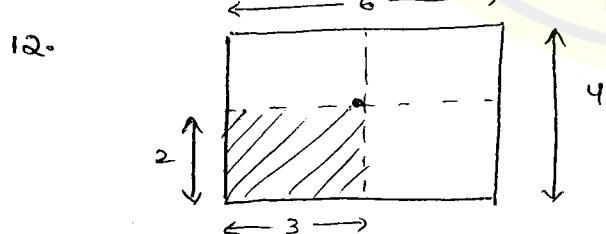
Ex:-)



point is given outside the plan  
so you can draw imaginary line

$$\Delta \epsilon_v = 2 \left[ q_s (I_{f_{(1-2-3-4-5-6)}} - I_{f_{(3-4-5-6)}}) \right]$$

P.g. No:- 44



$$\Delta \epsilon_v (\text{centre}) = 4 \left[ q_s (I_f)_{\text{shaded}} \right]$$

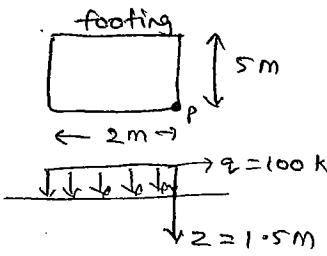
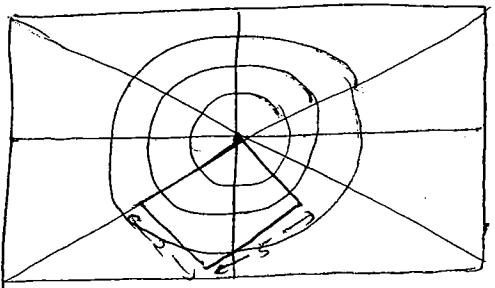
$$= 4 [A \epsilon_{\text{shaded}}]$$

$$= 4 (100)$$

$$= 400 \text{ kN/m}^2$$

## Newmark's influence chart :-

$$\Delta \sigma_v(p) = q_s(N) I_N$$



$$N_{\max} = \frac{1}{I_N} = 200 \text{ sectors}$$

$N_{\min} = 0$  (when point is far away from footing then sectors is zero).

P.g No:- 43

3. Given  $I_N = 0.005$ ,  $q = 40 \text{ t/m}^2$ ,  $n = 6$

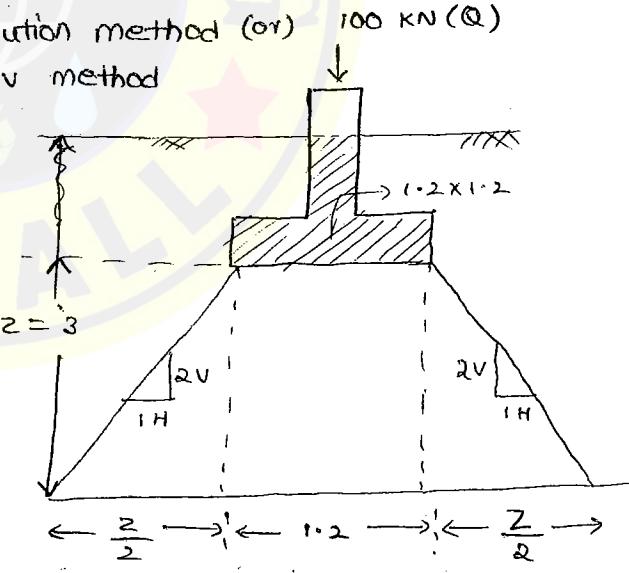
$$\begin{aligned}\Delta \sigma_v(c) &= q_s \cdot N \cdot I_N \\ &= 40 \times 6 \times 0.005 \\ &= 1.2 \text{ t/m}^2 \text{ [centre]}\end{aligned}$$

If point is located at corner the  $\Delta \sigma_v$  value decreases  
 $\therefore < 1.2 \text{ t/m}^2$  [corner]

Approximate method :- ~~(1)~~ 26° distribution method (or) ~~(2)~~  $1H:2V$  method

$$\begin{aligned}\Delta \sigma_v &= \frac{Q}{A_f} \\ &= \frac{100}{1.2 \times 1.2} = 69 \text{ KN/m}^2\end{aligned}$$

$$\begin{aligned}\Delta \sigma_v &= \frac{Q}{(B+z)^2} = \frac{100}{(1.2+3)^2} \\ &= 5.69 \text{ KN/m}^2\end{aligned}$$



P.g No:- 44

13. Given  $z = 1 \text{ m}$

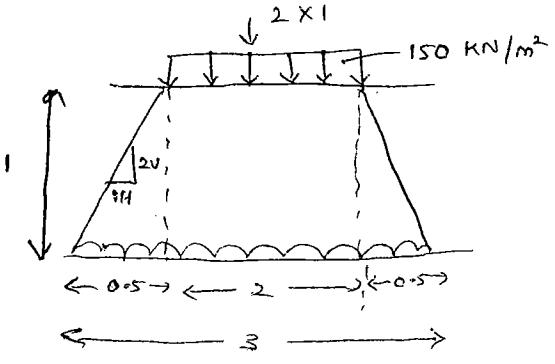
$$\sigma = \frac{F}{A}$$

$$F = \sigma \times A$$

$$= 150 \times (2)$$

$$Q = F = 300 \text{ KN}$$

$$\begin{aligned}\text{If } 2V = 1H \\ 1V = 0.5H\end{aligned}$$



$$\Delta \sigma_v(1m) = \frac{300 \text{ kN}}{3 \times 2} = 50 \text{ kN/m}^2$$

2) Equivalent point load method :-

$$\begin{aligned} F &= \sigma \times A \\ &= 150 \times (0.5 \times 1) \\ &= 75 \text{ kN} \end{aligned}$$

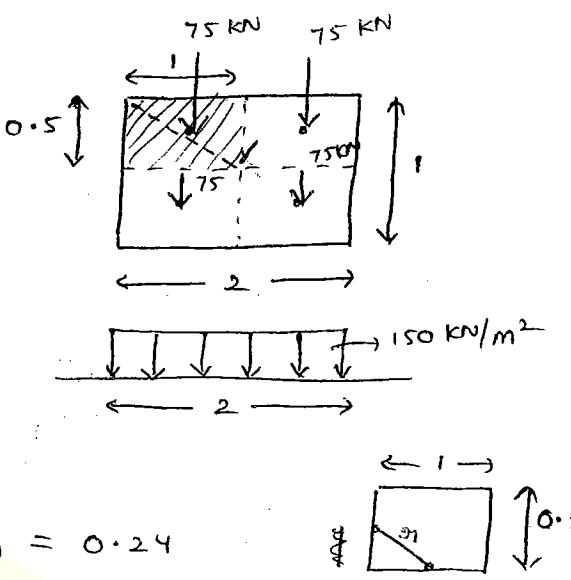
$$\sigma = \sqrt{\left(\frac{0.5}{2}\right)^2 + \left(\frac{1}{2}\right)^2}$$

$$\sigma = 0.56$$

$$\frac{\sigma}{z} = \frac{0.56}{1} = 0.56$$

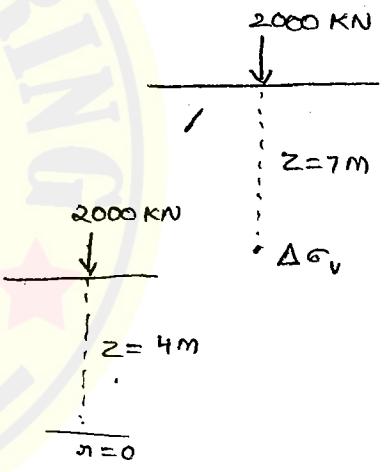
$$I_B \text{ (Boussinesq equation formula use)} = 0.24$$

$$\Delta \sigma_v(1m) = 4 \left[ \frac{Q}{z^2} (I_B) \right]$$



$$\begin{aligned} 4. \quad \Delta \sigma_v &= (I_B) \cdot \frac{Q}{z^2} \\ &= 0.4775 \times \frac{2000}{7^2} \\ &= 20 \text{ kN/m}^2 \end{aligned}$$

$$\begin{aligned} 5. \quad \tau_{(r_2)} &= [\Delta \sigma_v] \frac{r}{z} \\ &= \left[ \frac{3}{2\pi} \left( \frac{1}{1+(r/2)^2} \right)^{5/2} \frac{Q}{z^2} \right] \cdot \left( \frac{0}{4} \right) \\ &= 0 \end{aligned}$$

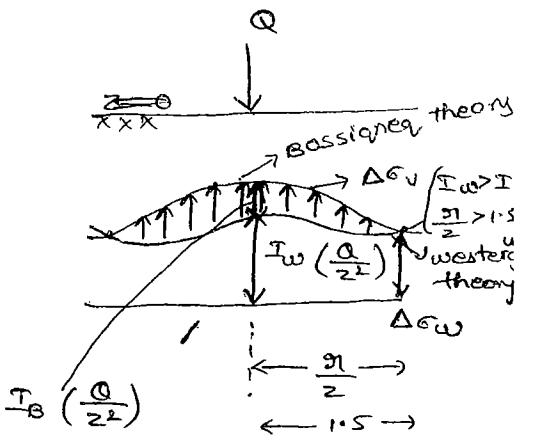


$$6. \quad I_B \left( \frac{Q}{z^2} \right) = 0.4775$$

$$= \frac{3}{24}$$

$$I_B = \frac{3}{2\pi} \left( \frac{1}{1+(1.5)^2} \right)^{2.5}$$

$$I_w = \frac{31}{2\pi} \left( \frac{1}{1+2(1.5)^2} \right)^{2.5}$$



Boussinesq

Westergaard's

1. Isotropic

1. Anisotropic

2.  $\frac{\sigma}{z} = 0$ ,  $I_B > I_w$

2.  $\frac{\sigma}{z} = 0$ ,  $I_w < I_B$

$$\Delta \sigma_v(B) > \Delta \sigma_v(w)$$

$$3. \quad \frac{\sigma}{z} = 1.5, \quad I_B = I_w$$

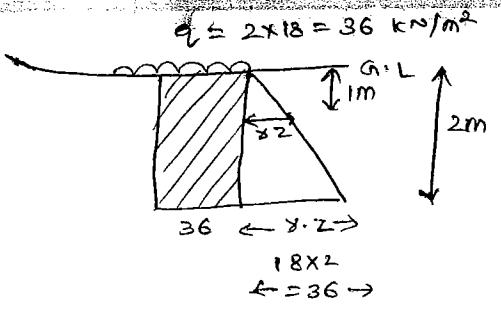
$$3. \quad \frac{\sigma}{z} > 1.5, \quad I_w > I_B$$

11.

$$36 \text{ kN/m}^2$$

P.Q. No. 1 - 44

$$\begin{bmatrix} \sigma_x & T_{yx} & T_{zx} \\ T_{xy} & \sigma_y & T_{zy} \\ T_{xz} & T_{yz} & \sigma_z \end{bmatrix}$$



Three normal stresses ( $\sigma_x, \sigma_y, \sigma_z$ ) and 6 shear stresses

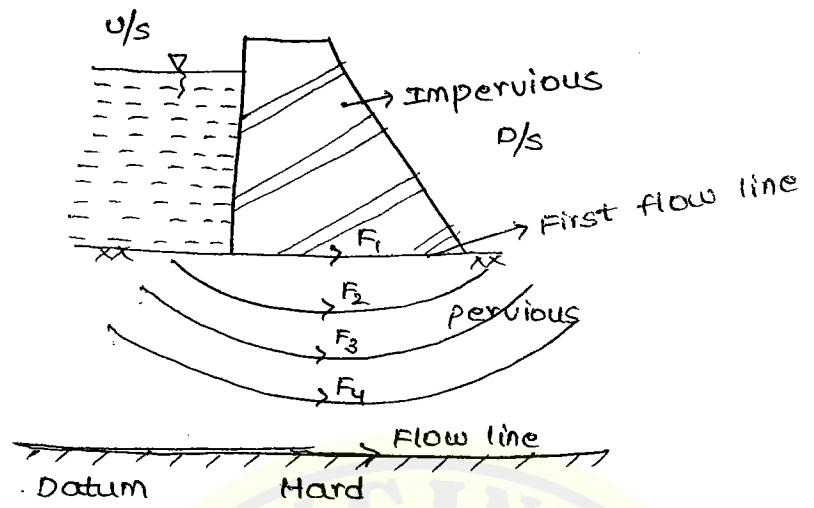
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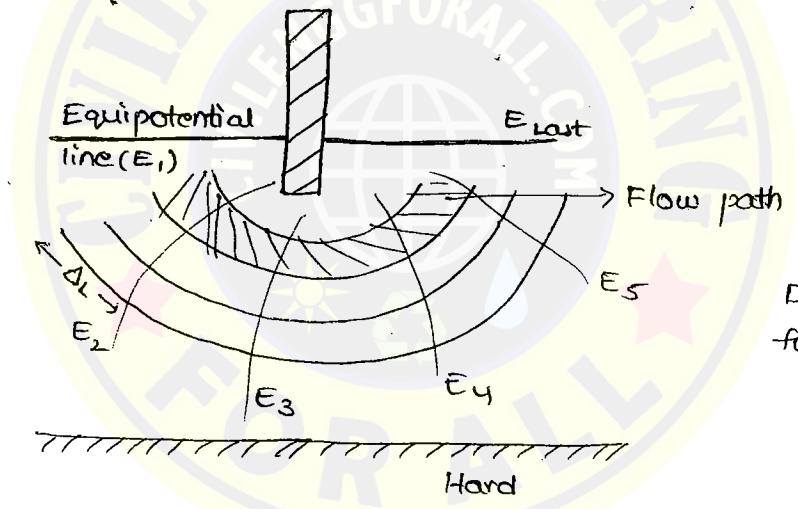
# UNIT - 9

## SEEPAGE ANALYSIS

Flow line :-



Flow path :-



Discharge is same  
for all chambers

$$H_1 - (H_2) = \text{Head capacity seepage}$$

$$H_{\text{net}} = H_1$$

$$H_{\text{net}} = N_o(\Delta H)$$

$$\Delta H = \frac{H_{\text{net}}}{N_o}$$

$$\Delta H = \frac{H_1 - H_2}{N_o}$$

Seepage quantity ( $q$ ):-

$$q = k \cdot i \cdot A$$

$$= k \cdot \frac{\Delta h}{\Delta x} \cdot (1 \times \Delta y)$$

$$= k \cdot \Delta h \cdot \frac{\Delta y}{\Delta x}$$

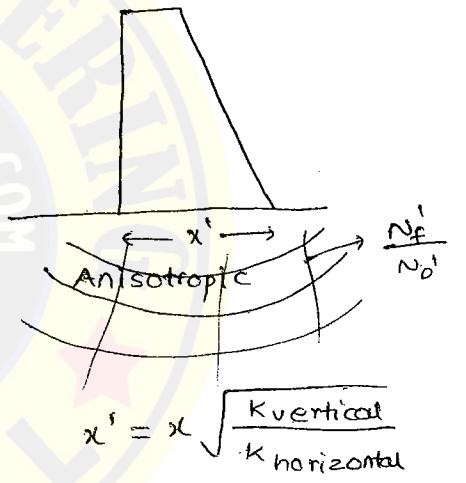
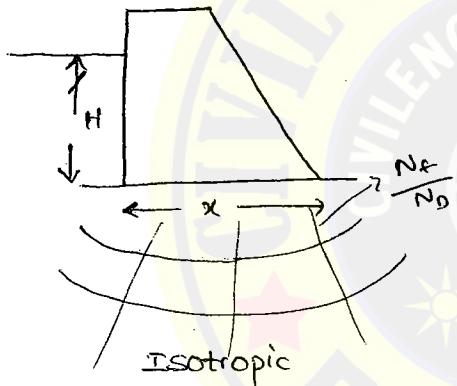
$$q = k \cdot \Delta h \cdot N_f$$

$$q_T = N_f (q_{\text{each}})$$

$$= k \cdot \frac{H_{\text{net}}}{N_D} (N_f)$$

$$q_{\text{loss}} = k \cdot H \cdot \frac{N_f}{N_D} \quad \text{m}^3/\text{sec}$$

Transformed section:-



Seepage pressure:-

$$P_s = \gamma_w \cdot h$$

$$h = H_{\text{net}} - N_D (\Delta h)$$

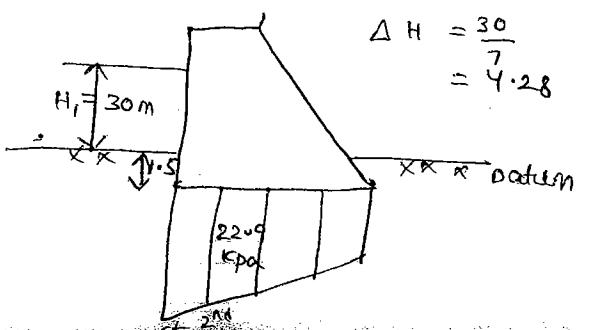
$$= (H_2 - H_1) - N_D (\Delta h)$$

Uplift pressure:-

$P_u = (\text{Hydraulic potential}) - \text{elevation head}$

$$= [30 - (\overset{2^{\text{nd}} \text{ drop}}{\rightarrow})(4.28)] - (-1.5 \text{ m})$$

$$= 22.9 \text{ m}$$



$$N_D = 7$$

$$\Delta H = \frac{30}{7} = 4.28$$

Use of flow net:-

$$i_{exit} = \frac{\Delta h}{\Delta L_{avg}}$$

$$i_{exit} < i_{critical}$$

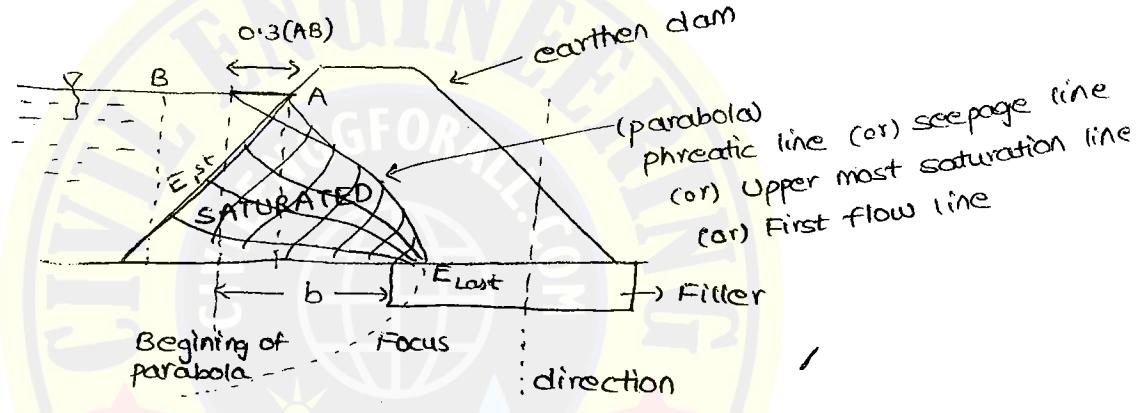
$$F.S = \frac{i_{critical}}{i_{exit}} > 1$$

(NO piping)

$$F.S < 1 \text{ (piping occurs)}$$

$$F.S = 1 \text{ (critical)}$$

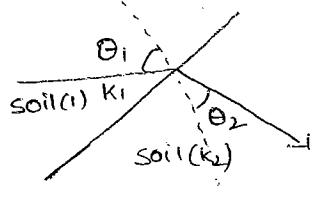
phreatic line (or) seepage line (or) top flow line:-



Discharge through body of the dam,  $q = ks$

$$s = \sqrt{(b^2 + H^2)} - b$$

Seepage in anisotropic soils:-



$$\frac{\tan \theta_1}{\tan \theta_2} = \frac{k_1}{k_2}$$

$$\frac{D_{15} \text{ (filter)}}{D_{15} \text{ (soil)}} \geq 5 \text{ (to allow water to pass)}$$

$$\frac{D_{15} \text{ (filter)}}{D_{85} \text{ (soil)}} \leq 5 \text{ (To prevent soil particle movement)}$$

P.T.O NO:- 39

8. Given  $N_f = 4$ ,  $N_d = 15$ ,  $\Delta H = 3m$ ,  $K = 2 \times 10^{-5} m/s$

$$\begin{aligned} q &= K \cdot H \left( \frac{N_f}{N_d} \right) & \Delta H = H_1 - H_2 \\ &= 2 \times 10^{-5} \times 3 \times \left( \frac{4}{15} \right) & \Delta H = H_{\text{net}} \\ &= 1.6 \times 10^{-5} m^3/s \end{aligned}$$

2. Given  $N'_f = 4$ ,  $N'_d = 16$ ,  $K_H = 4 \times 10^{-7} m/\text{sec}$ ,  $K_v = 1 \times 10^{-7} m/\text{sec}$

$$\begin{aligned} 1. \quad q &= K_{\text{equivalent}} \cdot (H_{\text{net}}) \left( \frac{N'_f}{N'_d} \right) \\ &= \sqrt{4 \times 10^{-7} \times 1 \times 10^{-7}} \quad (20) \left( \frac{4}{16} \right) \\ &= 2 \times 10^{-7} (5) \\ &= 10 \times 10^{-7} \\ &= 10^{-6} m^3/\text{sec} \end{aligned}$$

UNIT - II

(3)

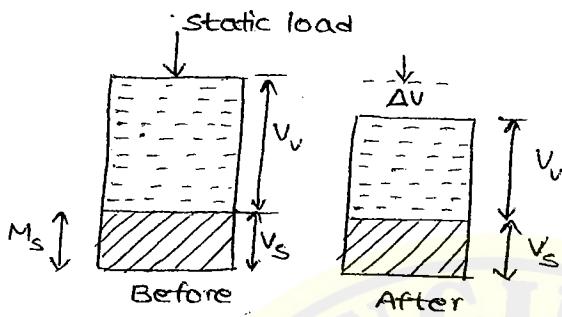
CONSOLIDATION

## Compressibility :-

Expulsion of 'any voids' compressibility occurs.

Ex:- Air is the highly compressible material.

## Consolidation :-



Expulsion of the water from the saturated soil due to static load is called consolidation.

1. saturated soil
2. static load
3. water voids are expelled
4. Long process
5. After making or building structures, consolidation occurs after construction as well as before construction.

Factors affecting consolidation :-

- a. For coarse grained soils (Gravel sand) :-

$$k \text{ (permeability)} = 10^0 \text{ cm/sec} \quad (\text{Fast consolidation})$$

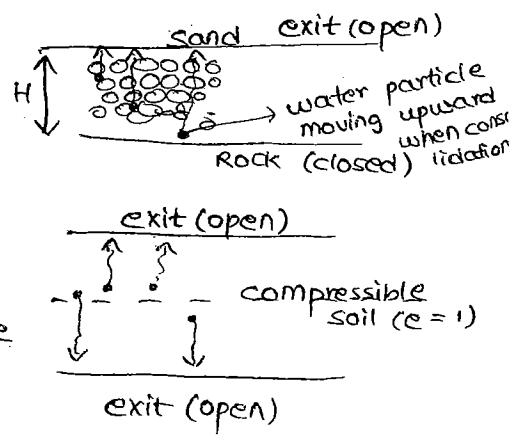
$$k = 10^{-7} \text{ cm/sec} \quad (\text{slow consolidation}),$$

Drainage (d) has two types

1. Single drainage,  $d = H$
2. Double drainage,  $d = \frac{H}{2}$

In double drainage, water particle are moving upward <sup>or</sup> downward because both sides are open.

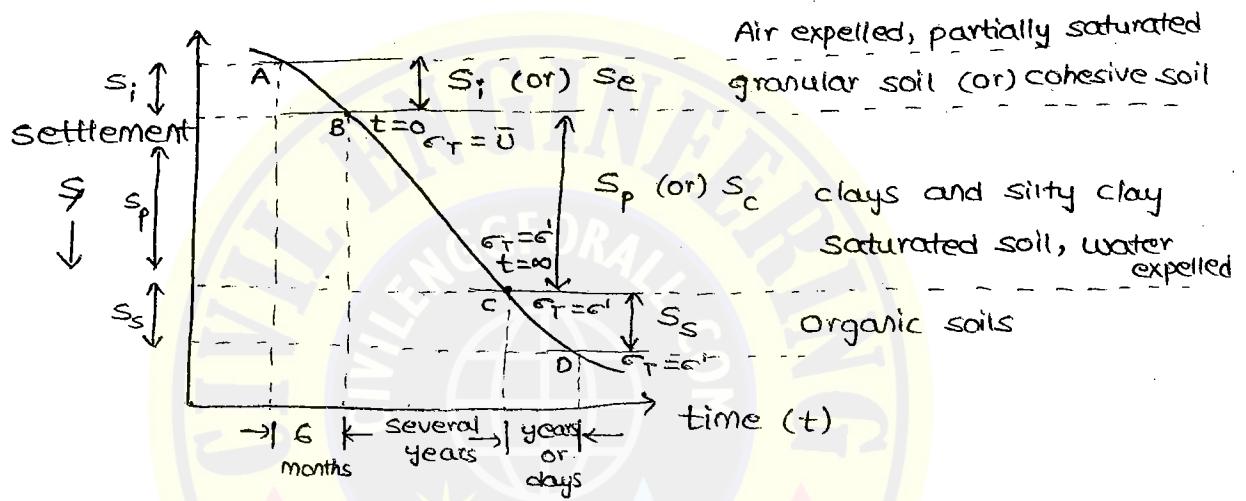
$$T_v = \frac{c_v t}{d^2}$$



(b) For clays:- (F.G.S = silt, clay)

1. permeability is low ( $t \rightarrow$  high, several years)
2.  $d \rightarrow S.D$  and double drainage
3. Expulsion of adsorbed water
4. slipping of grains.
5. sand drain technique is one of the ground improvement technique for clay to avoid the large settlement after construction.

Stages (or) Types of consolidation (or) compression:-



$$S_{\text{total}} = [S_{\text{immediate}} \text{ (or) } S_{\text{elastic}}] + [S_{\text{primary}} \text{ (or) } S_{\text{consolidation}} \\ \text{ (or) } S_{\text{time dependent}}] + [S_{\text{secondary compression}} \text{ (or) } S_{\text{creep}}]$$

$S_{\text{total}} = S_i + S_p + S_s$

For sand

$$S_T = S_i + 0 + 0$$

$S_T = S_i$

For clays

$$S_T = 0 + S_p + 0$$

$S_T = S_p$

For Organic soils

$$S_T = 0 + 0 + S_{\text{secondary}}$$

$S_T = S_c$

## In consolidated soil (or) primary consolidation :-

(33)

$$\rightarrow t = 0$$

$$\sigma_T = \sigma' + \bar{U}$$

$$= 0 + \bar{U}$$

$$\boxed{\sigma_T = \bar{U}}$$

∴ If in begining of the consolidation settlement  $t=0$ , then the load is carried by excess pore water

$$\rightarrow t = \infty$$

$$\sigma_T = \sigma' + \bar{U}$$

$$= \sigma' + 0$$

$$\boxed{\sigma_T = \sigma'}$$

∴ At the end of the consolidation settlement  $t = \infty$  (several years) then the load is carried by effective stress.

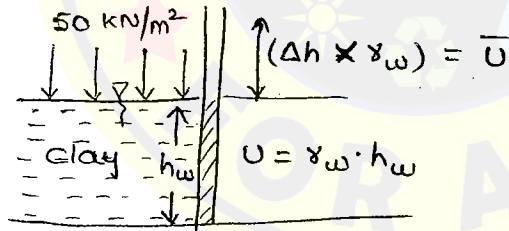
$\bar{U}$  = excess pore water pressure

## In secondary consolidation :-

$$\sigma_T = \sigma' \text{ (constant)}$$

Terzaghi's piston and spring analogy model:-

1. Excess pore pressure ( $\bar{U}$ ) :-



$$q = \sigma = 50 \text{ kN/m}^2$$

$$50 = \Delta h \times \gamma_w$$

$$\Delta h = 5 \text{ m}$$

Hydro dynamic lag :-

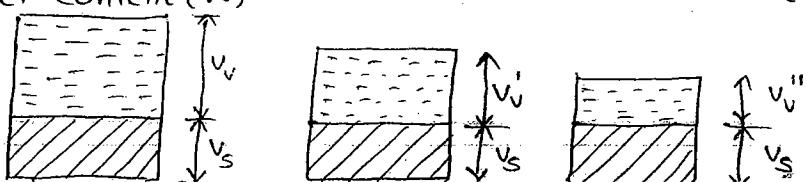
During consolidation (time is intermediate)

Decreasing

Increasing

constant

- |                                       |                                    |                                |
|---------------------------------------|------------------------------------|--------------------------------|
| 1. volume of voids ( $v_v$ )          | 1. weight of solids ( $\gamma$ )   | 1. Total stress ( $\sigma_T$ ) |
| 2. voids ratio ( $e$ )                | 2. shear strength                  | 2. Volume of solids            |
| 3. Excess pore pressure ( $\bar{U}$ ) | 3. Effective stress ( $\sigma'$ )  | 3. Degree of saturation        |
| 4. volume ( $v$ )                     | 4. Degree of consolidation ( $U$ ) |                                |
| 5. Water content ( $w$ )              |                                    |                                |

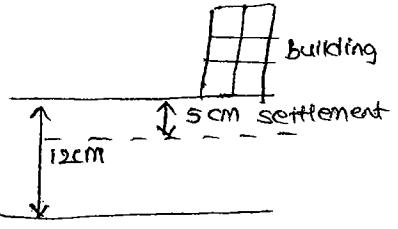


### Degree of consolidation (U) :-

After some years, the settlement occurs

$$U = \frac{5}{12} \times 100$$

$$= 42\%.$$



Again some more years, the settlement will be more. So

Degree of consolidation is increasing.

### Coefficient of volume compressibility ( $m_v$ ) :-

$$m_v = \frac{\Delta v}{v} / \Delta \sigma'$$

$$m_v = \frac{\Delta v}{v \cdot \Delta \sigma'}$$

$$a_v \text{ and } m_v = \frac{m^2}{kN} = \frac{1}{e}$$

$$m_v = \left( \frac{\Delta H}{H} \cdot \frac{A}{A} \right) / \Delta \sigma'$$

$$m_v = \frac{\Delta H}{H} \left( \frac{1}{\Delta \sigma'} \right)$$

$$= \left( \frac{\Delta e}{1+e} \right) \left( \frac{1}{\Delta \sigma'} \right)$$

$$= \frac{\Delta e}{\Delta \sigma'} \left( \frac{1}{1+e} \right)$$

$$m_v = \text{or } a_v \frac{a_v}{1+e}$$

$$\therefore \frac{\Delta H}{H} = \frac{\Delta e}{1+e}$$

### Coefficient of compressibility ( $a_v$ ) :-

$$a_v = \frac{\Delta e \downarrow}{\Delta \sigma' \uparrow} = \frac{e_i - e_f}{\Delta \sigma'}$$

Ex:- For same  $\Delta \sigma'$ , which of soil will have more ( $a_v$ ) [ ]

- a) Gravel      b) Sand      c) Clay      d) None

## Consolidation Settlement ( $S_f$ ):-

(34)

$$1. \quad m_v = \frac{\Delta v}{v} \cdot \frac{1}{\Delta \epsilon'}$$

$$m_v = \frac{\Delta H}{H} \left( \frac{1}{\Delta \epsilon'} \right)$$

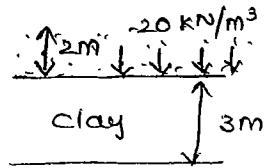
$$S_f = \boxed{\Delta H = m_v \cdot H \cdot \Delta \epsilon'} = \frac{1}{E_c} (H) (\Delta \epsilon')$$

$E_c$  = compression modulus

Ex:-  $q = \sigma' = 20 \text{ kN/m}^2 \cdot z_{\text{fill}}$

$$= 20 (2)$$

$$\Delta \epsilon' = 40 \text{ kN/m}^2$$



$$S_f = \Delta H = m_v \cdot H \cdot \Delta \epsilon'$$

$$= 5 \times 10^{-4} \times 3 \times 40$$

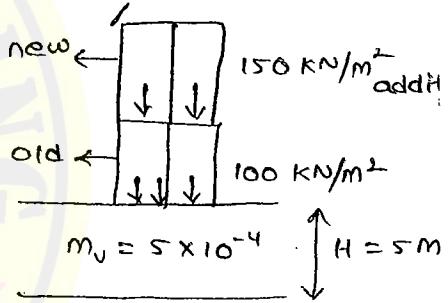
$$= 60 \text{ mm}$$

Ex:-

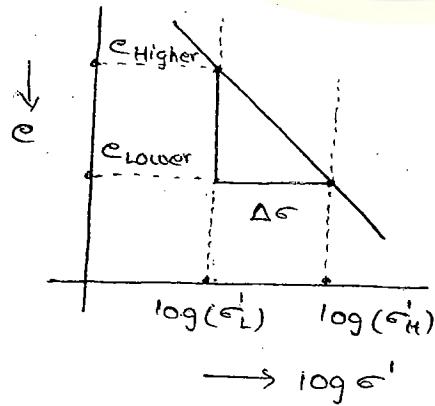
$$\frac{S_{\text{new}}}{S_{\text{old}}} = \frac{m_v \cdot H \Delta \epsilon'}{m_v \cdot H \cdot \Delta \epsilon'}$$

$$= \frac{(150 + 100)}{100}$$

$$= 2.5$$



Coefficient of laterally confined soils :-



$c_c$  = compression index

$$c_c = \frac{\Delta e}{\log \epsilon'_H - \log \epsilon'_L}$$

$$= \frac{e_H - e_L}{\log \epsilon'_H - \log \epsilon'_L} \quad (\text{compute log cycle})$$

$$c_c = \frac{\Delta e}{l}$$

$$c_c = \frac{e_H - e_L}{\log \left( \frac{e_f'}{e_i'} \right)}$$

$$c_c = \frac{\Delta e}{\log \left( \frac{e_0' + \Delta e}{e_0'} \right)}$$

$$\Delta e = c_c \log \left( \frac{e_0' + \Delta e}{e_0'} \right)$$

$$\frac{\Delta H}{H} = \frac{\Delta e}{1 + e_0}$$

$$\Delta H = \Delta e \cdot \frac{H}{1 + e_0}$$

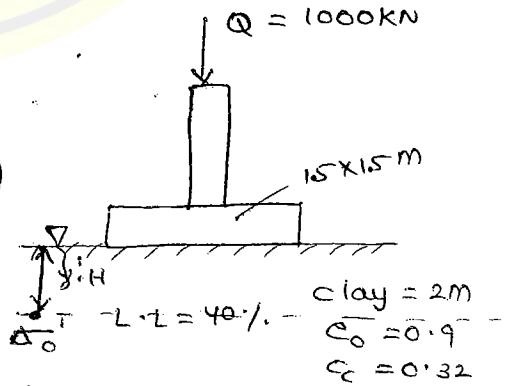
$$S_{\text{consolidation}} = \frac{c_c}{1 + e_0} (H) \log \left( \frac{e_0' + \Delta e}{e_0'} \right)$$

where,

$$c_c = \text{coefficient of compression index of clay}$$

$$= 0.009 (w_L - 10\%)$$

$S_{\text{consolidation}} \propto c_c$
$S_{\text{consolidation}} \propto \frac{1}{e_0}$
$S_{\text{consolidation}} \propto H$



$$S_{\text{consolidation}} = \frac{c_c}{1 + e_0} H \cdot \log \left( \frac{e_0' + \Delta e}{e_0'} \right)$$

$$e_0' = s' \cdot H$$

$$= 10 (1)$$

$$= 10 \text{ kN/m}^3$$

$$\Delta e = \frac{1000 \text{ kN}}{225 \text{ m}^2} = 440 \text{ kN/m}^2$$

$$S_c = \frac{0.32}{1 + 0.9} \times \frac{2000}{2} \times \log \left( \frac{10 + 440}{10} \right)$$

Note :-

- Max settlement occurs when applied load ( $\Delta \sigma$ ) is more
- Max settlement occurs when ' $c_c$ ' is more
- Max settlement occurs when 'H' is more

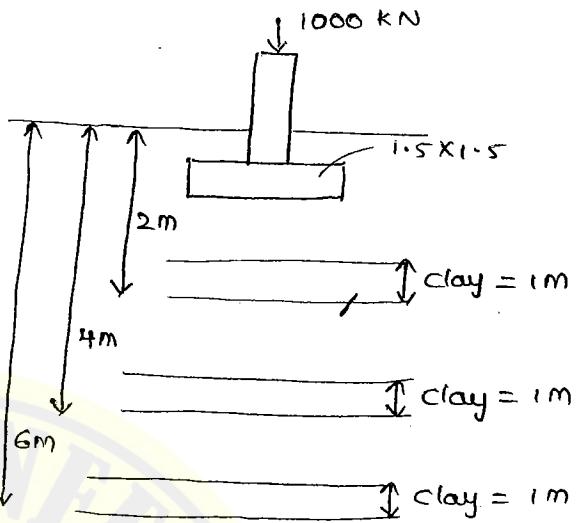
Ex:-

For the following cases.

$c_c, c_o, H = \text{same}$

In which case settlement is minimum?

- when clay is 2m below footing
- when clay is 4m below
- when clay is 6m below
- same

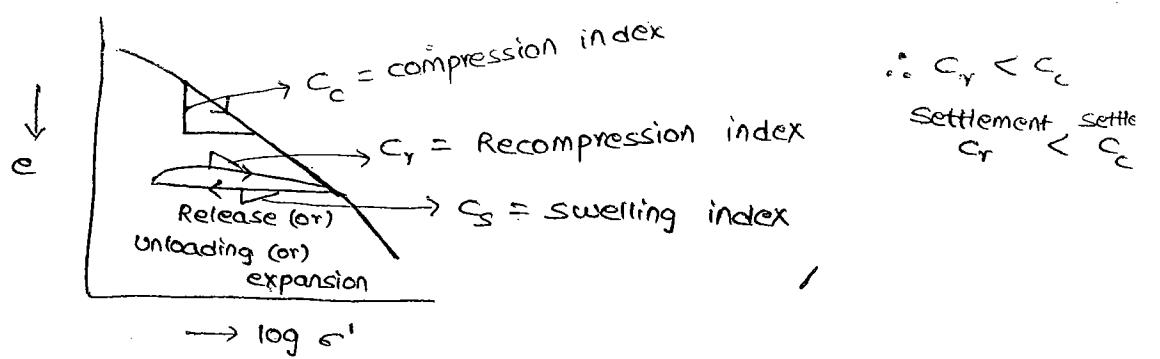
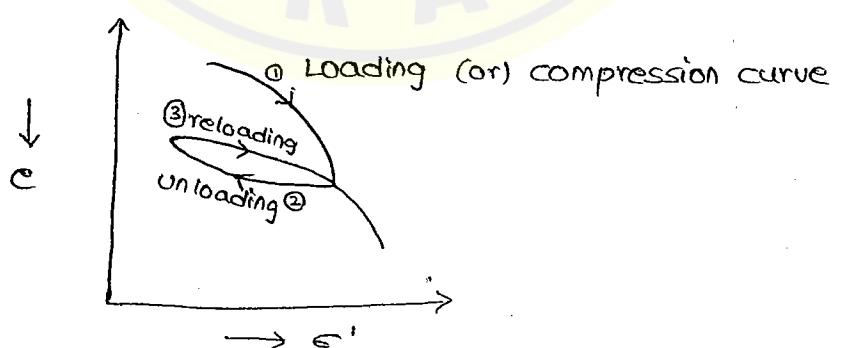


Ans:- (C) when goes down settlement is decreasing, settlement depends upon  $\Delta \sigma$  value.

Note:-

When settlement is zero ( $s=0$ ) such footing are called compensated footing (or) floating foundation.

Coefficient of laterally confined soils:-



## Consolidation of undisturbed specimens :-

### 1. Preconsolidated or Over consolidated soil:-

- a. void ratio decreased
- b. settlement decreased
- c. unit weight increased
- d. bearing capacity increased.

### 2. Under consolidated soil:-

- a. void ratio increases
- b. unit weight decreases
- c. bearing capacity decreases
- d. settlement increases

Ex:-

1. Excess pore pressure (or) hydrodynamic pressure (or) hydrostatic pressure is more at Middle
2. Excess pore pressure is minimum at the end of the consolidation is bottom (time =  $\infty$ ) and maximum at top ( $t=0$ )

Degree of consolidation ( $U$ ) and Time Factor ( $T_U$ ):-

$$T_U = \frac{\pi}{4} \left( \frac{u_A}{100} \right)^2, \text{ for } U \leq 60\%.$$

$$T_U = 1.781 - 0.933 \log_{10}(100 - U\%), \text{ for } U > 60\%.$$

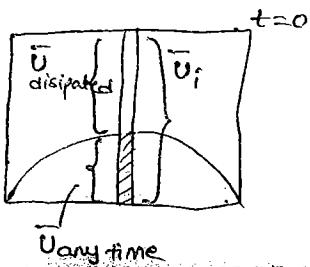
$U\%$	$T_U$
0%	0
:	:
100%	$\infty$

$$U = \left( \frac{\text{Settlement at any time}}{\text{Ultimate Settlement}} \right) \times 100$$

$$U = \left( \frac{s}{s_f} \right) \times 100$$

$$U = \frac{\bar{U}_{\text{initial}}(t=0) - \bar{U}_{\text{any time}}}{\bar{U}_{\text{initial}}(t=0)} \times 100$$

$$U = \frac{\bar{U}_{\text{Undissipated}}}{\bar{U}_{\text{Initial}}} \times 100$$



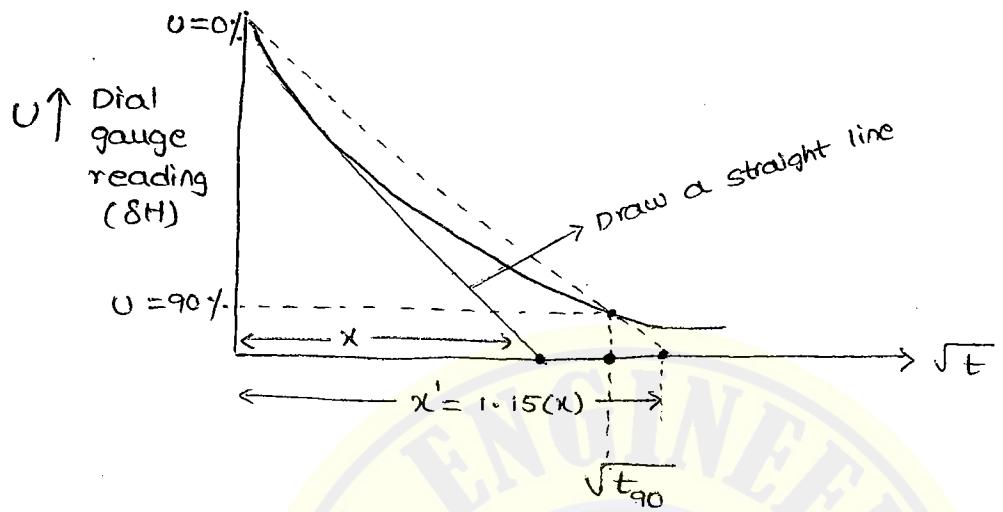
## Determination of coefficient of consolidation ( $C_v$ ):-

### i. Time fitting method

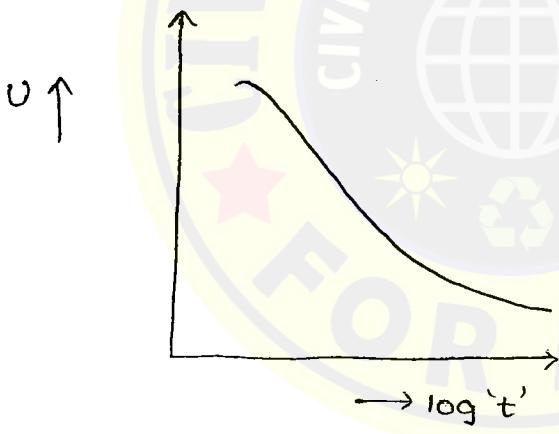
a. square root of time fitting method (Taylor's)

b. logarithm of time fitting method (Casagrande method)

a. square root of time fitting method :-



b. Logarithm of time fitting method:-



Ex:- During consolidation load transfers from pores to grain

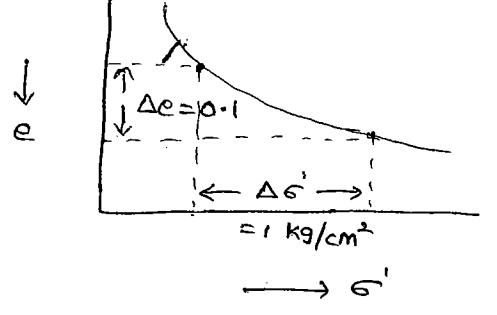
P.g No:- 50

$$6. \frac{\Delta H}{H} = \frac{\Delta e}{1+e_0}$$

$$\Delta H = H \left( \frac{\Delta e}{1+e_0} \right)$$

$$= 700 \left( \frac{0.1}{1+0.4} \right)$$

$$= 50 \text{ cm}$$



7. Given  $e_0 = 0.5$   $e_f = 0.2$

$$\frac{\Delta H}{H} = \frac{\Delta e}{1+e_0}$$

$$\Delta H = S = \frac{(e_0 - e_f)}{1+e_0} (H)$$

$$= \frac{0.5 - 0.2}{1+0.5} (10)$$

$$\Delta H = 2.0$$

16.

A

single drainage

$$d = H'$$

$$U = 50\%$$

$$t_1 = 10 \text{ min}$$

B

double drainage

$$d = \frac{H}{2}$$

$$U = 50\%$$

$$t_2 = ?$$

$$\frac{t_1}{t_2} = \left( \frac{d_1}{d_2} \right)^2 = \left( \frac{H}{H/2} \right)^2$$

$$\frac{10}{t_2} = 4$$

$$t_2 = 2.5 \text{ min}$$

17.

$$\text{settlement} = 1 \text{ cm}, \quad \sigma_0 = 1 \text{ kg/cm}^2, \quad \sigma_f = 2 \text{ kg/cm}^2$$

$$\text{settlement} = ?, \quad \sigma_0 = 2 \text{ kg/cm}^2, \quad \sigma_f = 4 \text{ kg/cm}^2$$

$$S = \frac{c_c H}{1+e_0} \log_{10} \left( \frac{\sigma_f}{\sigma_i} \right)$$

$$S_2 = \frac{c_c H}{1+e_0} \log_{10} \left( \frac{\sigma_f}{\sigma_i} \right)$$

$$1 = \log \left( \frac{2}{1} \right) = 2$$

$$S_2 = \log \left( \frac{4}{2} \right) = 2$$

$$2 S_2 = 2$$

$$S_2 = 1 \text{ cm}$$

20. Given  $k = 2$ ,  $m_v = \frac{1}{2}$   $c_{av} = ?$

$$c_{av} = \frac{k}{x_w \cdot m_v} = \frac{2}{\frac{1}{2}} = 4 \text{ times increased}$$

$x_w = \text{constant}$

(cont)

3F

$$C_{v_1} = \frac{k}{m v_1}$$

$$C_{v_2} = \frac{2k}{0.5 m v_1}$$

$$C_{v_2} = 4 (C_{v_1})$$

21.

A

double drainage

$$\frac{d}{2} = H$$

$$t_1 = t$$

B

single drainage

$$3d$$

$$t_2 = ?$$

$$\frac{t_1}{t_2} = \left(\frac{d_1}{d_2}\right)^2$$

$$\frac{t}{t_2} = \left(\frac{d_1}{3d}\right)^2$$

$$\frac{t}{t_2} = \frac{1}{36}$$

$$t_2 = 36t$$

23.

A

$$t_1 = 4 \text{ years}$$

$$U = 50\%$$

Single drainage

$$d_1 = H$$

B

$$t_2 = ?$$

$$U = 50\%$$

Double drainage

$$d_2 = \frac{H}{2}$$

$$\frac{t_1}{t_2} = \left(\frac{d_1}{d_2}\right)^2$$

$$\frac{4}{t_2} = \left(\frac{H}{\frac{H}{2}}\right)^2$$

$$t_2 = 1 \text{ year}$$

27.

$$T_v = \frac{C_v t}{d^2}$$

$$t = \frac{T_v \cdot d^2}{C_v}$$

$$t = \frac{T_v \cdot d^2}{\frac{k}{\gamma_w \cdot m_v}}$$

$$t = \frac{T_v \cdot d^2 - \gamma_w \cdot m_v}{k}$$

29. At  $t=0$ , the load is carried by pore water pressure and effective stress is zero.

$\therefore$  In piezometer the water is raised is equal to applied load.

Degree of consolidation (or) stage of consolidation ( $U$ )

$$U = \frac{\bar{U}_i - \bar{U}_{\text{any time}}}{\bar{U}_i}$$

$$= \frac{200 - 60}{200} \times 100$$

$$U = 70\%$$

At  $t=\infty$ ,  $\bar{U}_i = 200$ ,  $\bar{U}_{\text{any time}} = 0$

$$U = \frac{200 - 0}{200} \times 100\%$$

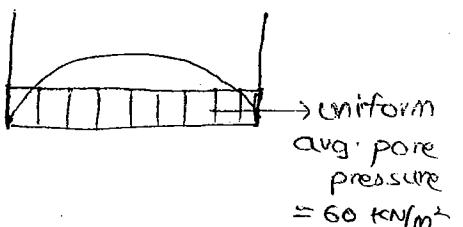
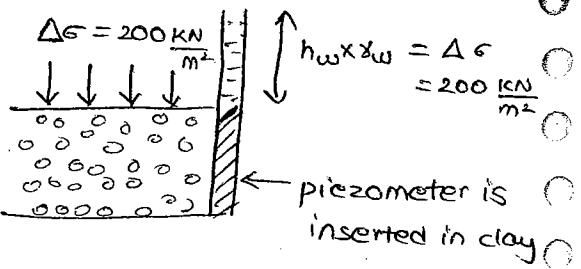
$$U = 100\%$$

At  $t=0$ ,  $\bar{U}_i = 200$ ,  $\bar{U}_{\text{any time}} = 200$

$$U = \frac{200 - 200}{200} \times 100$$

$$U = 0\%$$

$t$	$U\%$
0	0%
$\infty$	100%



30.  $s_1 = 80 \text{ mm}$        $s_2 = ?$

$t_1 = 4 \text{ years}$        $t_2 = ?$

$U = 60\%$ .       $U = 60\%$ .

In both cases  $U < 60\%$ .

$$T_v = \frac{\pi}{4} (U)^2$$

$$T_v = \frac{\pi}{4} \left[ \frac{s_{\text{any time}}}{s_{\text{max}}} \right]^2$$

$$\frac{S_v t}{d^2} = \frac{\pi}{4} \left[ \frac{s_t}{s_{\text{max}}} \right]^2$$

$$U = \frac{s_{\text{any time}}}{s_{\text{maximum}}} \times 100$$

(38)

$$\frac{c_v t}{d^2} = \frac{\pi}{4} \left( \frac{s_1 t}{s_{1\max}} \right)^2$$

$$\frac{c_v t}{d^2} = \frac{\pi}{4} \left( \frac{s_2 t}{s_{2\max}} \right)^2$$

$$\frac{s_1^2}{s_2^2} = \frac{t_1}{t_2}$$

$$\frac{t_1}{t_2} = \left( \frac{s_1}{s_2} \right)^2$$

$$= \left( \frac{4}{9} \right)^2 \cdot \frac{4}{9} = \left( \frac{80}{s_2} \right)^2$$

$$s_2 = 120 \text{ mm}$$

Complete Class Note Solutions  
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31.  $H = 4000 \text{ mm}$

$$s_{\max} = 50 \text{ mm}$$

single drainage

$$H = 4000 \text{ mm}$$

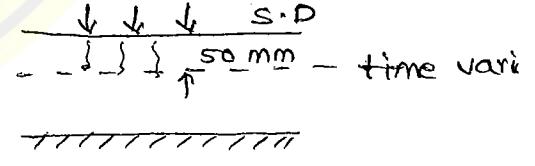
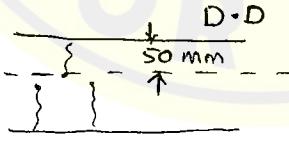
$$s_{\max} = ?$$

Double drainage

$$U = \frac{\text{variable}}{\text{constant}} \times 100$$

↓ ↓ ↓      ↓ ↓ ↓  
 Sanytime      S<sub>max</sub>

In single drainage settlement is same as well as in double drainage. But in S.D. time varies compare to double drainage. In S.D. time is low, in D.D. time is fast but settlement is same in both cases.



P-9 No :- 53

10.  $s = \frac{c_c}{1+c_0} H \log \frac{e'_0 + \Delta e}{e'_0}$

$$\Delta H = H(\Delta e)(m_v)$$

$$\Delta H = \frac{\Delta e}{1+e}(H)$$

13.  $s_f = \Delta H = \left( \frac{\Delta e}{1+e_0} \right) H$

$$s_f = \left( \frac{e_0 - e_f}{1+e_0} \right) H$$

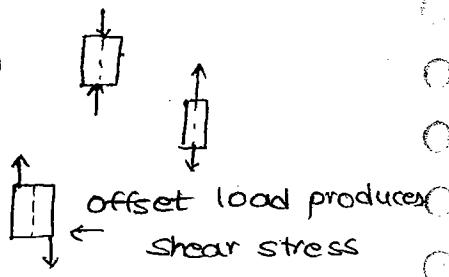
$$s_f \text{ at } 2000 = \left( \frac{1.00 - 0.92}{1+1.00} \right) (2000)$$

23-12-20

UNIT - 13SHEAR STRENGTH

Applied load

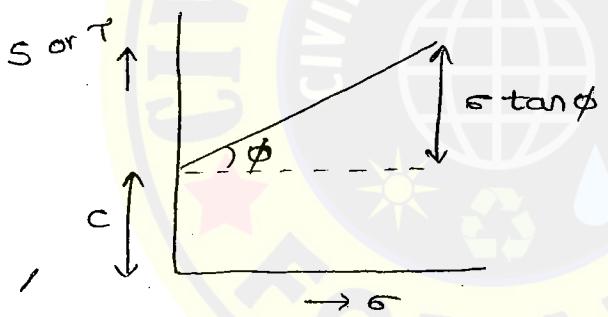
- compressive stress ( $\sigma_c$ )
- tensile stress ( $\sigma_t$ )
- shear stress ( $\tau$ )



Soil strength can be measured in shear strength ( $s$ ).

Contributors	soil type	Example	Significant	Minor contributor
Interlocking	$\phi$ - soils	sand, gravel	① & ②	-
$\phi$	c - soils	clay	clay ③	①
c	c- $\phi$	Murram	② & ③	①

Coulomb's Law :-



$$s = c + \sigma \tan \phi$$

$s$  = shear strength  $\text{KN}/\text{m}^2$

$c$  = cohesion  $\text{KN}/\text{m}^2$

$\phi$  = angle of internal friction (or) shear resistance

Notes:-

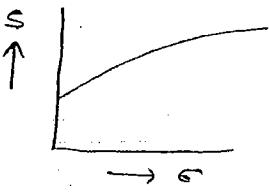
'c' and ' $\phi$ ' are not constant for a particular soil.

Mohr's theory :-

Very much used for the determination of shear strength of soils.

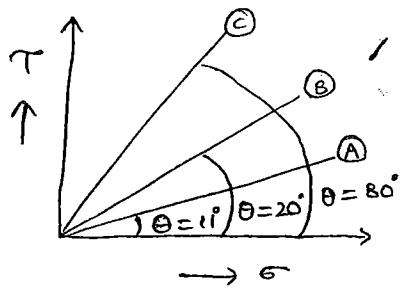
$$s = f(\sigma)$$

$s$  = normal stress



## Types of soil:-

1.  $\phi$  - soil
2. C - soil
3. C- $\phi$  - soil

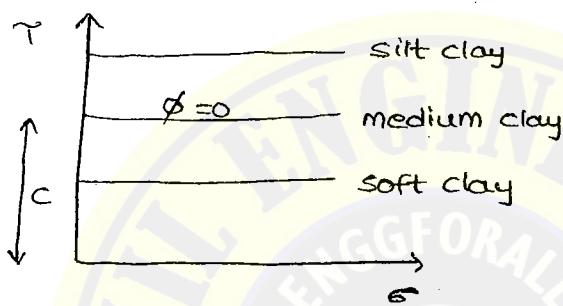


$\theta = 11^\circ \rightarrow$  size is small

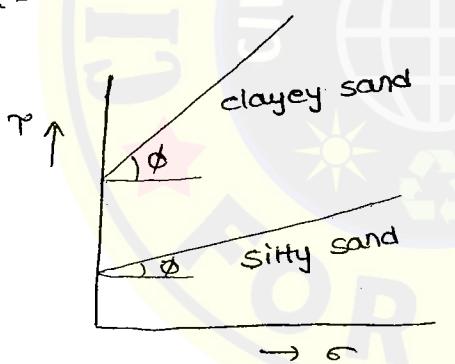
→ Dense state having a highest friction

→ Rounded particles having a low friction angle.

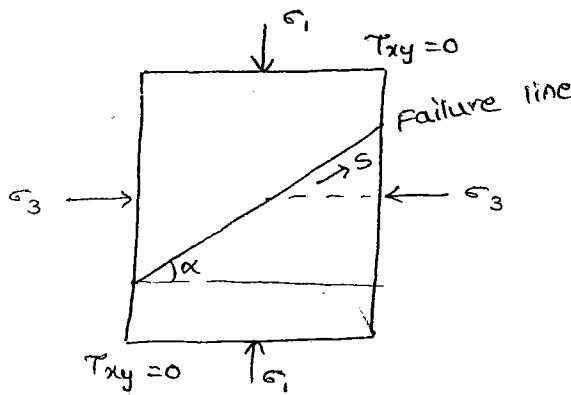
## C-soil:-



## C- $\phi$ soils:-



## Shear stress ( $T$ ), Mohr's circle diagrams:-



Major ( $\sigma_1$ ) and minor ( $\sigma_3$ ) principle planes (ab & ac) on which shear stress (or) Tangential shear stress acting is zero.

$T, \sigma_d \rightarrow$  induced stresses

$$\sigma_d = Deviatoric stress = (\sigma_1 - \sigma_3)$$

Terzaghi's concept:-

$$S = c' + \sigma' \tan \phi'$$

$$S = c' + (\sigma - u) \tan \phi'$$

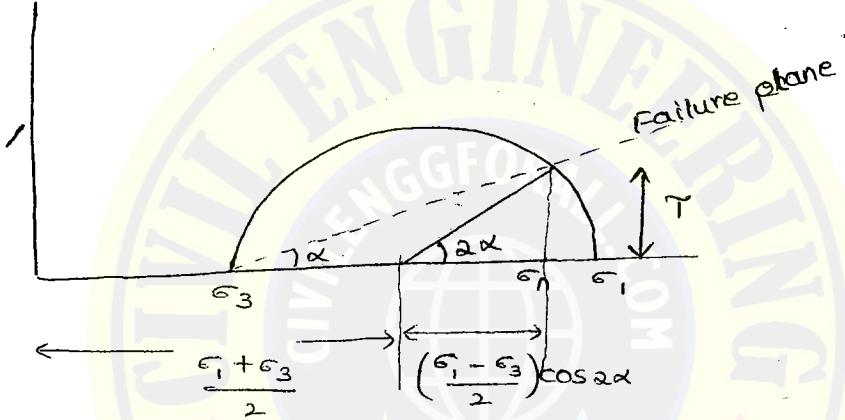
$c'$  = effective cohesion

$\phi'$  = effective angle of shear resistance

$$\sigma_n(\max) = \sigma_1, \quad \alpha = 0 \quad \left. \right\} \quad T_{\min} = 0$$

$$\sigma_n(\min) = \sigma_3, \quad \alpha = 90^\circ$$

$$\sigma_n = \frac{\sigma_1 + \sigma_3}{2}, \quad \alpha = 45^\circ \quad \left. \right\} \quad T_{\max} = \frac{\sigma_d}{2}$$



$$\sigma_n = \frac{\sigma_1 + \sigma_3}{2} + \left( \frac{\sigma_1 - \sigma_3}{2} \right) \cos 2\alpha$$

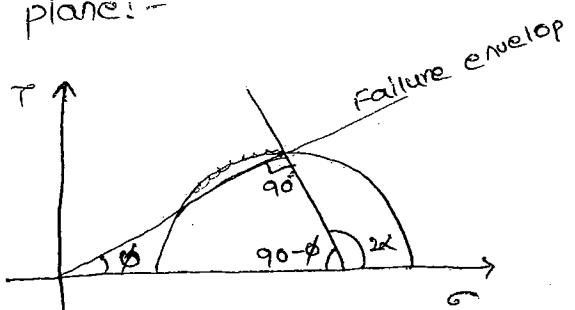
$$T = \frac{\sigma_1 - \sigma_3}{2} \sin 2\alpha$$

$$\sigma_R = \sqrt{T^2 + \sigma_n^2}$$

$$\beta = \tan^{-1} \left( \frac{T}{\sigma_n} \right)$$

$$\beta'_{\max} = \sin^{-1} \left( \frac{\sigma_1 - \sigma_3}{\sigma_1 + \sigma_3} \right)$$

Critical shear plane:-



$$180 = 2\alpha + (90 - \phi)$$

$$2\alpha = 180 - 90 + \phi$$

$$= 90 + \phi$$

$$\alpha_f = 45 + \frac{\phi}{2}$$

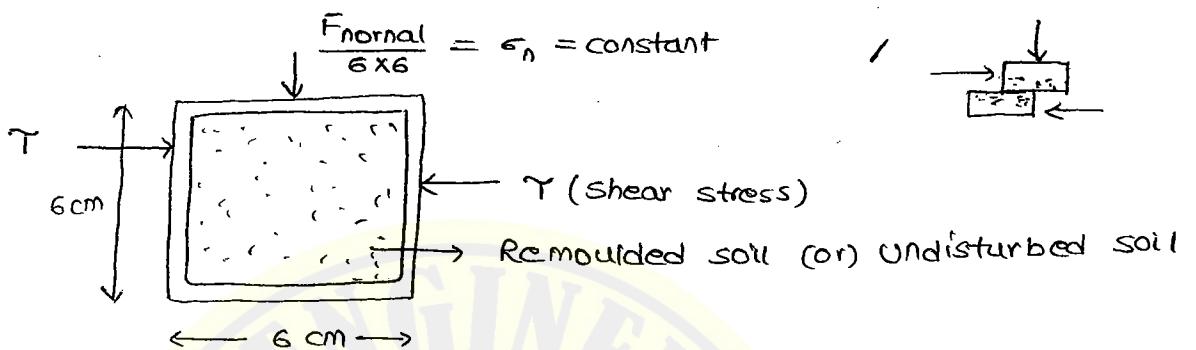
Most dangerous shear plane

Various tests to determine the strength of soil:-

(60)

1. Direct shear test is suitable for  $\phi$ -soils
  2. Tri-axial compression test is suitable for  $c-\phi$  soils
  3. Unconfined compressed strength
  4. Vane shear is suitable for soft clays
- } Lab tests

Direct shear (or) Box shear test:-



Advantages:-

1. It is a quick test
2. cheaper

Disadvantages:-

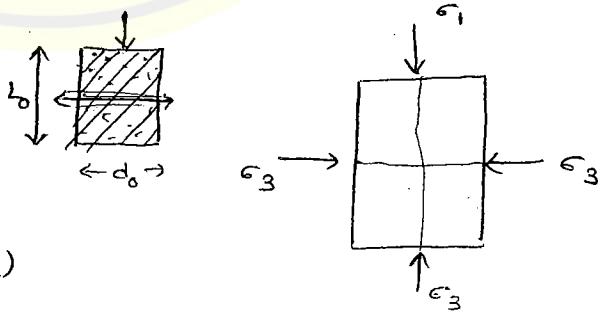
1. It is used only for  $\phi$  soils (frictional soil) not cohesive soil
2. No facility for "pore water pressure" measurement.
3. Area corrected is not used
4. Failure plane is always horizontal

Triaxial compression test:-

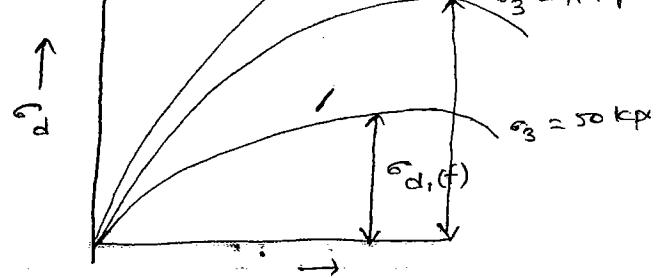
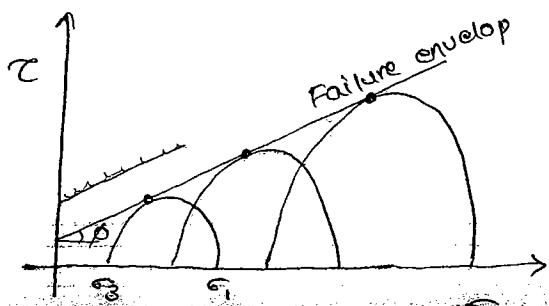
$$\sigma_1 = \sigma_d + \sigma_3$$

$$\sigma_d = \frac{\text{Load}}{\text{corrected Area } (A_c)}$$

$$A_c = \frac{A_o \text{ (original area)}}{1 - \frac{\Delta L}{L_o}}$$



$$\sigma_3 = 150 \text{ kPa}$$



## Shear characteristics of cohesionless soils:-

### Bulging failure:-

1. It occurs in loose sand and silt clay
2. When ' $\Delta L$ ' is large
3. It is a plastic failure

### Brittle failure:-

1. It occurs in dense sand
2. It occurs in silt clay
3. Original area ( $A_0$ )  $\approx$  corrected area ( $A_c$ )
4.  $\Delta L \approx$  small
5. It occurs in stabilize of soils

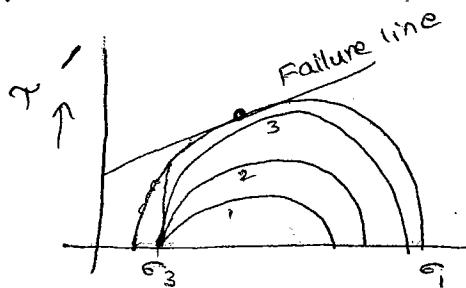
Depending upon drainage conditions, there are three types of tests as explained below:-

	stage-I	stage-II	
$\sigma_T$	U U		Quick test $\rightarrow$ Undrained (value is completely closed)
$\sigma'$	C U		R-test $\rightarrow$ semi / partially drained soil test (value is closed and open)
$\sigma'$	C D		slow test $\rightarrow$ drained (value is open throughout test)

1. UU — stage - I  $\rightarrow$  Not allowed  
stage - II  $\rightarrow$  Not allowed
2. CU — stage - I  $\rightarrow$  value opened  
stage - II  $\rightarrow$  value closed
3. CD — stage - I  $\rightarrow$  value opened  
stage - II  $\rightarrow$  value opened

} pore water pressure 'U' is measurable  
Both test measures effective stress ( $\sigma'$ ) but 'CU' takes less time as compared to 'CD'.

### Plastic equilibrium:-



1-2-3 circles are stable circles

P.g No:- 71

1. Given  $\sigma_T = 295 \text{ kPa}$

$$U = 120 \text{ kPa}$$

$$c' = 12 \text{ kPa}$$

$$\phi' = 30^\circ$$

$$S = c' + \sigma' \tan \phi'$$

$$= c' + (\sigma_T - U) \tan \phi'$$

$$= 12 + (295 - 120) \tan 30^\circ$$

$$= 113.0$$

2. Given  $c = 0$   $\phi = 30^\circ$   $\sigma_d = ?$   $\sigma_3 = 200 \text{ kPa}$

Method-I:  $\sigma_i = \sigma_3 \left( \tan(45^\circ + \phi/2) + 2c \tan(45 + \frac{\phi}{2}) \right)$

$$= 200 \left( \tan(45^\circ + \frac{30}{2}) \right) + 0$$

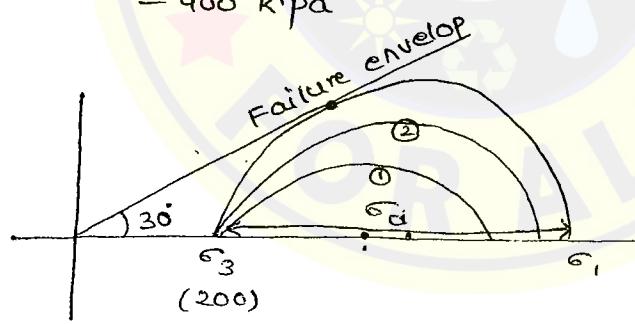
$$\sigma_i = 600 \text{ kPa}$$

$$\sigma_d = \sigma_i - \sigma_3$$

$$= 600 - 200$$

$$= 400 \text{ kPa}$$

Method-II



Remove ① & ② Mohr circ which is not touch and measure the touching circle distance

3. Given  $c = 0$

$$\sigma_n = 200 \text{ kPa}$$

$$\tau_f = 100$$

$$\phi_{\text{Q}} = ?$$

$$T = \sigma_n \tan \phi$$

$$100 = 200 \times \tan \phi$$

$$\phi = 26.56^\circ$$

Pg No:- 64.

### Unconfined compression test :-

1.  $\epsilon_3 = 0$
2. Axial stress =  $\sigma$  (or)  $\sigma_d$
3. U.C.S can be used for purely cohesive soils (clays)
4. U.C.S can also be used for 'c-φ' soils
5. U.C.S cannot be used for sand and gravel
6. Brittle and plastic failure
7.  $\phi = 0$
8.  $c = \frac{q_u}{2}$  (or)  $\frac{\sigma_d}{2}$  (or)  $\frac{U.C.S}{2}$
9. Mohr's circle dia = ( $U.C.S = \sigma_1 = \sigma_d$ )

$$U.C.S = \frac{F}{A_c} = \left[ \frac{\frac{F}{\frac{\pi d^2}{4}}}{1 - \frac{\Delta L}{L}} \right] = \left( \frac{F}{A_o \left( 1 - \frac{\Delta L}{L} \right)} \right)$$

$A_c$  = corrected area

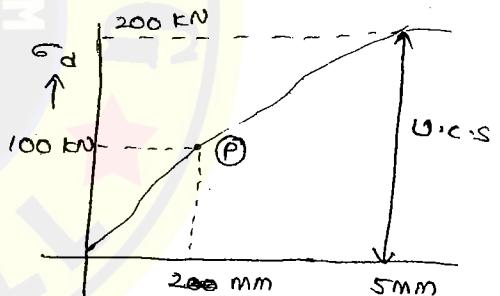
$A_o$  = original area

Ex:- Given  $d = 3.7 \text{ cm}$ , stress ( $P$ ) = ?

$$\sigma = \frac{F}{A_c}$$

$$F = \frac{100}{\left[ \frac{\frac{\pi (3.7)^2}{4}}{1 - \frac{0.2}{7.4}} \right]}$$

$\sigma =$



10. U.C.S can be used for stiff, medium, soft clays.

11. Vane shear can be used for very soft clays.

Material

Quick sand

Liquefaction

Fine sand & silt

"S.P" (poorly graded soil)  
uniform soil

Seepage pressure  
( $P_s$ )

Earthquake, vibration,  
pile driving

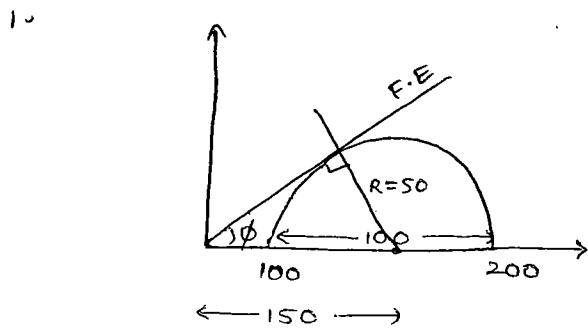
end results

$\sigma' = 0$

$\epsilon' = 0$

$$s = c + \sigma' \tan \phi$$

$$s = c + (\sigma_f - \sigma') \tan \phi$$



$$\frac{100+200}{2} = 150$$

$$\sin \phi = \frac{50}{150}$$

$$\phi = \sin^{-1} \left( \frac{1}{3} \right)$$

4. Given  $\sigma_3 = 100 \text{ kN/m}^2$

$$\sigma_d(f) = 200 \text{ kN/m}^2$$

$$\sigma_i = \sigma_3 + \tan^2 \alpha_f + 2c \tan \alpha_f$$

$$= 100 + \tan^2 \left( 45 + \frac{\phi}{2} \right) + 2c \tan \left( 45 + \frac{\phi}{2} \right)$$

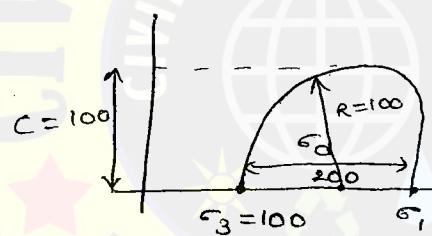
$$300 = 100 + \tan^2 (45) + 2c \tan (45)$$

$$300 = 100 + 2c$$

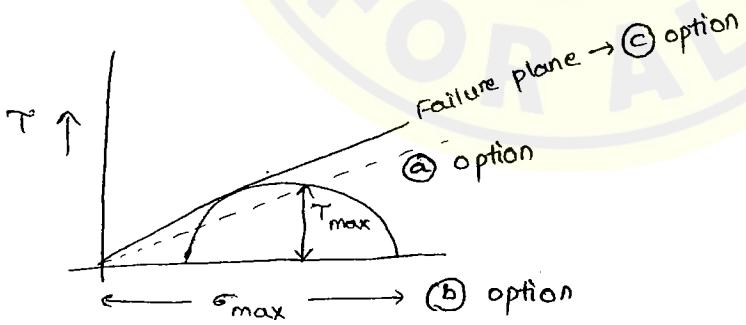
$$c = 100$$

$\therefore$  saturated clay

$$\phi = 0$$



5.



26. Given  $\sigma_i = 200 \text{ kN/m}^2$

$\sigma_3 = 0$  (U.C.S test)

$$= \frac{200 \times 1000}{(1000)^2} \frac{N}{mm^2} \quad \alpha_f = 45^\circ$$

$$\sigma_i = \sigma_3 + \tan^2 \left( 45 + \frac{\phi}{2} \right) + 2c \tan \alpha_f$$

$$0 \cdot 2 \left( \frac{N}{mm^2} \right) = 0 + 2c \tan 45^\circ$$

$$0 \cdot 2 = 2c$$

$$c = 0.1 \text{ N/mm}^2$$

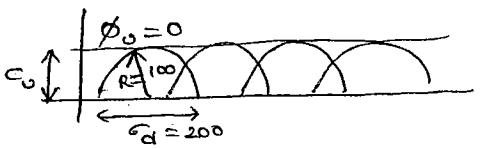
$$\alpha_f = 45 + \phi/2$$

$$45 = 45 + \phi/2$$

$$32. \quad \sigma_d = 200 \quad \sigma_3 = 100$$

$$c_o = \frac{200}{2} = 100$$

$$\therefore c_o = \text{Radius} = 100$$



$$33. \quad \text{Given } \sigma_3 = 50 \text{ kPa}$$

$$\sigma_d = 100 \text{ kPa}$$

$$\phi = ?$$

$$\sigma_1 = \sigma_3 + \sigma_d = 150 \text{ kPa}$$

$$\sigma_1 = \sigma_3 \tan^2\left(45 + \frac{\phi}{2}\right) + 2c \tan\left(45 + \frac{\phi}{2}\right)$$

$$150 = 50 \tan^2\left(45 + \frac{\phi}{2}\right) + 0$$

$\therefore c = 0$  (dry sand)

$$\tan^2\left(45 + \frac{\phi}{2}\right) = 3$$

$$\left(45 + \frac{\phi}{2}\right) = \tan^{-1}(\sqrt{3})$$

$$\frac{\phi}{2} = 60^\circ - 45^\circ$$

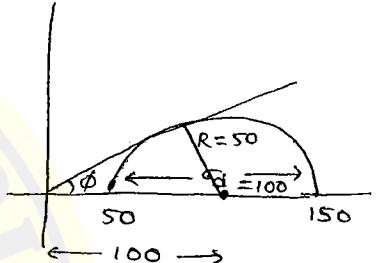
$$\phi = 30^\circ$$

P.g NO:- 64

$$\text{Given } \sigma_3 = 0.2 \text{ M.Pa}$$

$$\phi = 30^\circ$$

$c = 0$  (dry sand)



$$\sin \phi = \frac{50}{100}$$

$$\phi = \sin^{-1}\left(\frac{1}{2}\right)$$

$$\phi = 30^\circ$$

$$\sigma_1 = \sigma_3 \tan^2\left(45 + \frac{\phi}{2}\right) + 2c \tan \alpha_f$$

$$\sigma_1 = 0.2 \tan^2\left(45 + \frac{30}{2}\right) + 0$$

$$= 0.2 \tan^2(60)$$

$$= 0.2 \times 3$$

$$\sigma_1 = 0.6 \text{ M.Pa}$$

$$2. \quad q_u = 2c_o \quad (\text{or}) \quad \sigma_d = 2c_o \quad (\text{or}) \quad \text{U.C.S} = 2c_o$$

$$c_o' = \frac{q_u}{2}$$

$$= 0.5 q_u$$

$$3. \quad \text{Given } \sigma_1 = 50 \text{ kPa} \quad \phi = 30^\circ \quad c = 0$$

$$\sigma_1 = \sigma_3 \tan^2\left(45 + \frac{30}{2}\right) + 0$$

$$50 = \sigma_3 \tan^2(60)$$

$$c_o = \frac{50}{16.97} = 3 \text{ kPa}$$

## UNIT - 14

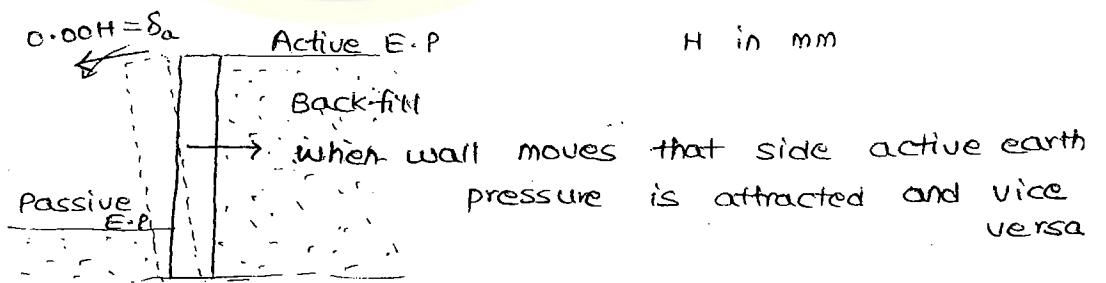
### EARTH PRESSURE

Retaining wall can be classified into many types:-

1. Based on material
  - a. R.C.C
  - b. Masonry
  - c. sheet pile (metal)
2. Based on type
  - a. Gravity Retaining wall
  - b. cantilever retaining wall
  - c. counter-fort retaining wall
3. Based on movement of the wall w.r.t Backfill
  - a. Earth pressure at rest
  - b. Earth pressure is active
  - c. Earth pressure is passive

Only for sheet piles:-

1. When wall moves away from Backfill is called Active Earth pressure.
2. When wall moves towards Backfill is called passive earth pressure
3. No wall movement is called pressure at rest



Coefficient of Earth pressure ( $K$ ):-

It is the ratio of horizontal stress ( $\sigma_h$ ) to vertical stress ( $\sigma_v$ ).

$$K = \frac{\sigma_h}{\sigma_v} = \frac{\sigma_{lateral}}{\sigma_{vertical}}$$

Earth pressure at rest:-

$$K_0 = \frac{\sigma_h}{\sigma_v}$$

$$\sigma_h = K_0 \cdot \sigma_v$$

$$\sigma_h = K_0 (\gamma z)$$

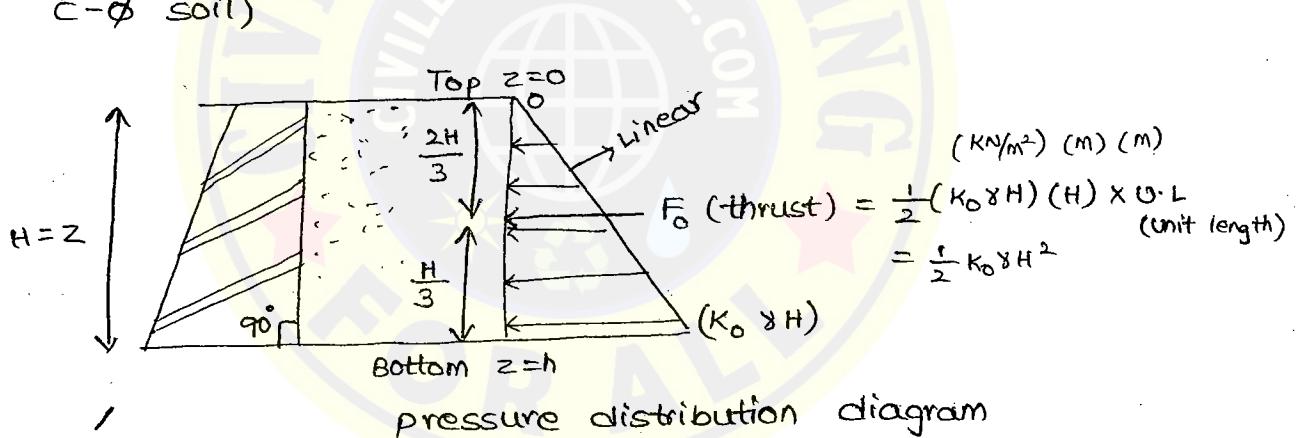
$$P_o = K_0 (\gamma z)$$

$$K_0 = \frac{\mu}{1-\mu}$$

$$K_0 = (1 - \sin\phi) \text{ for cohesionless soil}$$

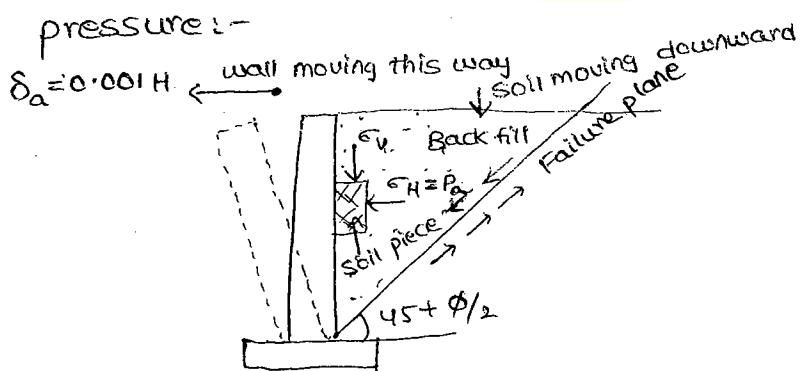
$K_0$  = coefficient of earth pressure at rest

- cohesive soil is not suitable for backfill material
- cohesive soil depends on kaolinite, Montmorillonite.
- cohesive soil having a swelling, shrinking, and misalignment properties.
- cohesionless less soil is suitable for back fill ( $\phi$  soil and  $c-\phi$  soil)



pressure distribution diagram

Active pressure:-



$H$  in mm

$$\sigma_i = \sigma_v = \gamma z$$

$$\sigma_h = \sigma_3 = P_a \text{ (active earth pressure)}$$

1. It was proposed by Rankine.
2. Retaining wall moving away from the backfill.
3. Soil yields to be stretching (or) tension

## Assumptions of Active pressure:-

1. Soil is homogeneous, semi-infinite, dry and cohesionless.
2. Retaining wall back is smooth and vertical.
3. plastic equilibrium condition.

$$\sigma_h < \sigma_v \text{ (active pressure)}$$

$$\sigma_h > \sigma_v \text{ (passive pressure)}$$

Rankine's lateral pressure for dry cohesion less soils:

$$\sigma_i = \sigma_3 \tan^2 \alpha_f + 2c \tan \alpha_f$$

$$\therefore c = 0$$

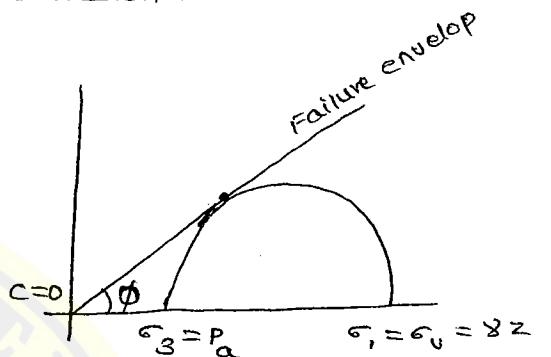
$$\sigma_i = \sigma_3 \tan^2 \alpha_f$$

$$\sigma_v = P_a \tan^2 \alpha_f$$

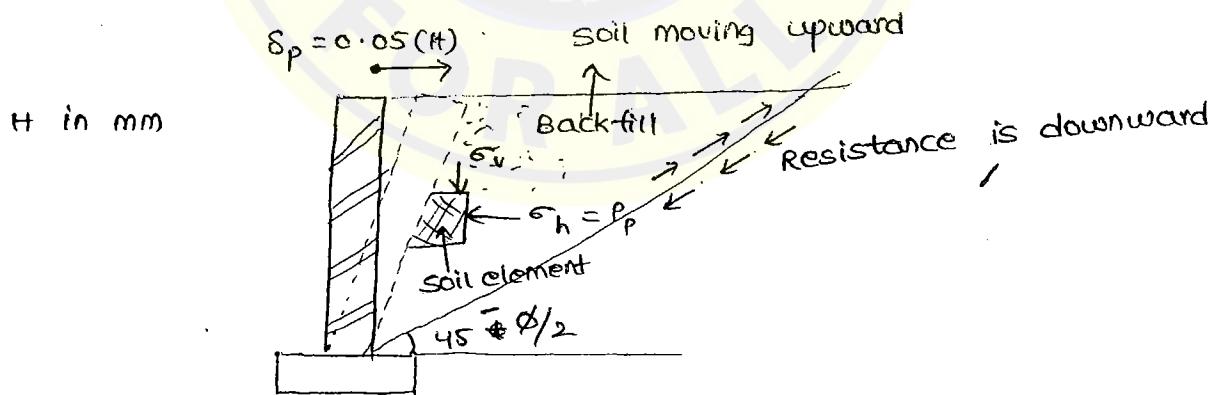
$$P_a = \left( \frac{1}{\tan^2(45 + \frac{\phi}{2})} \right) \sigma_v$$

$$P_a = K_a \cdot \sigma_v$$

$$\boxed{P_a = K_a \cdot (8z)}$$



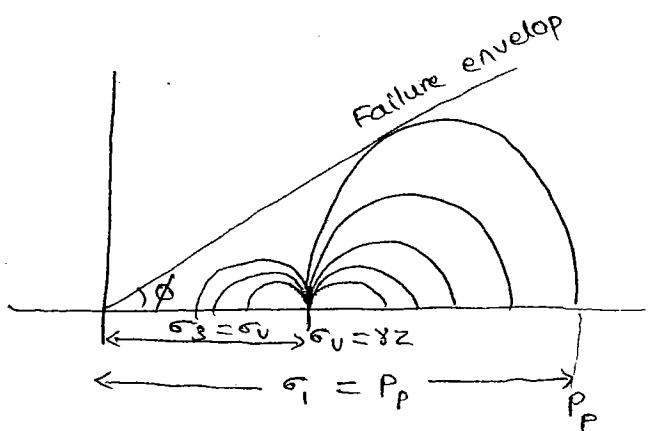
## Passive pressure ( $P_p$ ):-



$$\sigma_i = \sigma_3 \tan^2 (45 + \frac{\phi}{2}) + 0$$

$$P_p = (\gamma z) \tan^2 (45 + \frac{\phi}{2})$$

$$\boxed{P_p = K_p (8z)}$$



Relation between  $k_p$  and  $k_a$  :-

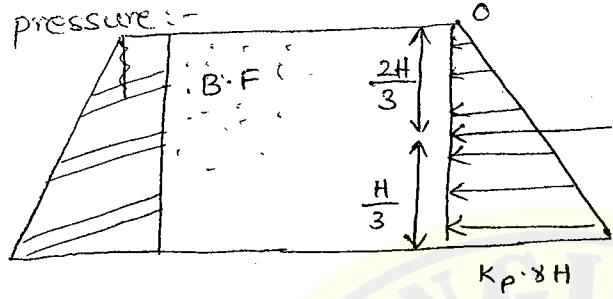
$$k_p = \frac{1}{k_a}$$

$$k_p \cdot k_a = 1$$

$$\text{For } \phi = 30^\circ, k_a = \frac{1}{3}$$

$$k_p = 3$$

Passive pressure :-

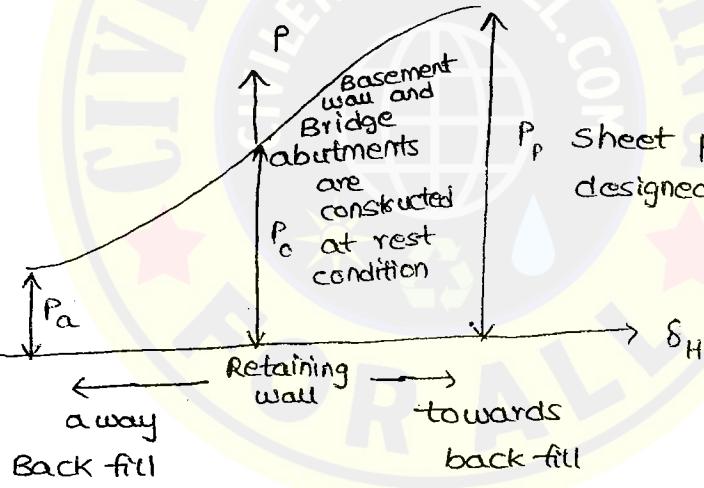


$$F_p = \frac{1}{2} (k_p \gamma H) \cdot (H) (1)$$

$$= \frac{1}{2} k_p \gamma H^2$$

Comparison of  $k_p$  and  $k_a$  :-

Most of the retaining walls are designed at active condition



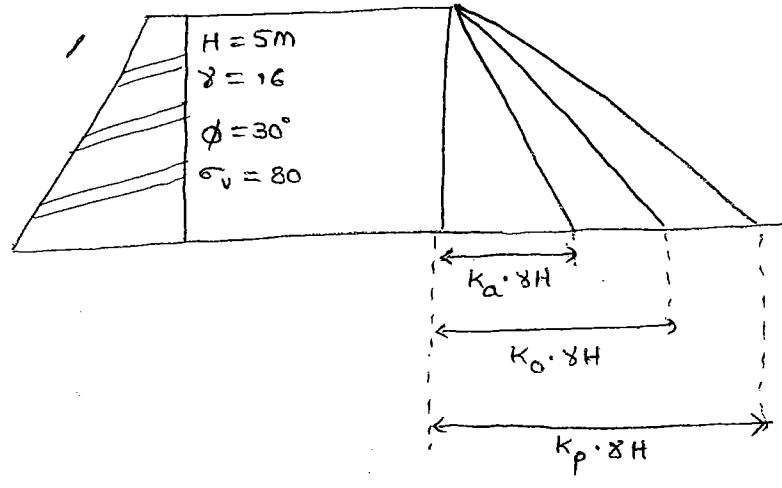
Sheet piles are designed for passive condition

Ex:- Given  $k_a = \frac{1}{3}$ ,  $k_o = 0.5$ ,  $k_p = 3$

$$\downarrow P_a = k_a \gamma z$$

$$P_p = k_p \gamma z$$

$$P_o = k_o \gamma z$$



$$\frac{P_p}{P_a} = ?$$

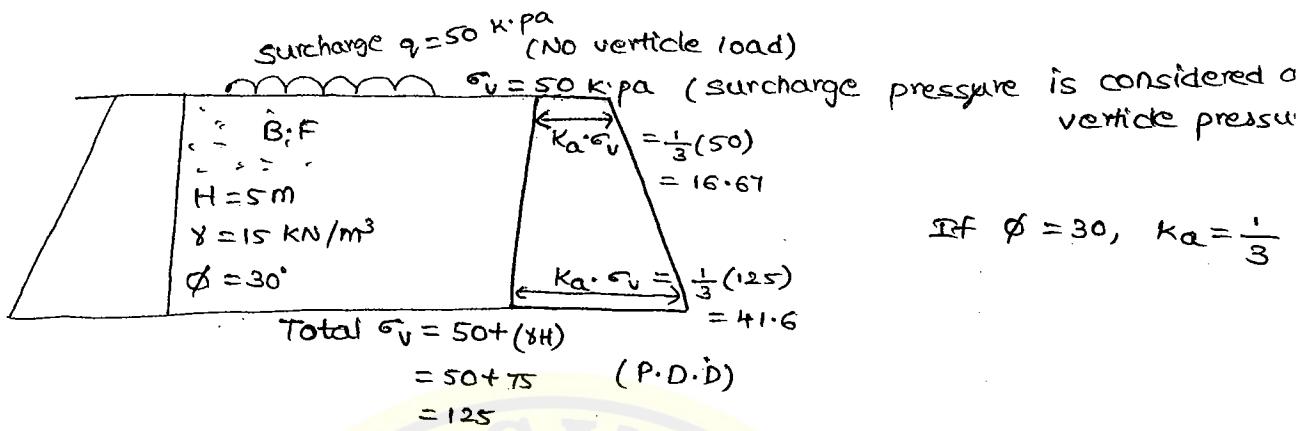
$$\frac{P_o}{P_a} = ?$$

$$\frac{P_p}{P_o} = ?$$

Note:-

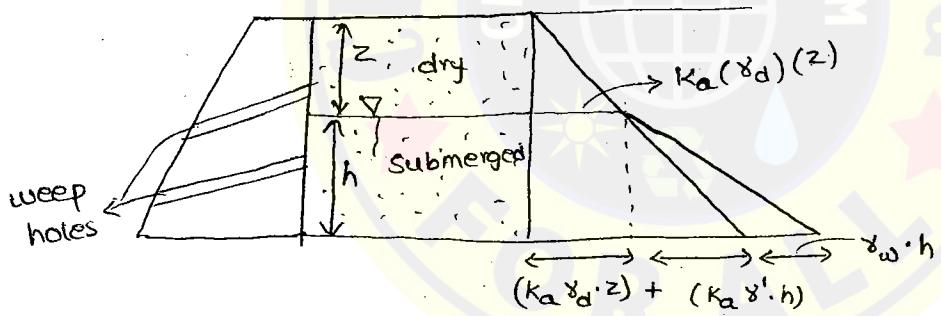
- Any soil which is having a lesser frictional angle ( $\phi$ ),  $K_a$  will be less
- Higher frictional angle is recommended for construction.

Ex:-

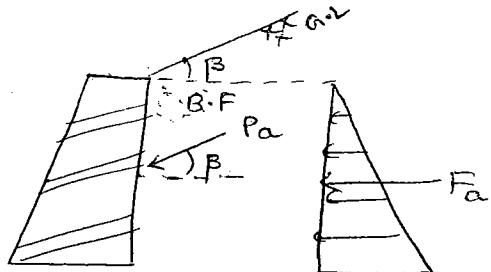


Due to (soil in Back fill + surcharge) the pressure distribution diagram will be "Trapezium" <sup>(P.D.D)</sup>

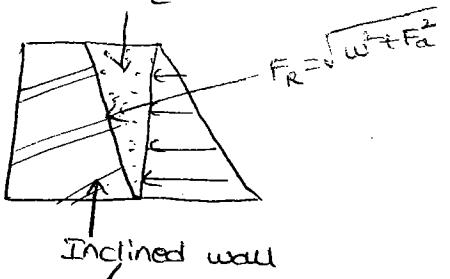
Variation of Lateral pressure:-



Rankine's earth pressure when ground is inclined (at surcharge angle) :-



$$(\text{wt. of soil}) w_s = \left[ \frac{1}{2} \cos(\beta) (H) (1) \right] \gamma_d$$



$$K_a = \cos \beta \left[ \frac{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \phi}}{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \phi}} \right]$$

$$K_p = \cos \beta \left[ \frac{\cos \beta + \sqrt{\cos^2 \beta - \cos^2 \phi}}{\cos \beta - \sqrt{\cos^2 \beta - \cos^2 \phi}} \right]$$

## Earth pressure in C-φ soil :-

1. Active pressure ( $P_a$ ) :-

$$\sigma_1 = \epsilon_3 \tan^2(45 + \phi/2) + 2c \tan(45 + \phi/2)$$

$$\sigma_1 = \gamma z, \quad \epsilon_3 = P_a$$

$$\gamma z - 2c \tan(45 + \phi/2) = P_a \tan^2(45 + \phi/2)$$

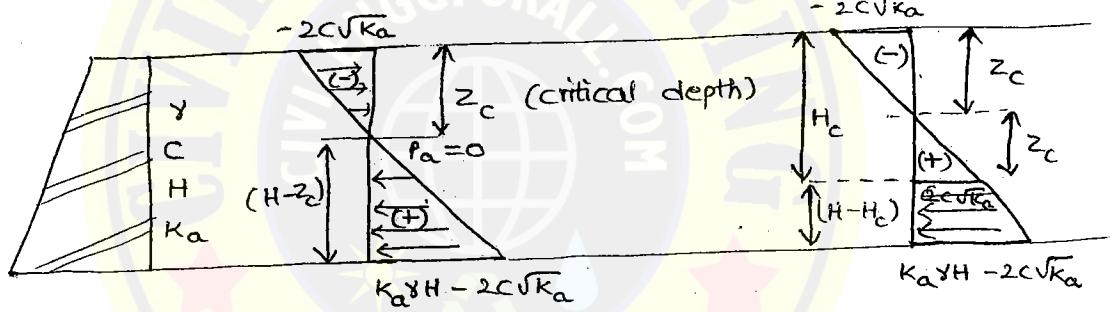
Divide both sides by  $\tan^2(45 + \phi/2)$

$$\frac{\gamma z}{\tan^2(45 + \phi/2)} - \frac{2c \tan(45 + \phi/2)}{\tan^2(45 + \phi/2)} = \frac{P_a \tan^2(45 + \phi/2)}{\tan^2(45 + \phi/2)}$$

$$K_a (\gamma z) - 2c \sqrt{K_a} = P_a$$

$$\therefore P_a = K_a (\gamma z) - 2c \sqrt{K_a}$$

when  $z > z_c$



$$P_a = K_a (\gamma z_c) - 2c \sqrt{K_a}$$

$$\therefore P_a = 0$$

$$K_a (\gamma z_c) = 2c \sqrt{K_a}$$

$$z_c = \frac{2c \sqrt{K_a}}{K_a \cdot \gamma}$$

$$= \frac{2c}{\gamma} \left( \frac{\sqrt{K_a}}{K_a} \right)$$

$$\therefore \frac{\sqrt{K_a}}{\sqrt{K_a} \cdot \sqrt{K_a}} = \frac{\sqrt{K_a}}{K_a}$$

$$z_c = \frac{2c}{\gamma \sqrt{K_a}} = \text{depth of tensile cracks.}$$

$H_c$  = Height of the unsupported excavation.

$$H_d = 2(z_c) = \text{depth of unsupported excavation}$$

$\therefore$  No pressure is acting on ' $H_c$ ' area. pressure is acting below the ' $H_c$ ' area ( $H - H_c$ ).

$$\text{Case 6: } \begin{array}{c} (H - H_c) \\ \hline K_a \gamma H - 2C\sqrt{K_a} \end{array}$$

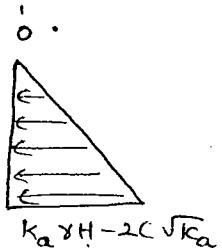
→ Area of the trapezium,  $F_a = \frac{h}{2}(a+b)$

$$= \frac{H-H_c}{2} [2C\sqrt{K_a} + (K_a \gamma H - 2C\sqrt{K_a})]$$

This case is economical and less force because shorter area.

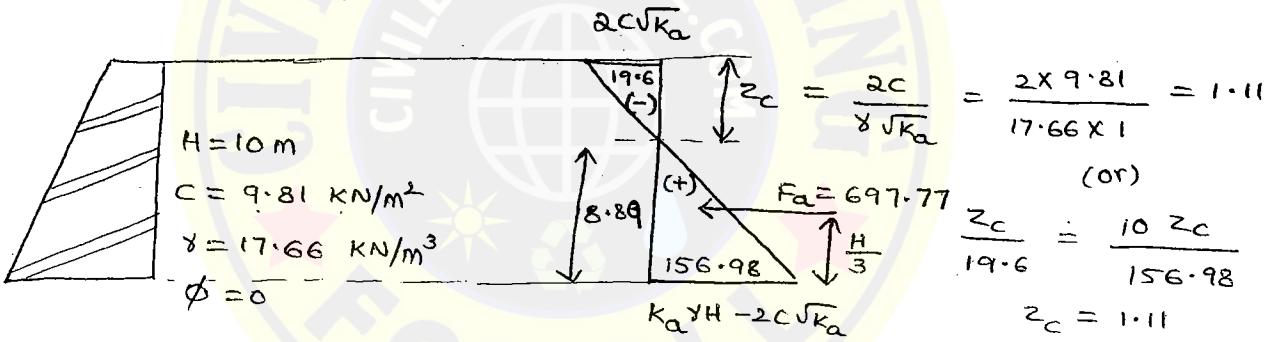
$$\rightarrow F_a = \frac{1}{2} [(K_a \gamma H - 2C\sqrt{K_a})(H - z_c)]$$

This is the worst case and highest  $(H - z_c)$  force (area is large)



$$\begin{array}{c} H \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} + \begin{array}{c} -2C\sqrt{K_a} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \\ \text{---} \end{array} = F_a = \left[ \frac{1}{2} (K_a \gamma H)(H) \right] + [-2C\sqrt{K_a} \times H] \\ = \frac{1}{2} K_a \gamma H^2 - 2C H \sqrt{K_a}$$

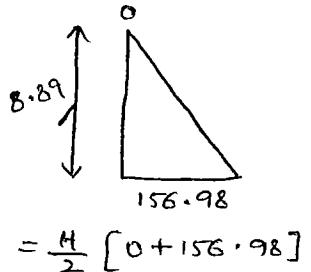
Ex:-



If  $\phi = 0^\circ$  then  $K_a = 1$

Neglect '-ve' zone

$$\begin{aligned} F_a &= \frac{1}{2} (156.98) (8.89) (\text{unit length}) \\ &= 697.77 \text{ kN} \end{aligned}$$

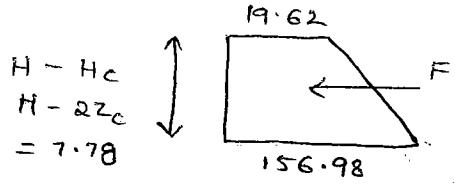


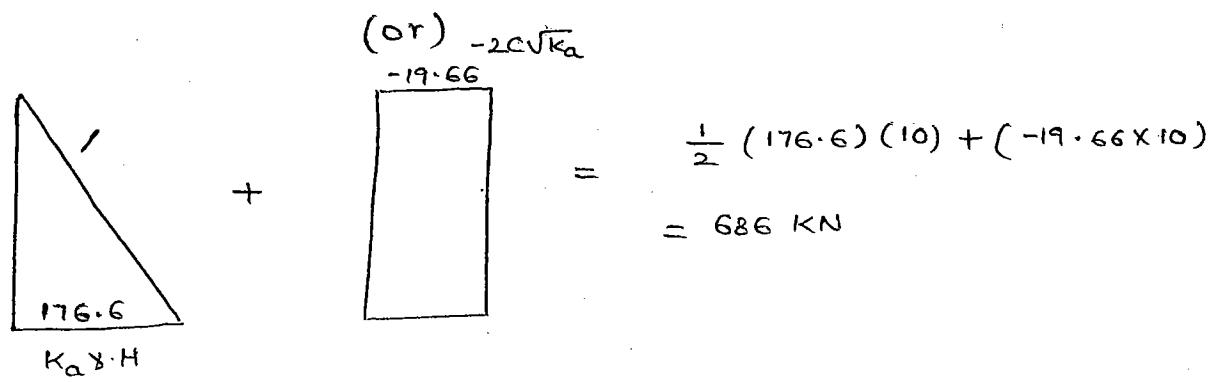
Now consider whole diagram

$$\begin{aligned} F_{\text{whole diagram}} &= 697.77 - \left( \frac{1}{2} \times 19.6 \times 1.11 \right) \\ &= 686 \text{ kN} \end{aligned}$$

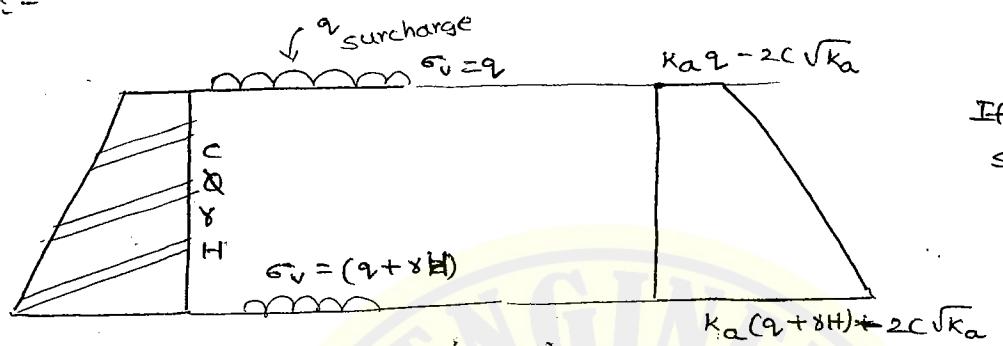
(or)

$$\begin{aligned} F_{\text{whole (or) total}} &= \frac{7.78}{2} (19.62 + 156.98) \\ &= 686 \text{ kN} \end{aligned}$$





Note:-

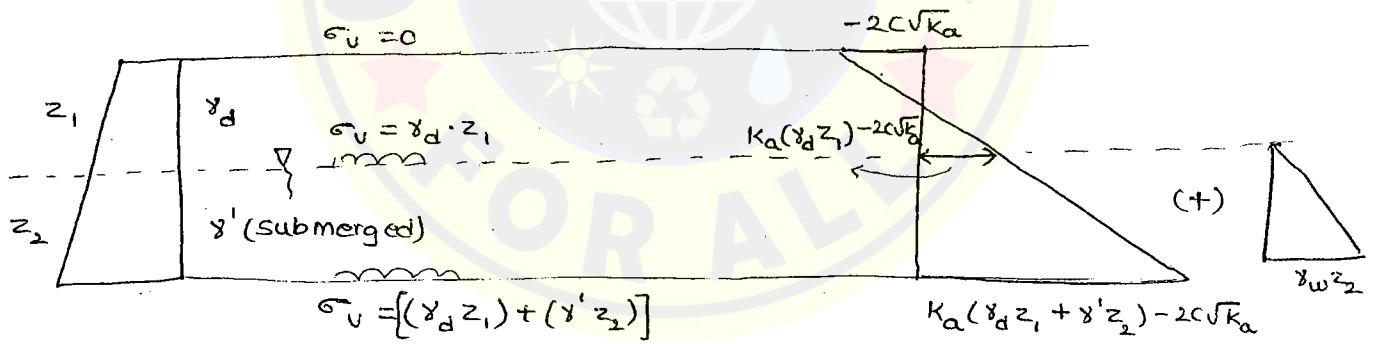


If there is a surcharge.

$$\begin{aligned} P_a(\text{top}) &= K_a(\gamma z) - 2C\sqrt{k_a} \\ &= K_a(q) - 2C\sqrt{k_a} \end{aligned}$$

$$P_a(\text{bottom}) = K_a(q + \gamma H) - 2C\sqrt{k_a}$$

2.



$$P_a = K_a(\sigma_v) - 2C\sqrt{k_a} = -2C\sqrt{k_a} \rightarrow \text{top}$$

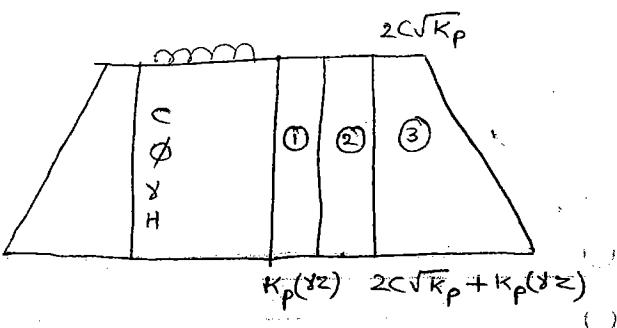
$$= K_a(\gamma_d z_1) - 2C\sqrt{k_a} \rightarrow \text{middle}$$

$$= K_a(\gamma_d z_1 + \gamma' z_2) - 2C\sqrt{k_a} \rightarrow \text{bottom}$$

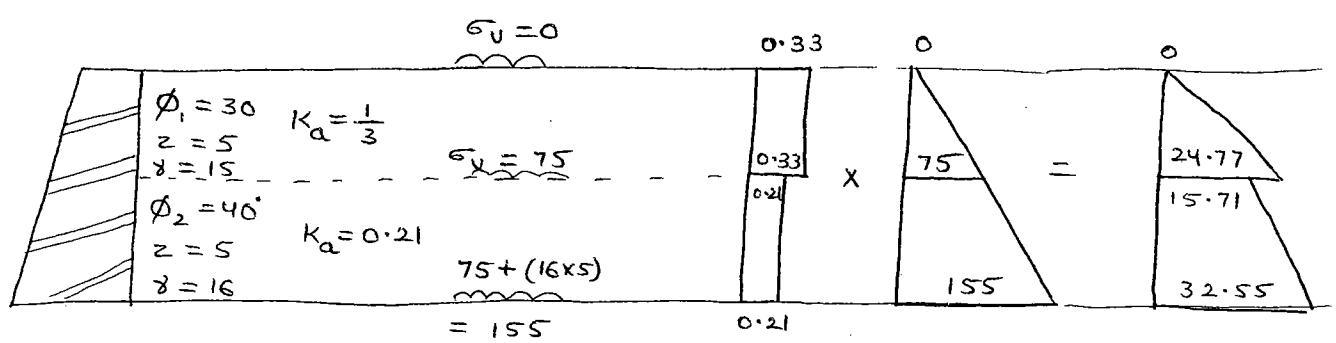
//

Q. Passive pressure ( $P_p$ ):- ( $C-\phi$  soils)

$$P_p = K_p(\gamma z) + 2C\sqrt{k_p}$$

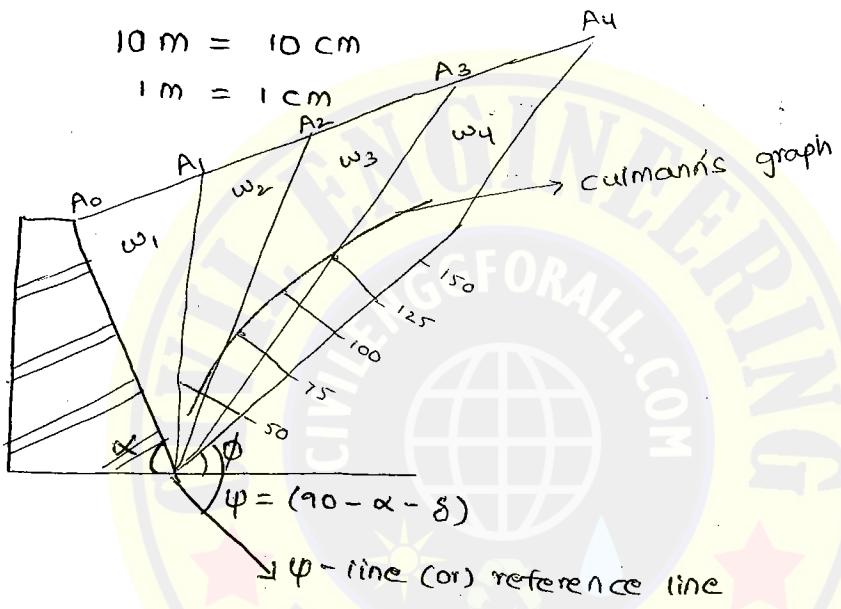


Ex :-



Graphical solution:-

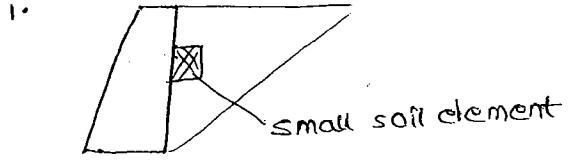
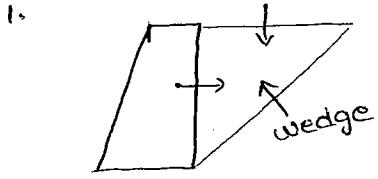
## 1. Culmann's method:-



Difference between Coulumb's theory and Rankine's theory

Coulumb's

Rankine's



1. Rough walls ( $\gamma \neq 0$ )
2. Masonry
3.  $K_a \Rightarrow \phi, \beta, \gamma, \alpha$

1. Smooth walls ( $\gamma = 0$ )
2. R.C.C.
3.  $K_a \rightarrow \phi^\circ, \beta^\circ$

P.g NO:- 69

Q. 1. Given  $C = 30 \text{ kN/m}^2$   
 $\gamma = 20 \text{ kN/m}^3$

$$H_c = 2 z_c$$

$$= \frac{4C}{\gamma \sqrt{k_a}}$$

$$= \frac{4 \times 30}{20 \times 1}$$

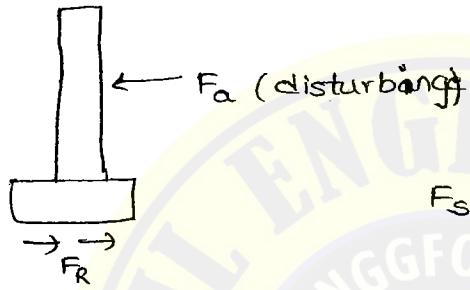
$$H_c = 6 \text{ m}$$

For saturated clay

$$\phi = 0$$

$$k_a = 1$$

Q.

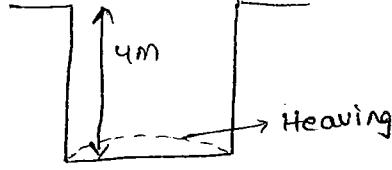


$$\begin{aligned} \text{Sliding} &= \frac{F_R}{F_D} \\ &= \frac{\gamma V \cdot \tan \delta}{F_D} \end{aligned}$$

$\delta$  = angle of wall friction

Q.

$$\frac{k_p}{k_a} = \frac{\frac{1+\sin\phi}{1-\sin\phi}}{\frac{1-\sin\theta}{1+\sin\theta}} = \frac{3}{\frac{1}{3}} = 3 \times 3 = 9$$



$$\gamma = 22$$

$\phi = 0^\circ$  for cohesion

$$k_a = 1$$

$$H_c = \frac{4C}{\gamma \sqrt{k_a}}$$

$$4 = \frac{4C}{22 \times 1}$$

$$C = 22 \text{ kN/m}^2$$

Q. 2. Retaining wall is a R.C.C. structure. It can be determined based on Rankine's theory.

$$\begin{aligned}
 16. \quad z_c &= \frac{2c}{8\sqrt{k_a}} \\
 &= \frac{2 \times 14}{16.5 \times 1.373} \\
 &= 2.33
 \end{aligned}$$

$$\sqrt{k_a} = \sqrt{\frac{1-\sin\phi}{1+\sin\phi}} = \sqrt{\frac{1-\sin 18^\circ}{1+\sin 18^\circ}} = 1.373$$

$$\begin{aligned}
 25. \quad q &= 120 \text{ kN/m}^2 \\
 \phi &= 30^\circ \\
 k_a &= \frac{1}{3} \\
 F &= k_a \cdot q \\
 &= \frac{1}{3} (120) = 40 \text{ kN/m}^2
 \end{aligned}$$

25-12-2019

UNIT - 20FOUNDATIONS IN EXPANSIVE SOILS

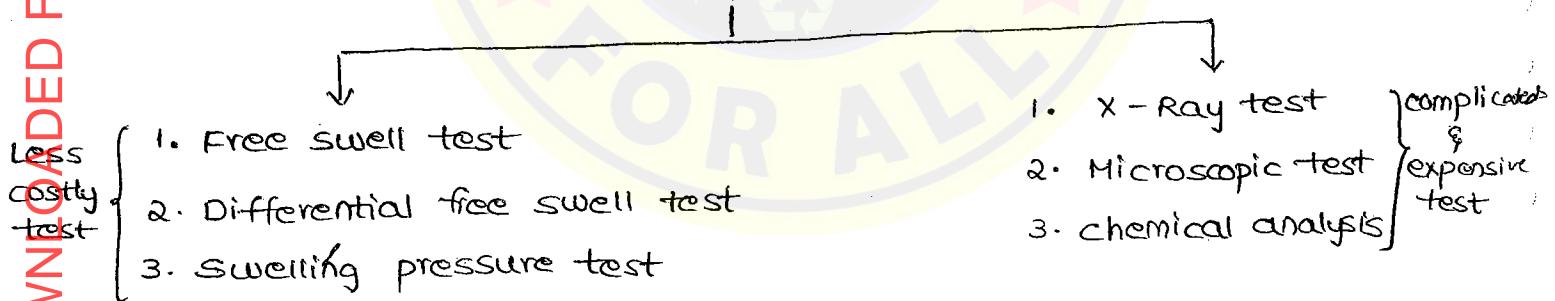
Expansive soils:-

1. Black cotton soils is also called Expansive soils
2. Water is a polar liquid and causes swelling and shrinkage
3. Montmorillonite mineral is present in clay which causes more swelling and shrinkage. Expansive soils are also called cohesive swelling soil.

Identification of expansive soils:-

1. In dry soil cracks are developed. Absorb that cracks and measure the size and depth of the crack.
  - size → inches
  - depth → metres
2. Walk on wet soils, if soil is sticky (highly plastic soils) can be indicated as expansive soils.
3. Observe lightly loaded structure (only ground storey building, roadsides, canal (empty)) if damage is severe soil can be expansive.

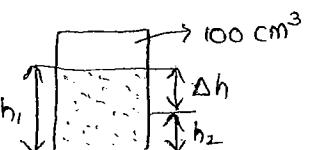
## Tests



Free swell test:-

$$\Delta h = h_2 - h_1$$

$$\text{Free swell} = \frac{\Delta h}{h_1} \times 100 \%$$



Free swell &gt; 50%. damage is caused

- Life
1. Light damage → It is nil
  2. Structural damage
  3. cosmetic (or) architectural damage
- } property damage

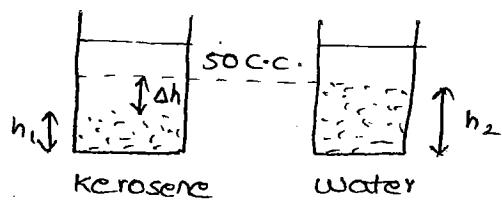
Most of the damage in the expansive soils are cosmetic damage

(cracks etc.)

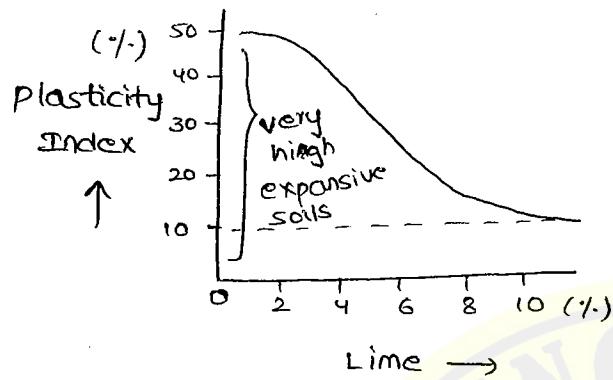
## Differential free swell test :-

$$DFS = \frac{h_2 - h_1}{\Delta h} \times 100$$

$$DFS = \frac{\Delta h}{h_1} \times 100$$

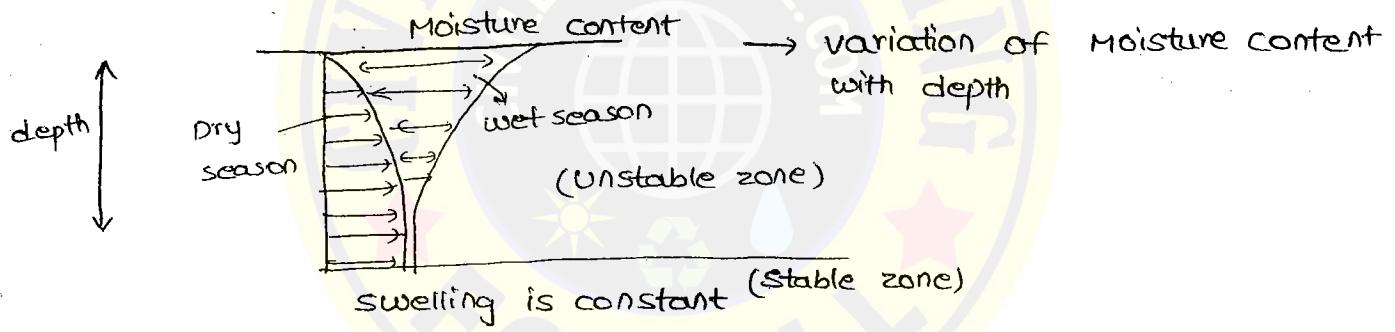


Relationship between swelling potential of soil and plasticity index:-



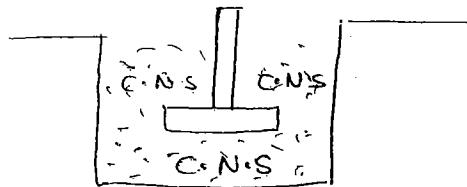
} Low expansiveness when lime is added, then the plasticity index drops down to 10%.

Methods of foundations in expansive soils:- Design



1. Shallow foundations are not recommended in expansive soils
2. Suitable for deep footing and under reamed pile footing. Min best method

3.



cohesive non swelling soil  
Ex:- Moorum

25-12-2014

## UNIT - 19

### SHEET PILES

Sheet pile is one of the "flexible retaining wall". They are made of timber, steel, RCC, prefabricated unit (RCC) etc.

1. sheet piles always designed for lateral force.
2. Timber carrying less load. Durability is less.

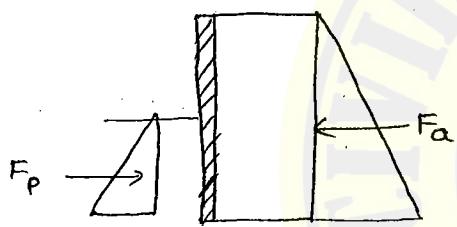
Steel pile : More load, less driving pile.

Timber pile : Less load, temporary structure, durability less

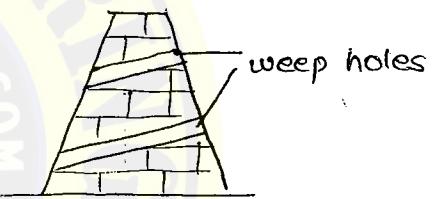
Prefabricated pile : More thickness, more load, life is good.

3. In sheet piles, section is thinner to suitable low bearing capacity soils.

sheet pile



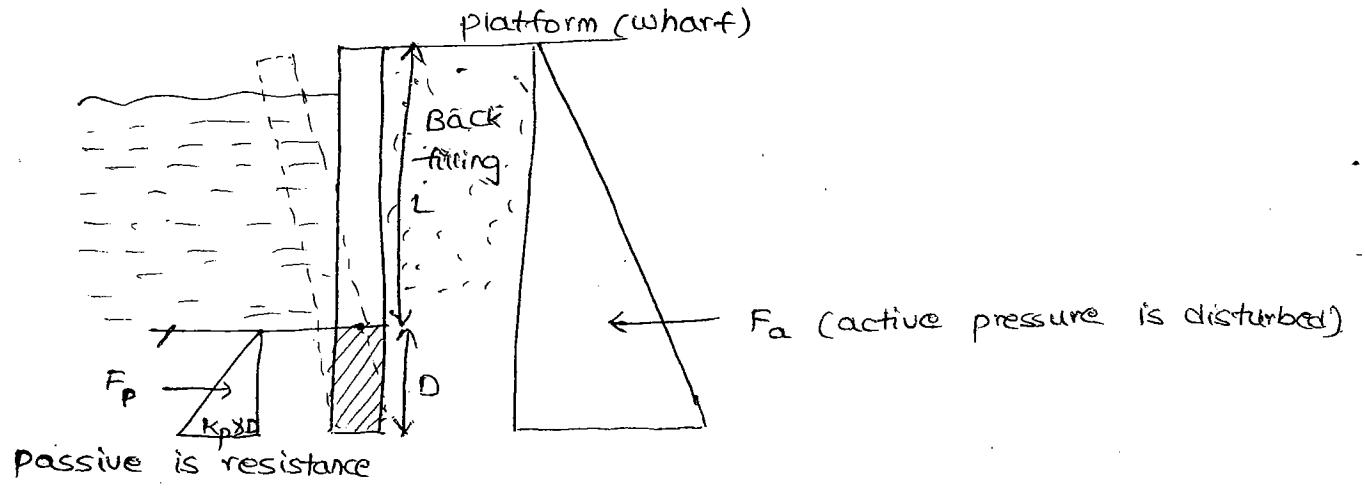
Retaining wall (R.C.C)  
(Masonry)



1. No weep holes in sheet piles
2. Anchored
3. Flexible

1. Bearing capacity increases
2. Rigid
3. Not anchored
4. Weep holes are provided.

Cantilever sheet pile:-



26-12-2014

UNIT - 18

50

SOIL EXPLORATION

Soil exploration is also called soil investigation (or) site investigation.

Exploration means to bring out the hidden things like rock, water table, type of soil, sound rock etc on earth.

Budget for site investigation is to spend maximum 2% of the total project cost

Site investigation is not done (or) adequate causes

1. Failure of the structure
2. Improper functioning of the structure
3. A Unable to decide alteration or addition.

Seismic refractive method is the one of the method which is non destructive method.

Note:-

1. When bore holes are in closer spacing, no. of bore holes are increasing, time is increasing cost is increasing
2. Soil → Homogeneous, uniform, spacing is more, no. of Bore holes is less
3. Soil → Erratic soil, non uniform soil, spacing is less, no. of Bore holes is high.

Methods of exploration:-

1. Test pit method:-

Disadvantages:-

1. Soil is disturbed
2. Uneconomical for deeper depth

Advantages:-

1. Economical
2. Large quantity of soil is available.

## 2. Boring method :-

Making a small hole in soil is called Boring. There are two types of borings.

### Auger Boring :-

1. Auger Boring gives highly disturbed soil.
2. It is economical for shallow depth.
3. It is a preliminary site investigation with a rapid time (quick).
4. There are two types of Auger Boring. They are

Hand Augers → suitable for shallow depths like Roads

power Augers → deeper depth.

### Wash boring :-

#### Advantages :-

1. Information for deeper strata

#### Disadvantages :-

1. Destructive test
2. Can't be used if Rock present
3. Disturbed soil.

### percussion drilling or cable tool method :-

#### Advantages :-

1. Suitable for all soils
2. Brings soil sample

#### Disadvantages :-

1. Highly disturbed
2. Progress is slow
3. Durability of Rock (or) "Rock durability test"
4. Destructive test.

### Factors affecting the sample disturbance:-

1. split spoon sampler (SSS) - disturbed
  2. Shelby tubes
  3. piston sampler
  4. thin wall sampler
- } undisturbed

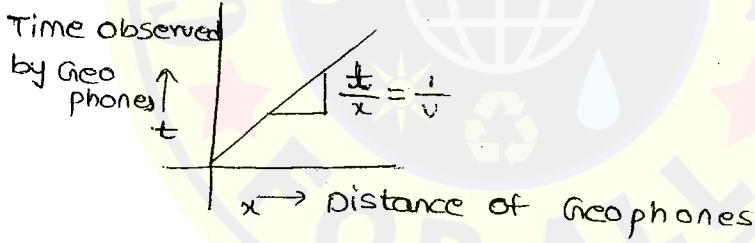
- Static loads are good for disturbed sample.
- Dynamic loads are good for undisturbed sample.

Pressure meter test:-

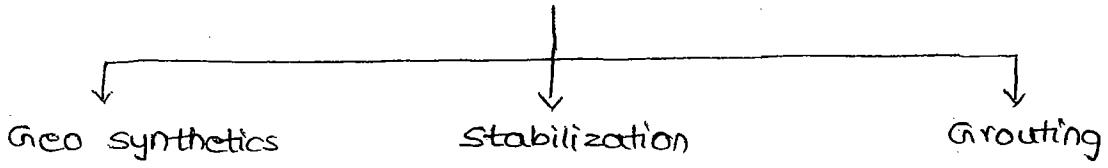
1. It is a field test
2. Deeper soil
3. Radial displacement
4. volume changes

Seismic refraction method:-

1. One of Non disturbed test
2. preliminary
3. No samples are taken out
4. surface or nearby surface zone (Deeper soil cannot be evaluate by this method)
5. suitable for runways, highways
6. Large area in short period of time
7. In seismic refraction method slope gives "inverse of velocity"



## Ground Improvement Engineering



1. Mechanical stabilization:-

By adding one soil + other soil is called Mechanical stabilization. No chemicals are used.

2. Chemical Stabilization:-

Soil + cement + water + compaction + curing. Quantity of cement required approximately, 5% for sand and 15% for clays

Soil + chemical = chemical stabilization.

## Lime stabilization:-

Lime + cohesive soils = Lime stabilization.

1. Binding increases
2. permeability decreases
3. durability increases
4. Erosion decreases
5. Water proofing.

## Ground improvement techniques:-

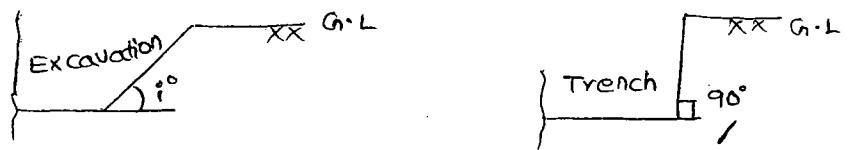
1. Electro osmosis
2. vibroflotation method
3. Terraprobe method
4. Lime piles
5. stone columns
6. Geotextiles

## Geotextiles:-

1. It is a synthetic material (or) artificial material.
2. It is used inside of soil like reinforcement, drainage.
3. It looks black in color.
4. It acts membrane (water proofing)

UNIT - 15STABILITY OF SLOPES

Slopes are Embankment, Earthen dams, canals, Trenches, Levees



Flat

- 1. More land
- 2. Stability is more
- 3. More material

steeper slope

- 1. Less land
- 2. stability is less
- 3. Less material.

Slope failure may takes place due to

- 1. Gravitational force
- 2. Natural disasters
- 3. Rains (seepage)

Toe failure:-

- 1. Toe failure is the common among the three failures

Base failure:-

- 1. It occurs beyond the toe failure.

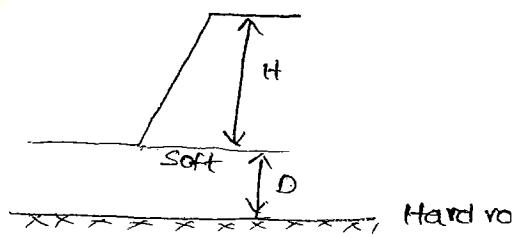
Depth factor ( $D_f$ ) :-

$$D_f = \frac{D + H}{H}$$

For face failure,  $D_f < 1$

For toe failure,  $D_f = 1$

For base failure,  $D_f > 1$



Stability of infinite slopes:

$$\text{Factor of safety, } F = \frac{s}{\tau} = \frac{\text{shear strength}}{\text{shear stress}}$$

Infinite slope in  $C-\phi$  soils:-

$$F = \frac{c + \sigma_n \tan \phi}{\gamma}$$

$$F = \frac{c + \gamma z \cos^2 i \tan \phi}{\gamma z \cos i \sin i}$$

$$I = \frac{c + (\gamma z_i \cos^2 i) \tan \phi}{\gamma z_c \cos i \sin i}$$

$$\frac{\gamma z_c \cos i \sin i}{z_c \gamma} = \frac{c}{z_c \gamma} + \frac{\gamma z_c \cos^2 i}{z_c \gamma}$$

$$\frac{c}{z_c \gamma} = \cos i \sin i - \cos i \tan \phi$$

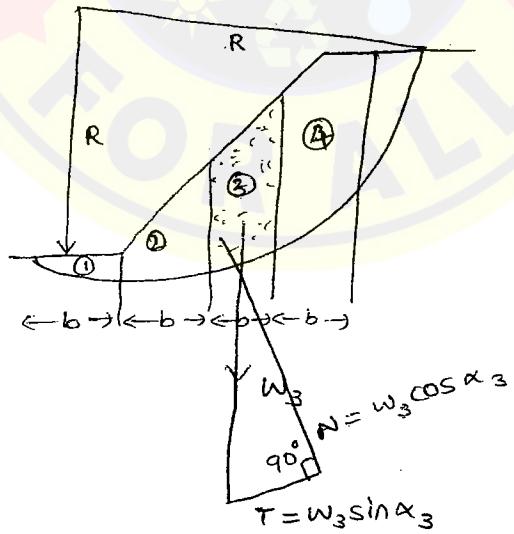
$$\frac{z_i}{z} = \frac{H_c}{H} = F_c$$

$$z_c = (F_c \cdot z)$$

$$\frac{c}{F_c \gamma z} = \cos^2 i (\tan i - \tan \phi) = s_N = \text{stability number.}$$

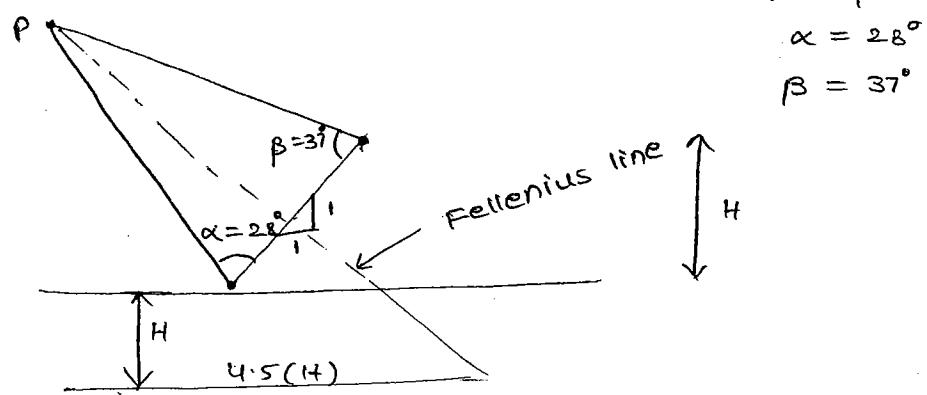
Swedish circle method (or) method of slices:-

- It can be used for  $C-\phi$  soils.



$$F_{c-\phi} = \frac{c(L_{arc} \times i) + (\varepsilon N) \tan \phi}{\varepsilon T}$$

## Fellenius method :-



For 1:1 slope

$$\alpha = 28^\circ$$

$$\beta = 37^\circ$$

Factor of safety :-

$$F_c = \frac{c}{c_m} = \frac{H_c}{H} = \frac{\text{Critical height}}{\text{Actual height of slope}}$$

$$F_\phi = \frac{\tan \phi}{\tan \phi_m} = \frac{\text{friction angle}}{\text{mobilised friction angle}}$$

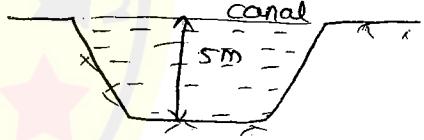
$$\phi_m = \tan^{-1} \left[ \frac{\tan \phi}{F_\phi} \right]$$

P.g No:-79

33. Given  $c = 1.5 \text{ t/m}^2$   $H = 5 \text{ m}$

$$\gamma_{\text{sat}} = 2 \text{ t/m}^3$$

$$s_n = 0.1$$



$$F_c = s_n = \frac{c}{F_c \cdot \gamma' \cdot H}$$

$$F_c = \frac{c}{s_n \gamma' H}$$

$$= \frac{1.5}{0.1 (2-1)(5)}$$

$$F_c = 3$$

34. Method of slices

$$\Sigma T = 500 \text{ kN}$$

$$\Sigma N = 900 \text{ kN}$$

$$\Sigma U = 200 \text{ kN}$$

$$L_{\text{arc}} = 27 \text{ m}$$

$$c = 20 \text{ kN/m}^2$$

$$\phi = 20^\circ$$

$$F_{c-\phi} = \frac{c (L_{\text{arc}} \times 1) + \Sigma (N-U) \tan \phi}{\Sigma T}$$

$$= \frac{20 (27 \times 1) + (900 - 200) \tan 20^\circ}{500}$$

$$= 1.5895$$

35. Given  $C = 2T/m^2$   $\gamma = 2T/m^3$ ,  $F = 2$   $s_n = 0.1$

$$s_n = \frac{C}{F_c \cdot \gamma \cdot H}$$

$$0.1 = \frac{2}{2 \times 2 \times H}$$

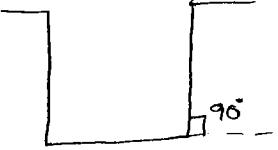
$$H = \frac{2}{0.4} = 5m$$

36. Given  $C = 2.6 t/m^2$

$$i = 90^\circ$$

$$s_n = 0.261$$

$$\gamma = 2 t/m^3$$



$$H = \frac{C}{s_n \times \gamma \times F}$$

$$= \frac{2.6}{0.261 \times 2 \times (1)}$$

$$= 5.04 m$$

If  $F \cdot s$  is not given then take  
safe  $F \cdot s = 1$

Additional questions:-

i. Given  $H = 7m$

$$\gamma = 16 \text{ kN/m}^3$$

$$C = 25 \text{ kN/m}^2$$

$$i = 30^\circ$$

$$s_n = 0.178$$

$$F_c = \frac{C}{s_n \cdot \gamma \cdot H}$$

$$= \frac{25}{0.178 \times 16 \times 7}$$

$$= 1.25$$

UNIT - 16BEARING CAPACITY

**Shallow Foundations:-**

A foundation is considered as shallow depth is called shallow foundation. If the depth is equal to or less than the width it is shallow.

Ex:- Spread footing, continuous footing, Raft foundation etc.

**Deep Foundation:-**

Load is transmitted at considerable depth below G.L.

Ex:- pile, pier, caisson etc.

**Net pressure ( $q_n$ ):-**

Gross pressure - original overburden pressure

$$q_n = q - \gamma D$$

D = Depth of foundation

**Ultimate bearing capacity:-( $q_u$ )**

The minimum gross pressure at the base of the foundation at which soil fails in shear.

**Net ultimate bearing capacity ( $q_{nu}$ ):-**

$$q_{nu} = q_u - \gamma D$$

**Net safe bearing capacity ( $q_{ns}$ ):-**

$$q_{ns} = \frac{q_{nu}}{F}$$

F = Factor of safety, = 3

**Gross safe bearing Capacity (or) Safe bearing capacity ( $q_s$ ):-**

$$q_s = q_{ns} + \gamma D$$

**Rankine's Analysis:-**

$$P_{min} = \frac{q}{\gamma} \left[ \frac{1 - \sin \phi}{1 + \sin \phi} \right]^2$$

q = load intensity at the base

Terzaghi's general bearing capacity equation for continuous footing :-

$$q_{ult} = C N_c + q D_f N_q + 0.5 \gamma B N_y \xrightarrow{\text{valid for } c-\phi, \text{G.S.F., strip}} C - \phi, \uparrow$$

$N_c, N_q, N_y$  are bearing capacity factors for general shear failure. It depends upon angle of friction  $\phi$

Note:-

As the angle of internal friction increases bearing capacity factors also increases.

$$q_{net} = [q_{ult} - q D_f]$$

$$q_{net} = C N_c + q(N_q - 1) + \frac{1}{2} B N_y \cdot \gamma$$

$$q_{ult}(\text{safe}) \text{ (or)} q_{ult}(\text{allow}) = \frac{1}{F} [C N_c + q(N_q - 1) + \frac{1}{2} \gamma B N_y]$$

$$q_{ult}(\text{gross}) = 1 \cdot C N_c + 1 \cdot q N_q + 1 \cdot \frac{1}{2} \gamma B N_y$$

$$S_c, S_q, S_y = 1$$

$S_c, S_q, S_y$  are shape factors.

Shape factors	strip	square	circular	rectangular
$S_c$	1	1.3	1.3	$1 + 0.3 \frac{B}{L}$
$S_q$	1	1.0	1.0	1.0
$S_y$	1	0.8	0.6	$1 - 0.2 \frac{B}{L}$

Circular footing:-

$$q_{ult}(\text{gross}) = 1.3 C N_c + 1.3 q N_q + 0.6 \times \frac{1}{2} (D) \gamma - N_y$$

$$S_c = 1.3, \quad S_q = 1, \quad S_y = 0.6$$

Square footing:-

$$q_{ult}(\text{gross}) = 1.3 C N_c + 1.3 q N_q + 0.8 \times \frac{1}{2} \gamma B N_y$$

Rectangular footing:-

$$q_{ult} = (1 + 0.3 \frac{B}{L}) C N_c + 1.3 q N_q + (1 - 0.2 \frac{B}{L}) \frac{1}{2} \gamma B N_y$$

(55)

Note:-

For pure cohesive soil ( $\phi = 0$ ),  $N_c = 5.7$ ,  $N_q = 1.0$ ,  $N_y = 0$

$$\sigma_{ult}(g) = c N_c + q(1) + 0$$

c-soils

$$\sigma_{net} = [c N_c + q] - q$$

$$\begin{aligned}\sigma_{net} &= c N_c \\ &\approx c \times 6\end{aligned}$$

$$\sigma_{net} \approx 6c$$

$$\sigma_{safe(Net)} = \frac{6c}{3} = 2c = U.C.S$$

$$c = \frac{U.C.S}{2}$$

$$2c = U.C.S$$

$\sigma_{safe(c\text{-soil})} = U.C.S$

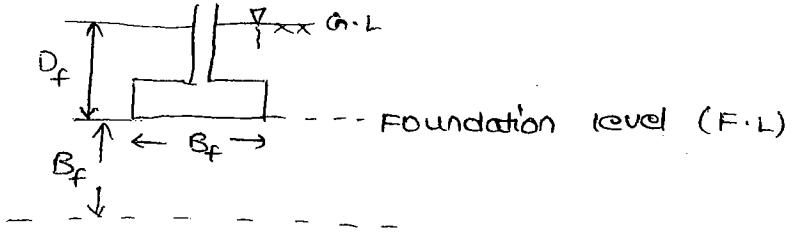
$\therefore$  Most of the soils Factor of Safety = 2 to 3.

$$\begin{aligned}\sigma_{net} &= [q \cdot N_q + \frac{1}{2} \gamma B N_y] - q \\ &= q(N_q - 1) + \frac{1}{2} \gamma B N_y\end{aligned}$$

$\sigma_{safe} = \frac{1}{F} (q(N_q - 1) + \frac{1}{2} \gamma B N_y)$ 
  
( $\phi$ -soil)

Effect of water table on Bearing capacity of soils :-

- Bearing capacity will not affect when water table is  $(D_f + B_f)$  from ground surface and above.



- If  $D_f + B_f$

$$R_{w_1} = R_{w_2} = 1$$

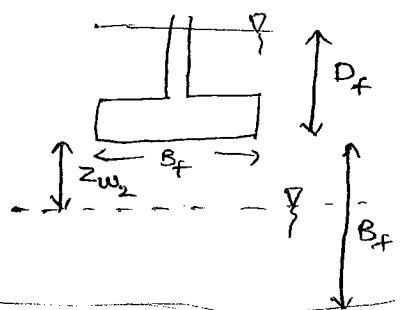
$$R_{w_2} = 0.5 \left( 1 + \frac{z_{w_2}}{B_f} \right)$$

- W.T is at F.L

$$R_{w_1} = 1 \quad R_{w_2} = 0.5$$

- W.T is at G.L

$$R_{w_1} = R_{w_2} = 0.5$$



$$\gamma_{sat} \times 0.5 = \gamma_{sat} = \gamma'$$

8-1-2015

UNIT - 17PILE FOUNDATION

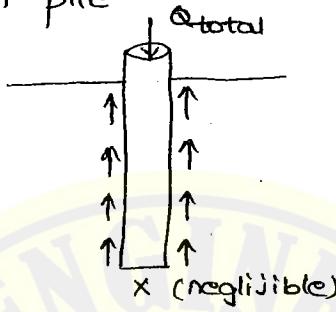
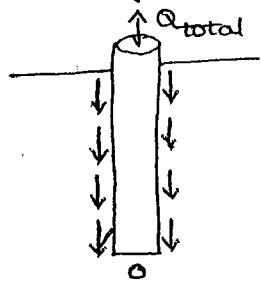
Classification of piles:-

a. Based on load transfer :-

i. End bearing piles

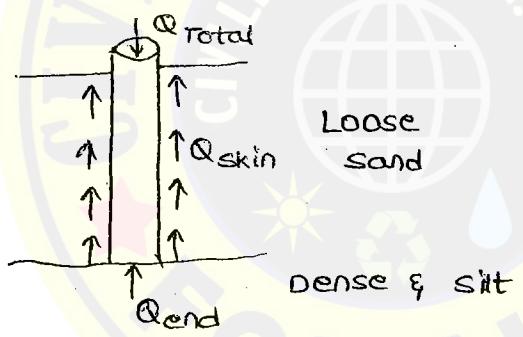
- No skin friction

2. Floating (or) friction pile



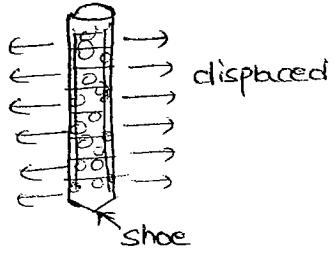
- No hard strata available in reasonable depth.

3. Combined end bearing and friction pile



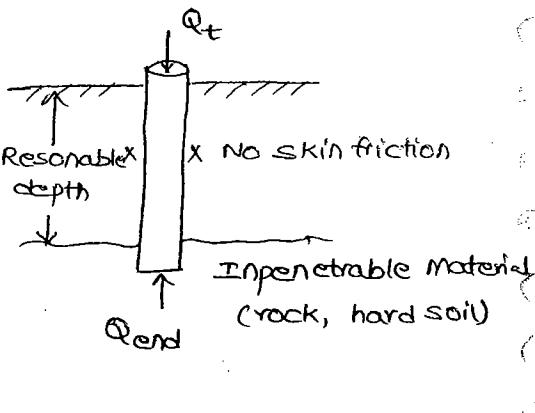
b. Based on method of installation:-

i. Driven and cast-in-situ piles:-



Load carry capacity of piles:-

1. Static formula
2. Dynamic formula
3. penetration test (SPT, CPT)
4. pile load test



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Static formula:-

a. piles in clay:-

$$Q_{ult} = Q_{end} + Q_{skin}$$

$$= (f_b) A_{tip} + (f_s) A_{surface}$$

$$= (c \cdot N_c) A_{tip} + (c \cdot \alpha) A_{surface}$$

 $\alpha$  = Adhesion factor (or)

Shear mobilised factor

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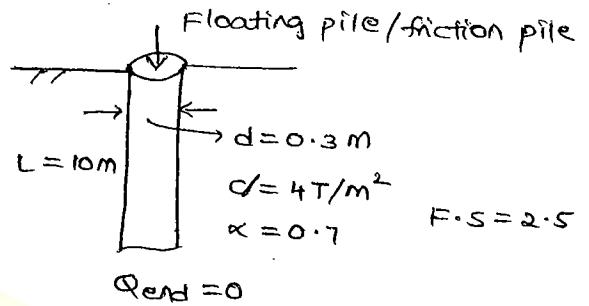
$$9. Q_{ultimate} = c \cdot \alpha \cdot A_{surface}$$

$$= 4 \times 0.7 \times \pi (0.3) 10$$

$$= 26.389 \text{ T}$$

$$Q_{safe} = \frac{Q_{ult}}{F.S} = \frac{26.389}{2.5}$$

$$= 10.55 \text{ T}$$



If top of the pile load is zero and end is given

$$Q_{ult} = Q_{end} + 0$$

$$= c N_c (A_s)$$

$$= 4 \times 9 \times \frac{\pi (0.3)^2}{4}$$

$$= 2.5 \text{ T}$$

$$Q_{safe} = \frac{2.5 \text{ T}}{2.5} = 1 \text{ T}$$

If both loads are given then  $Q_{safe} = 10.55 + 1 = 11.55 \text{ T}$ 

Ex:-

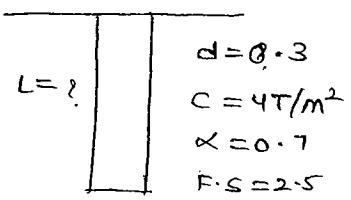
$$Q_{ult} = Q_{end} + Q_{skin}$$

$$Q_{ult} = 0 + Q_{skin}$$

$$(2.5 \times 25 \text{ T}) = c \alpha (\pi d L)$$

$$62.5 \text{ T} = 4 (0.7) (\pi \times 0.3 \times L)$$

$$L = 24 \text{ m}$$



$$\therefore Q_{safe} = \frac{Q_{ult}}{F.S}$$

b. Piles in sand:-

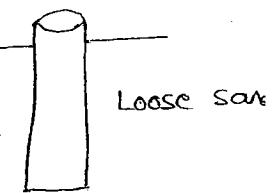
$$Q_{ult} = Q_{end} + Q_{skin}$$

$$= (f_b) A_{tip} + (f_s) A_{surface}$$

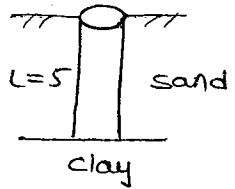
$$= (q'_{tip} \cdot N_q) A_{tip} + (K \cdot \tan \delta \cdot q'_{avg}) \cdot A_s$$

$$\phi, \frac{1}{\rho}$$

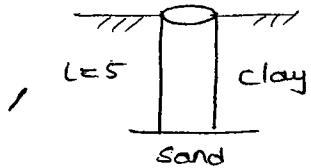
earth pressure coefficient

 $\delta$  = angle of wall friction $K = \frac{1}{\rho}$

Ex:- i)  $Q_{ult} = C N_c A_{tip} + \gamma \tan \phi q' A_s$



ii)  $Q_{ult} = C N_c A_s + \gamma \tan \phi q' A_{tip}$



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S. Given  $W = 12 \text{ kN}$   $h = 2 \text{ m}$   $s = 10 \text{ mm}$

$F.S = 6$  (assume)

$\eta_h = 1$  (assume) max

$c = 254 \text{ cm}$  for drop hammer

$$Q_s = \frac{W h \eta_h}{F(s+c)}$$

$$= \frac{12 \times 200 \times 1}{6(1+254)}$$

$$= 112.99 \text{ kN}$$

Group of piles:-

$$\text{Efficiency of pile group, } \eta_g = \frac{Q_g \times 100}{N \times Q_{s.p}}$$

Group capacity of piles in clay ( $Q_g$ ):-

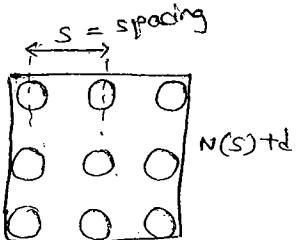
a. Individual failure:-

$$Q_{gi} = n \cdot Q_{s.p}$$

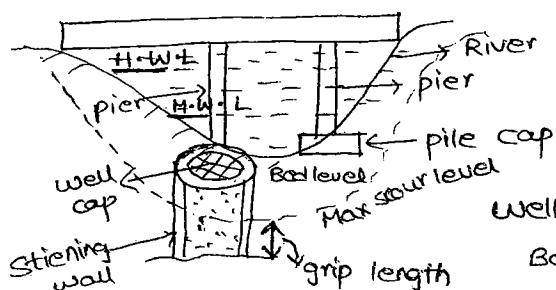
$$= n [(C_{tip} N_c) A_{tip} + (C_\infty) A_s] \rightarrow ①$$

$$Q_{group/block/pier} = C_{tip} \cdot N_c \cdot A_{block(tip)} + C_{avg} \cdot A_s(block) \rightarrow ②$$

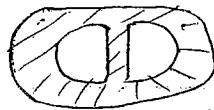
$$= C_{tip} \cdot N_c \cdot (N(s)+D)^2 + C_{avg} \cdot A_s(block)$$



Well foundation:-



Well cap is constructed at  
bed level of river

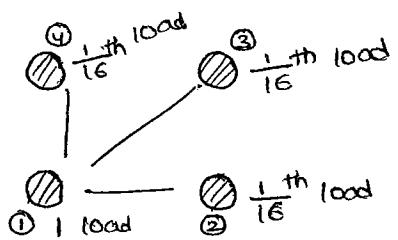


Double - D shape

(S7)

P.G NO:-96

6.



1<sup>st</sup> pile carry a load something '1'  
 2<sup>nd</sup> pile carry a  $\frac{1}{16}$ <sup>th</sup> of 1<sup>st</sup> pile  
 3<sup>rd</sup>, 4<sup>th</sup> also carry same  $\frac{1}{16}$ <sup>th</sup> load

$$\therefore 1 - 3 \left( \frac{1}{16} \right) \\ = \frac{16 - 3}{16} \\ = \frac{13}{16}$$